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**Exploiting the bulk-driven approach in CMOS analogue amplifier design**

**Yasutaka Haga**

School of Electronics and Computer Science

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EXPLOITING THE BULK-DRIVEN  
APPROACH IN CMOS ANALOGUE  
AMPLIFIER DESIGN



Yasutaka Haga

A thesis submitted in partial fulfilment of the requirements of the  
University of Westminster for the degree of  
Doctor of Philosophy

December 2011

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## Declaration

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I hereby declare that this thesis has been completed by myself and that the research documented is carried out entirely on my own. Where other sources of information have been used, they have been quoted. I have acknowledged all main sources of help.

No part of this thesis has been submitted in support of an application for any other degree.

Yasutaka Haga

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To Hiromi

*For her understandings, love and support*

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Yasutaka Haga

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## Abstract

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This thesis presents a collection of new novel techniques using the bulk-driven approach, which can lead to performance enhancement in the field of CMOS analogue amplifier design under the very low-supply voltage constraints. In this thesis, three application areas of the bulk-driven approach are focused – at the input-stage of differential pairs, at the source followers, and at the cascode devices.

For the input stage of differential pairs, this thesis proposes two new novel circuit design techniques. One of them utilises the concept of the replica-biased scheme in order to solve the non-linearity and latch-up issues, which are the potential problems that come along with the bulk-driven approach. The other proposed circuit design technique utilises the flipped voltage scheme and the Quasi-Floating Gate technique in order to achieve low-power high-speed performances, and furthermore the reversed-biased diode concept to overcome the issue of degraded input impedance characteristics that come along with the bulk-driven approach.

Applying the bulk-driven approach in source followers is a new type of circuit blocks in CMOS analogue field, in which to the author's best knowledge has not been proposed at any literatures in the past. This thesis presents the bulk-driven version of the flipped voltage followers and super source followers, which can lead to eliminating the DC level shift. Furthermore, a technique for programming the DC level shift less than the

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threshold voltage of a MOSFET, which cannot be achieved by conventional types of source followers, is presented.

The effectiveness of the cascode device using the bulk-driven approach is validated by implementing it in a complete schematics design of a fully differential bulk-driven operational transconductance amplifier (OTA). This proposal leads to solving the low-tranconductance problem of a bulk-driven differential pair, and in effect the open loop gain of the OTA exceeds 60dB using a 0.35 $\mu$ m CMOS technology.

The final part of this thesis provides the study result of the input capacitance of a bulk-driven buffer. To verify the use of the BSIM3 MOSFET model in the simulation for predicting the input capacitance, the measurement data of the fabricated device are compared with the post-layout simulation results.

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## List of Acronyms

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| <i>Name</i> | <i>Definition</i>                                  | <i>Section defined</i> |
|-------------|--|------------------------|
| BDCCM       | Bulk-Driven Cascoded Current Mirror                | 5.1.2                  |
| BDDRB       | Bulk-Driven Double Replica-Biased                  | 3.1.2                  |
| BDDP        | Bulk-Driven Differential Pair                      | 3.1.1, 5               |
| BDFVDP      | Bulk-Driven Flipped Voltage Differential Pair      | 3.2.3                  |
| BDFVF       | Bulk-Driven Flipped Voltage Follower               | 3.2.3, 4.1.3           |
| BDSSF       | Bulk-Driven Super Source Follower                  | 4.2.2                  |
| CMFB        | Common-Mode Feedback                               | 5.1.2                  |
| FVF         | Flipped Voltage Follower                           | 4.1.1                  |
| FVFDP       | Flipped Voltage Follower pseudo Differential Pair  | 3.2.2                  |
| GBW         | Gain-Bandwidth                                     | 3.2.4                  |
| ICMR        | Input Common-Mode Range                            | 2.1                    |
| ITRS        | International Technology Roadmap for Semiconductor | 1.1                    |
| JFET        | Junction Field Effect Transistor                   | 2.1                    |
| OTA         | Operational Transconductance Amplifiers            | 1.4, 3, 5              |
| PSRR        | Power Supply Rejection Ratio                       | 3.2.4, 5               |
| QFG         | Quasi-Floating Gate                                | 3.2.3, 4.2.2           |
| RBS         | Replica-Biased Scheme                              | 3.1.1                  |
| SR          | Slew-Rate  | 3.1.1, 4.2.2           |
| SSF         | Super Source Follower                              | 4.2.1                  |
| THD         | Total Harmonic Distortion                          | 4.1.4                  |

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## List of Symbols and Common MOSFET Equations

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As this thesis consists of various equations with many symbols, the meaning of variables and physical constants are listed below so that readers can refer easily. Also, common MOSFET equations and a general note about the symbol convention are provided. [SED11], [JOH97], [ALL02], [BAK08], [GRA01]

### **List of Symbols**

| <i>Symbols used<br/>in this thesis</i> | <i>Description</i>   | <i>Units</i>     |
|--|--|------------------|
| <b>Physical constants</b>              |  |                  |
| $\epsilon_0$                           | Permittivity of free space = $8.854 \times 10^{-14}$ F/cm  | F/cm             |
| $\epsilon_{Si}$                        | Permittivity of silicon = $11.7 \epsilon_0 = 1.036 \times 10^{-12}$ F/cm   | F/cm             |
| $\epsilon_{OX}$                        | Permittivity of SiO <sub>2</sub> = $3.97 \epsilon_0 = 3.52 \times 10^{-13}$ F/cm   | F/cm             |
| $k$                                    | Boltzmann's constant = $1.38 \times 10^{-23}$ J/K  | J/K              |
| $q$                                    | Charge of electron = $1.062 \times 10^{-19}$ C   | C                |
| $n_i$                                  | Intrinsic concentration of silicon = $1.45 \times 10^{10}$ /cm <sup>3</sup> at 300°K   | /cm <sup>3</sup> |
| <b>Temperature parameters</b>          |  |                  |
| $T$                                    | Temperature in degree Kelvin = 300°K at room temperature   | K                |
| $V_t$                                  | Thermal voltage (= 25.9mV at room temperature)<br>$V_t = \frac{kT}{q}$   | V                |
|  | <i>Note: In this thesis, the thermal voltage is represented by <math>V_t</math> (i.e. uppercase symbol with lowercase subscript), whereas the threshold voltage is represented by <math>V_T</math> (i.e. uppercase symbol with uppercase subscript).</i> |                  |

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| <b>Basic MOSFET parameters</b>      |  |                      |
|-------------------------------------|--|----------------------|
| $g_m$                               | Transconductance of a gate-driven MOSFET   | $\Omega^{-1}$        |
| $g_{mb}$                            | Transconductance of a bulk-driven MOSFET   | $\Omega^{-1}$        |
| $g_d$                               | Transconductance seen from the drain of a MOSFET   | $\Omega^{-1}$        |
| $t_{ox}$                            | Gate-oxide thickness (SPICE parameter = TOX)   | m                    |
| $C_{ox}$                            | Gate-oxide thickness (SPICE parameter = TOX)<br>$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$  | F/m <sup>2</sup>     |
| $\mu$                               | Carrier mobility (SPICE parameter = U0)  | cm <sup>2</sup> /V·s |
| $\lambda$                           | Channel-length modulation coefficient (SPICE parameter = LAMBDA)   | V <sup>-1</sup>      |
| <b>Threshold voltage parameters</b> |  |                      |
| $V_{T0}$                            | Zero-bias threshold voltage (SPICE parameter = VT0)  | V                    |
| $N_A, N_D$                          | Substrate doping (SPICE parameter = NSUB)<br>$N_A$ = Number of acceptors in the p-type semiconductor<br>$N_D$ = Number of donors in the n-type semiconductor | /cm <sup>3</sup>     |
| $\gamma$                            | $\gamma = \frac{\sqrt{2q\epsilon_{si}N_A}}{C_{ox}}$<br>= body-effect coefficient (or bulk-threshold) of p-type semiconductor                                 | V <sup>1/2</sup>     |
| $\gamma$                            | $\gamma = \frac{\sqrt{2q\epsilon_{si}N_D}}{C_{ox}}$<br>= body-effect coefficient (or bulk-threshold) of n-type semiconductor<br>(SPICE parameter = GAMMA)    | V <sup>1/2</sup>     |
| $2 \Phi_F $                         | $2 \Phi_F  = -V_t \ln(N_A/n_i)$ = Fermi potential of a p-type semiconductor  | V                    |
| $2 \Phi_F $                         | $2 \Phi_F  = V_t \ln(N_D/n_i)$ = Fermi potential of an n-type semiconductor<br>(SPICE parameter = PHI)   | V                    |

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| <b>MOSFET Diode Parameters</b>           |   |                  |
|--|---|------------------|
| $I_S$                                    | Body-junction saturation current density (SPICE parameter = JS)   | A/m <sup>2</sup> |
| $C_{J0}$                                 | Zero-bias body-junction capacitance, per unit area over the drain/source region (SPICE parameter = CJ)  | F/m <sup>2</sup> |
| MJ                                       | Grading coefficient, for area component (SPICE parameter = MJ)  |                  |
| $C_{Jsw0}$                               | Zero-bias body-junction capacitance, per unit length along the sidewall (periphery) of the drain/source region (SPICE parameter = CJSW)   | F/m              |
| MJSW                                     | Grading coefficient, for sidewall component (SPICE parameter = MJSW)  |                  |
| $V_0$                                    | Built-in voltage of an open-circuit pn junction, also known as bulk junction potential or barrier potential (SPICE parameter = PB)<br>$V_0 = V_t \ln\left(\frac{N_A N_D}{n_i^2}\right)$ | V                |
| <b>MOSFET Dimension Parameters</b>       |   |                  |
| AS, AD                                   | Areas for source and drain (SPICE parameter = AS, AD)   | m <sup>2</sup>   |
| PS, PD                                   | Perimeters for source and drain (SPICE parameter = PS, PD)  | m                |
| <b>MOSFET Gate-Capacitance Parameter</b> |   |                  |
| $C_{GSO}$                                | Gate-source overlap capacitance, per unit channel width (SPICE parameter = CGSO)  | F/m              |

---

## MOSFET Equations

### *Large-signal operation*

|       | Linear Region   | Saturated Region   |
|-------|---|--|
| $I_D$ | $I_D = \mu_0 C_{OX} \frac{W}{L} (V_{GS} - V_T - \frac{V_{DS}}{2}) V_{DS}$ | $I_D = \frac{\mu_0 C_{OX}}{2} \frac{W}{L} (V_{GS} - V_T)^2 (1 + \lambda V_{DS})$ |
| $V_T$ | $V_T = V_{T0} + \gamma (\sqrt{2 \Phi_F  + v_{SB}} - \sqrt{2 \Phi_F })$    |  |

### *Small-signal operation*

|   | Linear Region   | Saturated Region  |
|---|---|---|
| $g_m = \frac{\partial i_d}{\partial v_{gs}}$    | $\beta V_{DS} = \mu_0 C_{OX} \frac{W}{L} V_{DS}$  | $\mu_0 C_{OX} \frac{W}{L} (V_{GS} - V_T) (1 + \lambda V_{DS})$<br>$= \sqrt{2\mu_0 C_{OX} \frac{W}{L} I_D} (1 + \lambda V_{DS})$ |
| $g_{mb} = \frac{\partial i_d}{\partial v_{bs}}$ | $\eta g_m = g_m \frac{\gamma}{2\sqrt{2 \Phi_F  + V_{SB}}}$  |   |
| $g_d = \frac{\partial i_d}{\partial v_{ds}}$    | $\beta (V_{GS} - V_T - V_{DS})$   | $I_D \lambda$   |
| $C_{gs}$  | $C_{gs} = \frac{2}{3} W L C_{OX} + W C_{GSO}$   |   |
| $C_{bd}$  | $\frac{C_{j0}}{(1 - \frac{V_{BS}}{V_0})^{MJ}} AS + \frac{C_{jSW0}}{(1 - \frac{V_{BS}}{V_0})^{MJSW}} PS$ |   |
| $C_{ds}$  | $\frac{C_{j0}}{(1 - \frac{V_{BD}}{V_0})^{MJ}} AS + \frac{C_{jSW0}}{(1 - \frac{V_{BD}}{V_0})^{MJSW}} PS$ |   |
| $f_T$   | $\frac{g_m}{2\pi(C_{gs} + C_{gd} + C_{gb})}$  |   |

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## **Symbol Convention**

Unless otherwise stated, the following symbol convention is used to represent signals in this thesis:

| <b><i>Represented Symbol</i></b>                                | <b><i>Meaning</i></b>  |
|---|--|
| Uppercase symbols with<br>uppercase subscripts<br>(e.g. $I_D$ ) | Bias or DC quantities<br>(e.g. the DC portion of transistor drain current)                                       |
| Lowercase symbols with<br>lowercase subscripts<br>(e.g. $i_d$ ) | Small-signal quantities<br>(e.g. the incremental change in transistor drain current)                             |
| Lowercase symbols with<br>uppercase subscripts<br>(e.g. $i_D$ ) | Sum of bias and small-signal quantities<br>(e.g. the total transistor drain current,<br>i.e. $i_D = I_D + i_d$ ) |

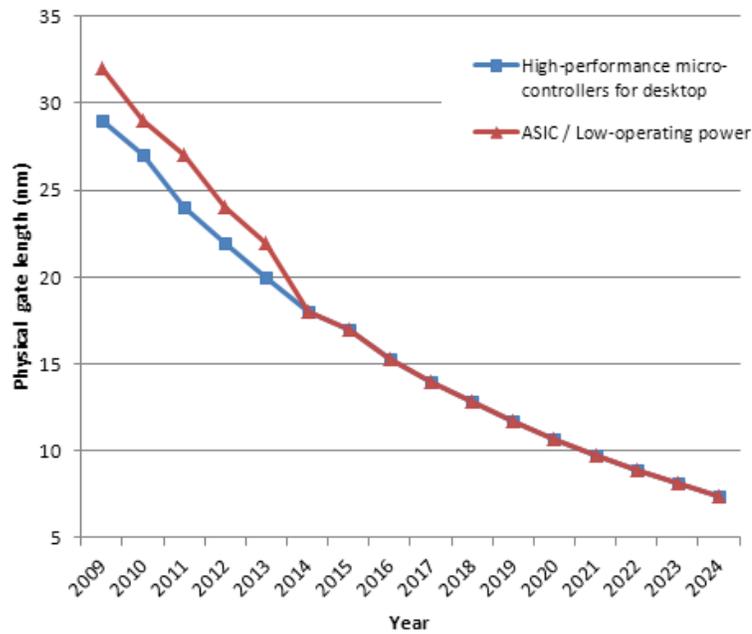
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## Chapter 1 Introduction

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### ***1.1 Moore's Law and More***

Complementary Metal-Oxide Semiconductor (CMOS) technology is continuously downscaling to increase the number of Metal-Oxide-Semiconductor Field Effect Transistors (MOSFET) to be integrated in a single chip. Intel co-founder Gordon E. Moore postulated the trend in 1965, which is known as Moore's Law, that the number of transistors per chip doubles roughly every 2 years [MOR65]. Along with this integration level trend, the cost-per-function is decreased and thus economic productivity and in effect overall quality of life are significantly improved through proliferation of computers, communication, and other industrial and consumer electronics [ITR10]. This miniaturisation trend, however, cannot be continued forever. Semiconductors are getting harder to downscale, and eventually the level of integration would not scale with Moore's Law anymore. Figure 1-1 shows how the International Technology Roadmap for Semiconductor (ITRS) draws the CMOS technology roadmap for the next decades.



**Figure 1-1 CMOS Technology Roadmap [ITR10]**

In order to keep up responding to the requirements in the economy growth and improving the quality of life despite the scaling limits according to Moore’s Law which would come in the next decade, the ITRS has addressed a new concept of research target called “Moore’s Law and More”. This concept is constructed by three sub-sets of focus area – *scaling*, *functional diversification*, and *beyond CMOS*. *Scaling* (which is also known as *more Moore*) refers to not only the continued shrinking of transistors but also includes non-geometrical process techniques such as study of new materials that affect the electrical performance of the chip, as well as design technologies that enable high performance, low power, high reliability, low cost, and high design productivity. *Functional diversification* (which is also known as *more than Moore*) aims to provide additional value, in particular non-digital functionalities (e.g. RF communication), to be migrated from the system board level into package-level (system-in-package, SiP) or chip-level (System-on-Chip, SoC). *Beyond CMOS* focuses on a “new switch” that can provide substantial functional scaling beyond that attainable by ultimately scaled CMOS. In the field of *Beyond CMOS*, the ITRS lists some examples like carbon-based nano-electronics, spin-based

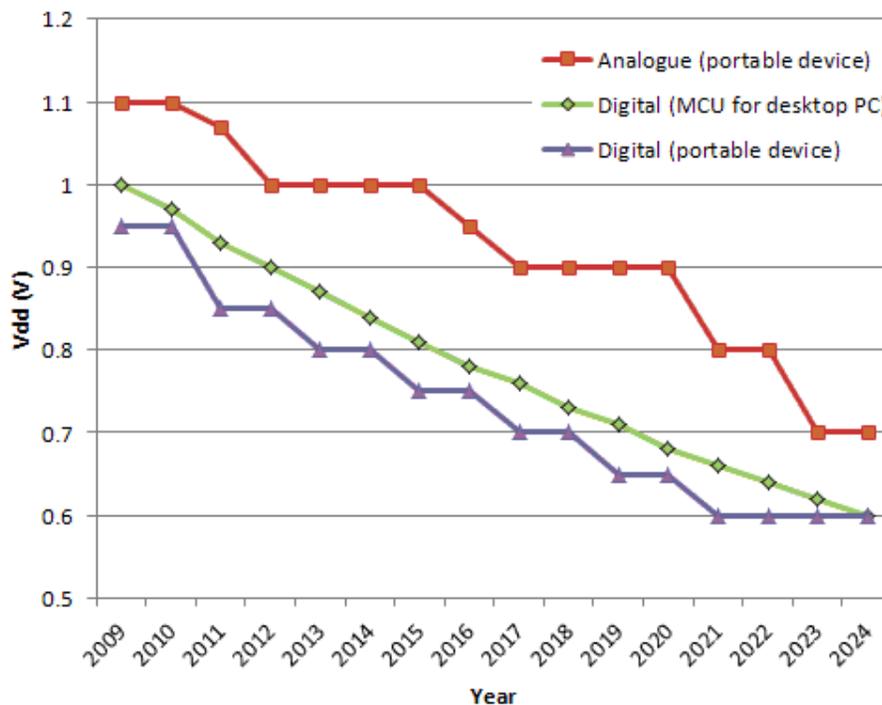
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devices, ferromagnetic logic, atomic switches, and nano-electro-mechanical-system (NEMS) switches.

This CMOS technology trend introduces a new issue and consequently a motivation of new development in the area of CMOS analogue circuit design, which is described in the next section.

### ***1.2 Supply Voltage Trend***

Along with the scaling trend of CMOS technology, the ITRS set the target of research effort towards lowering of supply voltages, since small transistors suffer from reduced voltage breakdowns (which is known as hot carrier effect) [ITR10]. Figure 1-2 shows how the ITRS draws the roadmap of supply voltage reduction for analogue and digital systems.



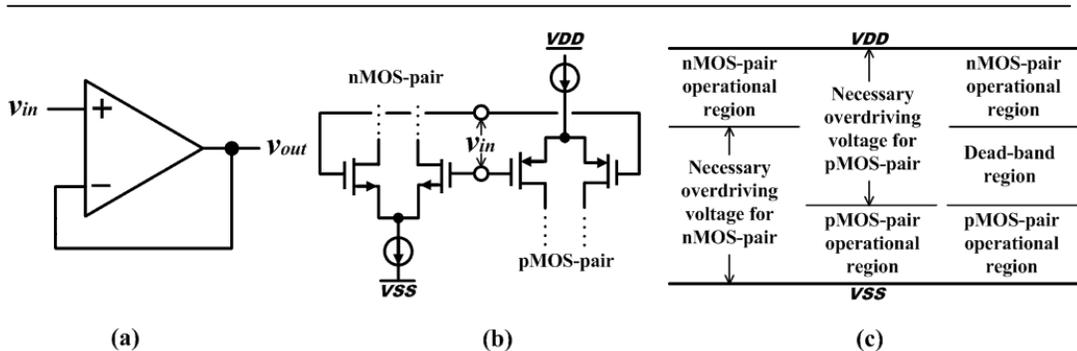
**Figure 1-2 Supply Voltage Reduction Roadmap [ITR10]**

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With Figure 1-2, the ITRS describes that the supply voltage reduction for analogue systems will continue to lag that of digital systems by two or more generations, due to the fact that the threshold voltage for CMOS technology is not expected to be decreased drastically. In digital systems, a threshold voltage too close to zero would cause appreciable leakage current to flow into logic devices even when they are off, which would result to increased power dissipation as the leakage current gets multiplied by the number of logic devices integrated in the digital system [ALL02]. Thus, from this reason the threshold voltage cannot be significantly reduced, which causes an issue from analogue circuit designers' viewpoint since conventional design techniques cannot fit into the ITRS roadmap. There is a need for new development of analogue circuit design techniques to overcome this dilemma.

### ***1.3 Rail-to-Rail Analogue Voltage Buffer and the Bulk-Driven Approach***

One particular example where new circuit design techniques are needed for low-voltage systems is analogue voltage buffers. Voltage buffers, which are usually constructed with an operational amplifier (op-amp) in unity-gain voltage configuration as illustrated in Figure 1-3(a), are essential building blocks for applications where the weak signal needs to be delivered to a large capacitive or a small resistive load without being distorted. In order to maximise the dynamic range under the low supply voltage constraint, rail-to-rail input and output stages are required for those op-amps.



**Figure 1-3 (a) Op-amp in unity-gain configuration, (b) complementary differential pair, and (c) illustration describing dead-band region under low-supply voltage condition**

For the input stage, the conventional circuit design approach for achieving rail-to-rail operation has been to utilise both p-type (pMOS) and n-type (nMOS) of the differential pairs as shown in Figure 1-3(b). However, as illustrated in Figure 1-3(c), the supply voltage being too low would cause a dead-band of the operational area where neither pMOS nor nMOS pairs can detect the input. In order to operate with this conventional circuit design approach, its supply voltage needs to be much greater than  $2V_T + 2V_{DSmin}$ , where  $V_T$  is the threshold voltage of the MOSFET and  $V_{DSmin}$  is the minimum required voltage of drain-to-source voltage of the MOSFET. Considering that  $V_T$  varies by the bulk (or body) biasing voltage, the chip (or junction) temperature, and the process variation for the CMOS technology, a new circuit design approach such that the rail-to-rail operation can be achieved with a supply voltage near  $V_T$  is rather in favour for the ITRS roadmap.

A candidate of circuit design techniques that can achieve rail-to-rail input operation with low supply voltages is the bulk-driven approach, which utilises the bulk of the MOSFET instead of the gate for applying the signal. Figure 1-4 illustrates this approach. With this technique the amount of supply voltage can be reduced to near  $V_T$ , however many drawbacks have been reported in [BLA98]. The author's research work solely focuses on the bulk-driven approach in order to develop new circuit design techniques that can overcome those drawbacks.

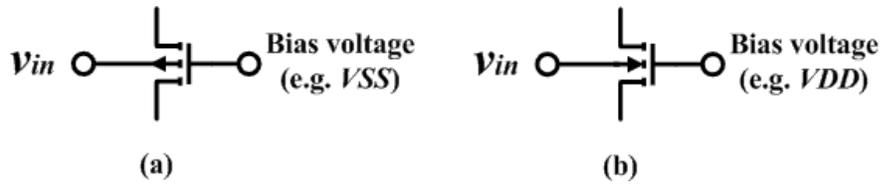


Figure 1-4 (a) pMOS bulk-driven device, and (b) nMOS bulk-driven device

## 1.4 Research Objective and Thesis Outline

The research theme reported in this thesis is the bulk-driven approach. The research objective is to develop new circuit design techniques using the bulk-driven approach that can overcome many of those drawbacks which have been reported by literatures, and furthermore invent new ways application areas of the bulk-driven approach that can lead to performance enhancement in the field of CMOS analogue amplifier design. This thesis is structured as follows:

Chapter 2 provides a general overview of the bulk-driven approach. The device physics, operation principle and mathematical modelling, and drawbacks of this circuit design approach are discussed.

Chapter 3 focuses on the circuit design techniques of rail-to-rail input stage for analogue amplifiers using the bulk-driven approach. This chapter reviews previous works and proposes a novel new circuit design technique that solves the issues of nonlinearity and latch up. Furthermore, another new circuit design technique that can achieve low-power high-speed performances whilst minimise the issue of low-input resistance large input capacitance of the bulk-driven approach is also proposed.

Chapter 4 presents a new invention of designing source followers using the bulk-driven approach, which in author's best knowledge has not been proposed in

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literatures before. A new design technique of source followers such that the DC level shift can be freely programmed is proposed in this chapter.

Chapter 5 proposes a new way of utilising the bulk of the cascode devices at the output stage of Operational Transconductance Amplifiers (OTA), which leads to enhanced output resistance without having any additional hardware in the core part of the OTA.

Chapter 6 focuses on the study of the input capacitance of a bulk-driven buffer. To verify the use of the BSIM3 MOSFET model in the simulating for predicting the input capacitance, the measurement data of the fabricated device compared with the simulated results using the extracted netlist of the postlayout design.

Chapter 7 is the concluding session of this research work. The summary of this work and the author's recommendations for further work are provided.

Lastly, Appendix A provides the copies of the author's publications, Appendix B provides the supplementary information to Chapter 6 (including the SPICE code used for the simulation, the IC layout of the whole die and the bonding diagram, more snapshots of the microphotograph, and the used test board for the measurement), and Appendix C lists the logs of the measurement results of the input capacitance of the fabricated bulk-driven buffer presented in Chapter 6.

### ***1.5 List of the Author's Publications***

The author's research works documented in this thesis are based on the following publications:

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- [HAG05] Y. Haga, H. Zare-Hoseini, L. Berkovi, and I. Kale, “Design of a 0.8 Volt Fully Differential CMOS OTA Using the Bulk-Driven Technique”, *IEEE Proc. International Symposium in Circuits and Systems*, 2005, pp. 220 – 223
- [HAG06] Y. Haga, R. C. S. Morling, and I. Kale, “A New Bulk-Driven Input Stage Design for sub 1-volt CMOS Op-Amps”, *IEEE Proc. International Symposium in Circuits and Systems*, 2006, pp.1547 – 1550
- [HAG09A] Y. Haga and I. Kale, “Bulk-Driven Flipped Voltage Follower”, *IEEE Proc. International Symposium in Circuits and Systems*, 2009, pp.2717 – 2720
- [HAG09B] Y. Haga and I. Kale, “CMOS Buffer Using Complementary Pair of Bulk-Driven Super Source Followers”, *IEEE Electronic Letters*, Vol. 45, Issue 18, 2009, pp. 917 – 918
- [HAG09C] Y. Haga and I. Kale, “Class-AB Rail-to-Rail CMOS Buffer with Bulk-Driven Super Source Followers”, *IEEE European Conference on Circuit Theory and Design*, 2009, pp. 695 – 698
- [HAG10] Y. Haga and I. Kale, “Bulk-Driven Flipped Differential Pair”, *IEEE Proc. PhD Research in Microelectronics and Electronics*, 2010
- [HAG11] Y. Haga and I. Kale, “Bulk-Driven DC Level Shifter”, *IEEE Proc. International Symposium in Circuits and Systems*, 2011, pp.2039-2042

The knowledge contributions of the above publications are summarised in the next section.

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## ***1.6 Knowledge Contributions***

The work presented in this thesis, which includes several novel proposals of circuit design techniques that utilise the bulk-driven approach, is solely developed by the author. The novelties of these developed techniques, which greatly help enhancing performances in the CMOS analogue amplifier design field, are described below:

Applying the proposal at the input stage of CMOS analogue amplifiers not only leads to providing rail-to-rail operation at extremely low supply voltage condition, but also improves the linearity and furthermore enhances the latch up immunity [HAG06]. In fact there are several previously proposed works that improve the linearity of the bulk-driven approach, however in the author's best knowledge there is no publication of the technique that can enhance the latch up immunity.

This thesis also presents another input stage design technique utilising the bulk-driven approach, which achieves low-power high-speed performances and helps reducing the input capacitance [HAG10]. A new concept of utilising a reversed-biased diode with the bulk-driven MOSFET is introduced.

Applying the bulk-driven approach in source follower design is a complete new way of circuit design techniques. The bulk-driven approach allows the DC level shift to be freely programmed, which has not been possible to do with conventional source followers [HAG09A], [HAG09B], [HAG09C], [HAG11].

Utilising the bulk-driven approach in the cascode devices of the OTA is also a complete new design method, which leads to increasing the output resistance and

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hence enhancing the open-loop gain of the OTA without the need of any extra hardware in the core part of the OTA [HAG05].

With the above contributions to knowledge, the author aims to make for the readers of this thesis to realise that the bulk-driven approach has many new possible ways to be applied in CMOS analogue amplifier design for further performance improvement, and to encourage for new researchers to continue with developing modified techniques of the bulk-driven approach.

### ***1.7 Impact of this Work***

This last section of the Chapter aims to demonstrate the impact of this research work.

During the research activities, the author noticed that the work reported in this thesis has been cited by several institutions' works. Section 1.7.1 shows the list of citations to the author's publications which the author is aware of.

The BDFVDP reported in Chapter 3 of this thesis, which is the work the author published in [HAG10], received the Gold Leaf Certificate from PhD Research In Microelectronics and Electronics (PRIME). In Section 1.7.2, the scanned copy of the received award is shown.

#### **1.7.1 The List of "Referred" Publications**

*The List of Citations to [HAG05]*

- 
- [AGG09] B. Aggarwal and M. Gupta, “Low-Voltage Cascode Current Mirror based on Bulk-Driven MOSFET and FGMOS techniques”, *IEEE Proc. International Conference on Advances in Recent Technologies in Communication and Computing*, 2009, pp. 474 – 477
- [BAU07] F. Bautista, S. O. Martínez, G. Dieck, and O. Rossettoy, “An ultra-low voltage high gain operational transconductance amplifier for biomedical applications”, *Workshop on Design and Architectures for Signal and Image Processing (DASIP)*, 2007, Grenoble: France
- [CAR09] J. M. Carrillo, R. Pérez-Aloe, J. M. Valverde, and J. F. Duque-Carrillo, “Compact Low-Voltage Rail-to-Rail Bulk-Driven CMOS Opamp for Scaled Technologies”, *IEEE Proc. European Conference on Circuits Theory and Design*, 2009, pp. 263 – 266
- [CAR10] J. M. Carrillo, G. Torelli, R. Pérez-Aloe, J. M. Valverde, and J. F. Duque-Carrillo, “Single-pair bulk-driven CMOS input stage: A compact low-voltage analog cell for scaled technologies” *Integration, the VLSI Journal*, 2010, Vol.43, Issue 3, pp. 251 – 257, Elsevier
- [CAR11] J. M. Carrillo, G. Torelli, M. A. Domínguez, and J. F. Duque-Carrillo, “On the input common-mode voltage range of CMOS bulk-driven input stages”, *International Journal of Circuit Theory and Applications*, 2011, 39, pp. 649 – 664, Wiley Online Library
- [CHA10] C. Chanapromma and K. Daoden, “A CMOS Fully Differential Operational Transconductance Amplifier Operating in Sub-threshold Region and Its Application”, *IEEE Proc. International Conference on Signal Processing Systems*, 2010, pp. V2-73 – V2-77

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- [HE06] X-Y He, K-P Pun, C-S Choy, and C-F Chan, "A 0.5V Fully Differential OTA with Local Common Feedback", *IEEE Proc. International Symposium on Circuits and Systems*, 2006, pp. 1559 – 1562
- [KHA10] H. Khomeh and H. Shamsi, "A Sub-1V High-Gain Two-Stage OTA Using Bulk-Driven and Positive Feedback Techniques", *IEEE Proc. European Conference on Circuits and Systems for Communications*, 2010, pp. 103 – 106
- [LAY08] K. D. Layton, D. T. Corner, and D. J. Corner, "Bulk-driven gain-enhanced fully-differential amplifier for  $V_T + 2V_{dsat}$  operation", *IEEE Proc. International Symposium on Circuits and Systems*, 2008, pp. 77 – 80
- [LI10] Y. Li, C. C. Y. Poon, and Y-T Zhang, "Analog Integrated Circuits Design for Processing Physiological Signals", *IEEE Reviews in Biomedical Engineering*, 2010, Vol. 3, pp. 93 – 105
- [PAN09] S-W Pan C-C Chuang C-H Yang and Y-S Lai, "A novel OTA with dual bulk-driven input stage", *IEEE Proc. International Symposium on Circuits and Systems*, 2009, pp. 2721 – 2724
- [RAI10] G. Raikos and S. Vlassis, "0.8 V Bulk-Driven Operational Amplifier", *Analog Integrated Circuits and Signal Processing*, 2010, 63, pp. 425 – 432, Springer
- [ROH10] H. Roh, H. Lee, Y. Choi, and J. Roh, "A 0.8-V 816-nW delta-sigma modulator for low-power biomedical applications", *Analog Integrated Circuits and Signal Processing*, 2010, 63, pp. 101 – 106, Springer
- [TAI06] C-F Tai, J-L Lai, and R-J Chen, "Using Bulk-driven Technology

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Operate in Subthreshold Region to Design a Low Voltage and Low Current Operational Amplifier”, *IEEE Proc. International Symposium on Consumer Electronics*, 2006, pp. 1 – 5

- [ZAB07] S. A. Zabihian, and R. Lotfi, “Ultra-Low-Voltage, Low-Power, High-Speed Operational Amplifiers Using Body-Driven Gain-Boosting Technique”, *IEEE Proc. International Symposium on Circuits and Systems*, 2007, pp. 705 – 708

*The List of Citations to [HAG06]*

- [CAR11] J. M. Carrillo, G. Torelli, R. Pérez-Aloe, J. M. Valverde, and J. F. Duque-Carrillo, “On the input common-mode voltage range of CMOS bulk-driven input stages”, *International Journal of Circuit Theory and Applications*, 2011, 39, pp. 649 – 664, Wiley Online Library
- [LI10] Y. Li, C. C. Y. Poon, and Y-T Zhang, “Analog Integrated Circuits Design for Processing Physiological Signals”, *IEEE Reviews in Biomedical Engineering*, 2010, Vol. 3, pp. 93 – 105
- [RAI10] G. Raikos and S. Vlassis, “0.8 V Bulk-Driven Operational Amplifier”, *Analog Integrated Circuits and Signal Processing*, 2010, 63, pp. 425 – 432, Springer

*The List of Citations to [HAG09A]*

- [KHA11] F. Khatib, N. Khatib, and D. Kubánek, “Novel low-voltage low-power high-precision  $CCII_{\pm}$  based on bulk-driven folded cascade

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- OTA”, *Microelectronics Journal*, 2011, 42, pp. 622 – 631, Elsevier
- [RAI10] G. Raikos and S. Vlassis, “0.8 V Bulk-Driven Operational Amplifier”, *Analog Integrated Circuits and Signal Processing*, 2010, 63, pp. 425 – 432, Springer
- [YOD10] A . Yodtean, P. Isarasena, and A. Thanachayanont, “0.8- $\mu$ W CMOS Bulk-Driven Linear Operational Transconductance Amplifier in 0.35- $\mu$ m Technology”, *IEEE Proc. Asia Pacific Conference on Circuits and Systems*, 2010, pp. 784 – 787

*The List of Citations to [HAG09B]*

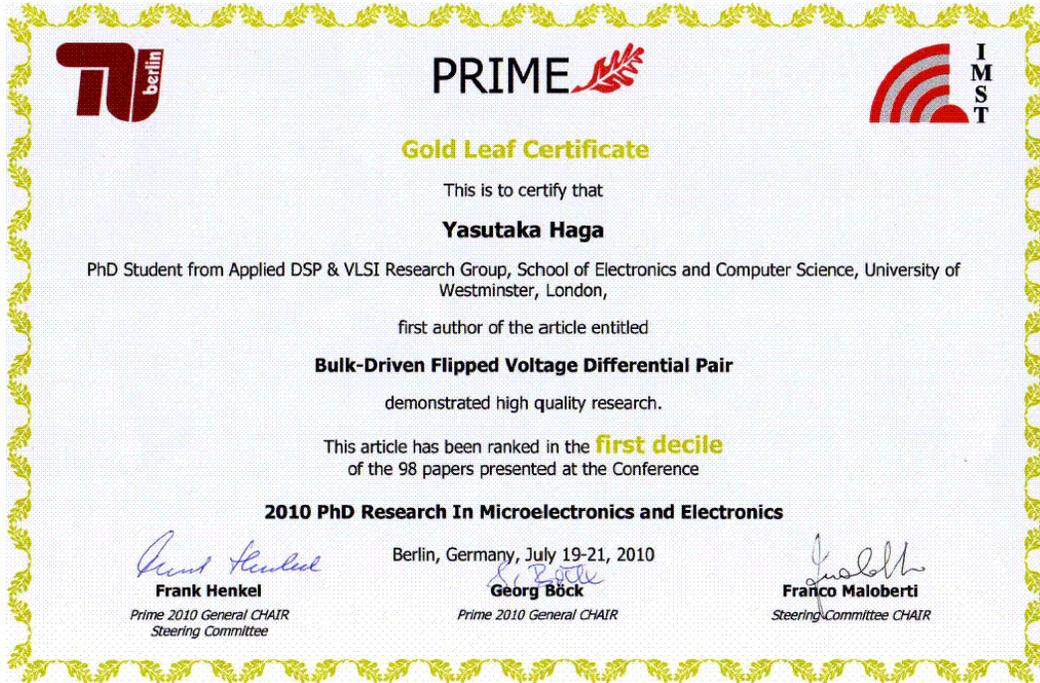
- [URB11] C. Urban, J. E. Moon, and P.R. Mukund, “Scaling the Bulk-Driven MOSFET into Deca-Nanometer Bulk CMOS Processes”, *Microelectronics Reliability Journal*, 2011, 51, pp. 727 – 732, Elsevier

*The List of Citations to [HAG09C]*

- [KUM11] M. Kumar and G. Kumar, “Optimization Techniques for Source Follower Based Track-and-Hold Circuit for Wireless High Speed Wireless Communication”, *AIRCC International Journal of VLSI design & Communication Systems*, 2011, Vol.2, No. 1, pp. 45 – 59
- [MAR11] A. L. Martin, J. M. A. Miguel, L. Acosta, J. Ramírez-Angulo, and R. G. Carvajal, “Design of Two-Stage Class AB CMOS Buffers: A Systematic Approach”, *ETRI Journal*, 2011, Vol.33, No.3, pp. 393 - 400

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## 1.7.2 The Scanned Copy of the Gold Leaf Certificate Awarded by PRIME'10



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## Chapter 2 Characterising the Bulk-Driven Approach

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This chapter provides an overview of the bulk-driven approach, which is essential to be understood in prior to assessing the bulk-driven circuit design. The benefit of the bulk-driven approach, the device realisation in CMOS technology, and the drawbacks are thoroughly discussed.

### 2.1 The Benefit of Utilising the Bulk-Driven Approach

The benefit of the bulk-driven approach can be easily realised by simulating its transconductance characteristics and comparing with the gate-driven approach. Figure 2-1 shows the simulated plot of the gate-driven and the bulk-driven nMOS transistors using a  $0.35\mu\text{m}$  CMOS technology.

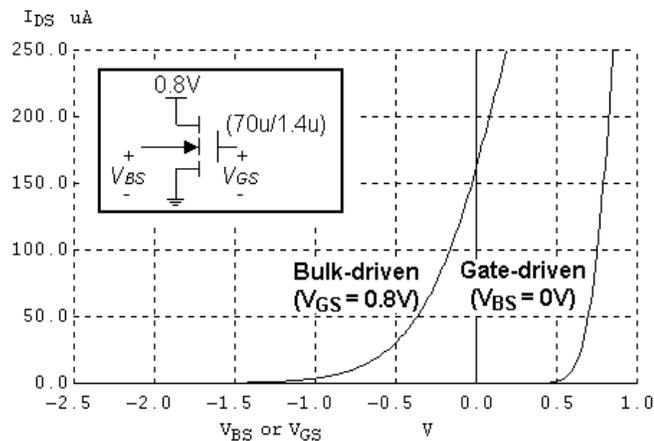


Figure 2-1 Simulating transconductance characteristics of gate-driven and bulk-driven nMOS transistors using a  $0.35\mu\text{m}$  CMOS technology

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As can be seen in Figure 2-1, to operate the gate-driven MOS transistor in the active region, the gate-to-source voltage needs to be greater than the threshold voltage (which is approximately 0.6 volts in this case). On the other hand, the bulk-driven MOS transistor behaves in a similar fashion to a depletion MOS transistor or a Junction Field Effect Transistor (JFET). Therefore, with the zero-bias voltage at the input node, the transistor is still in the active region.

This characteristic is the key benefit we use in designing low-supply voltage op-amps and other analogue circuits, as the bulk-driven device allows an extension in its input range on the negative side and hence leads to improving the Input Common-Mode Range (ICMR).

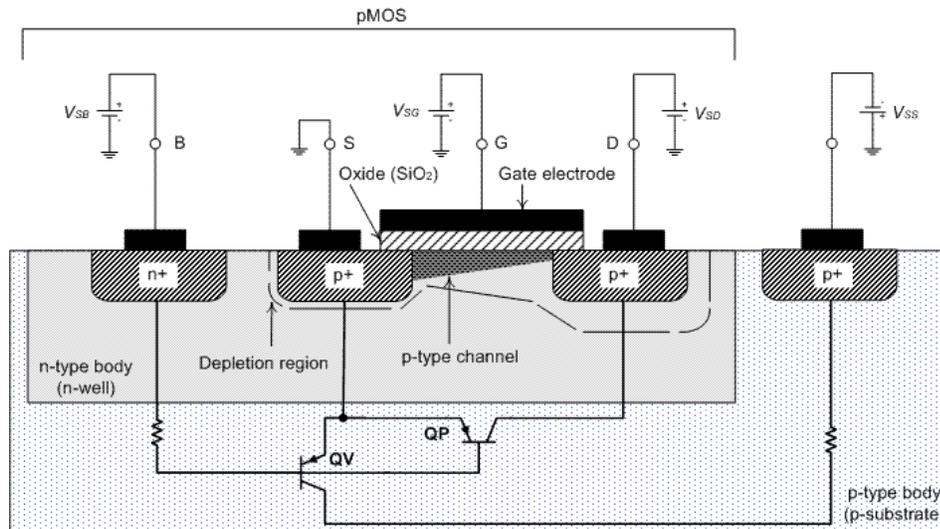
## ***2.2 Realising the Bulk-Driven Device in CMOS Technology***

This section describes how a bulk-driven device is realised in CMOS technology, which is an important topic to be covered before discussing the drawbacks of the bulk-driven approach. Case studies of the realisation in n-well type and in twin-well type of CMOS technologies are discussed.

### **2.1.1 Bulk-Driven Device Realised in N-Well CMOS Technology**

In semiconductor market today n-well CMOS technologies are more popular than p-well types, since n-types ones allows the substrate to be connected to the ground instead of the supply voltage, which is in more favour by circuit designers [SAN06], [YTT03]. Thus, it is essential to discuss the realisation of a bulk-driven device in n-well CMOS technology.

In n-well CMOS technology, pMOS can be bulk-driven. Figure 2-2 illustrates the cross sectional view of how the pMOS bulk-driven device can be realised in an n-well CMOS technology.



**Figure 2-2 Cross sectional view of a bulk-driven pMOS device in an n-well CMOS technology**

The operation principle of a bulk-driven device is simple to follow. The voltage at the bulk affects the depletion region depicted in Figure 2-2, which in effect controls the channel and hence the drain current. Let's suppose that the pMOS device formed in the n-well in Figure 2-2 is in linear region, and thus the depth of the p-type channel is narrower at the drain than the source, as shown in the sketch. As the voltage potential at the bulk of the pMOS device is increased above the source, the depletion region becomes widened and hence the p-type channel reduces its overall depth, and eventually the channel is pinched off at the drain end so that the pMOS device becomes saturated [ALL02].

The behaviour of the reduced channel depth can be alternatively described that the overvoltage of the pMOS device is decreased when the bulk voltage increases above the source voltage  $V_{SB}$  [SED11]. However, since the gate voltage of the pMOS

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device  $V_{SG}$  remained unchanged, the threshold voltage  $V_T$  increased instead. This  $V_T$  behaviour can be mathematically modelled by:

$$V_T = V_{T0} + \gamma(\sqrt{2|\Phi_F| + V_{SB}} - \sqrt{2|\Phi_F|}) \quad (2-1)$$

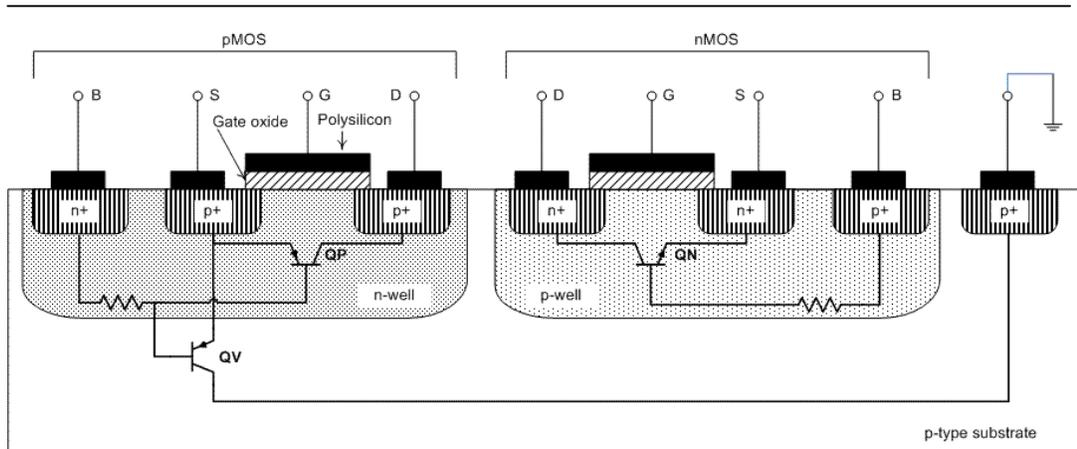
where  $V_{T0}$  is the threshold voltage at zero-bias (i.e.  $V_{SB}=0$ ),  $\gamma$  is the body-effect coefficient, and  $2|\Phi_F|$  is the Fermi potential, which are all dependent of the CMOS technology. Hence in summary, with the bulk-driven approach the drain current is controlled by varying  $V_T$  instead of  $V_{SG}$ .

From Figure 2-2 it is important to realise the parasitic bipolar effect, which are denoted as QP and QV in the sketch, since this parasitic effect contributes to one of the severe drawbacks of the bulk-driven approach. More detail discussions of this drawback is covered in Section 2.3.

Finally, it is worth adding a comment that a bulk-driven transistor is often said to be in *depleted-mode* [BLA96] since the voltage potential at the bulk affects the shape of the depletion region. However, in terms of device physics the actual MOS transistor that is dealt with is enhancement type, thus this discussion may cause confusion by first-time learners of the bulk-driven approach.

### **2.1.2 Bulk-Driven Device Realised in Twin-Well CMOS Technology**

Since twin-well CMOS technology is also available today, it is also worth discussing how a bulk-driven device can be realised in this technology. The cross section view is sketched in Figure 2-3.



**Figure 2-3 Cross sectional view of twin-well CMOS technology**

In the previous section it was discussed that only pMOS can be bulk-driven in n-well technology. In twin-well technology, on the other hand, nMOS device can also be bulk-driven since the device has an isolated body (bulk) in p-well instead of the common p-substrate.

As can be observed from Figure 2-3, the parasitic bipolar effect for the pMOS formed in twin-well technology remains in identical manner as the pMOS device formed in n-well technology. This is because, in either case, the n-well is formed in p-substrate. In contrast, with the nMOS there is only one type of bipolar effect denoted by QN. This is because p-well and p-substrate are not related by pn-junction effect since they both have the p-type of polarity.

It is worth noting that this technology allows separate optimization of the nMOS and pMOS transistors [SED11], and therefore many submicron processes are based on this technology. As mentioned before, with this technology both pMOS and nMOS devices can be bulk-driven. However for fabless semiconductor companies where the fabrication needs to be outsourced, there might be a case that the foundry allows layout designers to draw only n-well layers but not p-well layers [MOS11], which consequently means that layout designers cannot assign nMOS devices to be

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individually bulk-driven. This matter has to be identified before starting the circuit design.

### ***2.3 Drawbacks Introduced with the Bulk-Driven Approach***

In Section 2.1 the benefit of the bulk-driven approach has been described that the transistor can be utilised in depleted-mode similar like JFET. However, many associated drawbacks have been reported in [BLA98]. This section thoroughly discusses these drawbacks, as they are essential to be understood in prior to assessing the bulk-driven circuit design.

#### **2.3.1 Transconductance Reduction**

One significant disadvantage of the bulk-driven approach is that the transconductance of a bulk-driven MOSFET  $g_{mb}$  is substantially less than a gate-driven MOSFET  $g_m$ . As can be realised from Figure 2-1, the slope of the bulk-driven MOSFET ( $= g_{mb}$ ) is much gentle than the slope of the gate-driven MOSFET ( $= g_m$ ).

The  $g_{mb}/g_m$  ratio,  $\eta$ , can be expressed by

$$\eta = g_{mb} / g_m = \frac{\gamma}{2\sqrt{2|\Phi_F| - V_{BS}}} \quad (2-2)$$

where  $2|\Phi_F|$  is the Fermi potential,  $\gamma$  is the body-effect coefficient, and  $V_{BS}$  is the bulk-to-source voltage of the MOSFET. This ratio  $\eta$  is thus dependent to  $V_{BS}$ , but it is typically around 0.1 to 0.3 [SED11].

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### 2.3.2 Transconductance Variation

It can be also noted from Equation (2-2) that  $g_{mb}$  ( $= \eta g_m$ ) is dependent to  $V_{BS}$ , which causes a substantial transconductance variation when a bulk-driven MOSFET is applied in a differential pair design.

### 2.3.3 Process Related

As discussed in Section 2.2, the polarity of the bulk-driven MOS transistor is process related because *wells* are required to isolate bulk-terminals. In case of n-well CMOS technology, only pMOS devices can be bulk-driven. For applications where both pMOS and nMOS devices are required, a twin-well technology is needed.

### 2.3.4 Degraded Latch up Immunity

As can be observed from Figure 2-2 and 2-3, CMOS technologies consist of parasitic bipolars. If for instance any of those bipolars, in particular vertical bipolars QV, are turned on, then there would be a short-circuit path between positive and negative supply rails. In digital systems this is known as a latch up effect, which may cause destructive breakdown of the chip.

To minimise this unwanted effect to happen, the forward-bias voltage of the bulk of the MOSFET must be kept as small as possible in order not to strongly turn on the parasitic bipolars [BLA98].

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### 2.3.5 Degraded Input Impedance Characteristics

With the bulk-driven approach, the input impedance characteristics become worse due to the parasitic bipolars. The resistive and input capacitive characteristics of the bulk-driven input are thoroughly discussed below:

#### *Input Resistance*

As illustrated in Figure 2-2, the bulk of the MOSFET is the base terminal of the parasitic bipolar. Therefore some appreciable input current  $i_B$  may flow.  $i_B$  can be expressed by

$$i_B = I_S [\exp(\frac{qV_{BS}}{kT}) - 1] \quad (2-3)$$

where  $I_S$  is the pn-junction current, which is also known as the scale current when the voltage across the pn-junction  $v_{BS}$  is zero,  $k$  is the Boltzmann constant ( $=1.38 \times 10^{-23} \text{JK}^{-1}$ ),  $T$  is the temperature in Kelvin, and  $q$  is the charge of an electron ( $=1.602 \times 10^{-19} \text{C}$ ).  $I_S$  can be expressed by

$$I_S = A_S q n_i^2 \left( \frac{D_p}{L_p N_D} + \frac{D_n}{L_n N_A} \right) \quad (2-4)$$

where  $A_S$  is the active area of the source of the MOSFET,  $N_A$  and  $N_D$  are the doping concentrations of the acceptors and donors respectively,  $L_n$  and  $L_p$  are the diffusion length of holes and electrons respectively,  $D_p$  and  $D_n$  are the diffusion constant of holes and electron respectively, and  $n_i$  is the number of free electrons and holes in a unit volume of intrinsic temperature at a given temperature ( $\approx 1.5 \times 10^{10}$  carriers/cm<sup>3</sup> at room temperature).

#### *Input Capacitance*

The capacitance of the bulk-driven device can also be understood from the study of bipolar devices. As illustrated in Figure 2-2, the bulk-driven input consists of two

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types of bipolars, QP and QV, which are classified as a lateral bipolar and a vertical bipolar, respectively.

From the bipolar characteristics modelling for QP, the source-to-bulk depletion capacitance  $C_{sb-depletion}$  can be expressed by

$$C_{sb-depletion} = \frac{CJ_{nwell-p+}}{\left(1 - \frac{V_{SB}}{V_0}\right)^{MJ_{nwell-p+}}} AS + \frac{CJSW_{nwell-p+}}{\left(1 - \frac{V_{SB}}{V_0}\right)^{MJSW_{nwell-p+}}} PS \quad (2-5)$$

where  $CJ_{nwell-p+}$  is the zero-bias (i.e.  $V_{SB}=0$ ) body-junction capacitance per unit area over the drain/source region,  $CJSW_{nwell-p+}$  is the zero-bias body-junction capacitance per unit length along the sidewall of the drain/source region,  $MJ_{nwell-p+}$  and  $MJSW_{nwell-p+}$  are the grading coefficient for area and sidewall components respectively,  $V_0$  is the body-junction built-in potential, and  $AS$  and  $PS$  are the area and the perimeters of the source region of the MOSFET respectively. As can be realised from this equation, forward-bias (i.e.  $V_{SB}>0$ ) operation of a bulk-driven MOSFET causes an increase in  $C_{sb-depletion}$ .

Furthermore, from the study of bipolar characteristics, the diffusion capacitance  $C_{sb-diffusion}$  is introduced when the bulk is in forward-biased.  $C_{sb-diffusion}$  can be expressed by

$$C_{sb-diffusion} = \frac{\tau_T}{V_t} i_B \quad (2-6)$$

where  $\tau_T$  is the mean transit time of the junction and  $V_t$  is the thermal voltage ( $\approx 26\text{mV}$  at room temperature).

On the other hand, the pn-junction formed between n-well and p-substrate is never forward-biased since the most negative voltage is connected at the p-substrate. Hence

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only depletion capacitance is introduced across this pn-junction. This junction capacitance, namely well-to-substrate capacitance  $C_{ssub}$ , can be expressed by

$$C_{ssub} = \frac{CJ_{nwell-psub}}{\left(1 - \frac{V_{SB}}{V_0}\right)^{MJ_{nwell-psub}}} A_{nwell} + \frac{CJSW_{nwell-psub}}{\left(1 - \frac{V_{SB}}{V_0}\right)^{MJSW_{nwell-psub}}} P_{nwell} \quad (2-7)$$

where  $CJ_{nwell-psub}$  is the zero-bias (i.e.  $V_{nwell-psub}=0$ ) body-junction capacitance per unit area over the n-well and p-substrate region,  $CJSW_{nwell-psub}$  is the zero-bias body-junction capacitance per unit length along the sidewall of the n-well and p-substrate region,  $MJ_{nwell-psub}$  and  $MJSW_{nwell-psub}$  are the grading coefficient for area and sidewall components respectively,  $V_0$  is the body-junction built-in potential, and  $A_{nwell}$  and  $P_{nwell}$  are the area and the perimeters of the n-well respectively.

In summary, the total capacitance of the bulk  $C_b$  is given by

$$C_b = C_{bs-depletion} + C_{bs-diffusion} + C_{ssub} \quad (2-8)$$

The  $C_b$  is significantly greater than the gate-to-source capacitance  $C_{gs}$ , given by

$$C_{gs} \approx \frac{2}{3} WLC_{OX} + WC_{GSO} \quad (2-9)$$

where  $W$  and  $L$  are the width and the length of the MOSFET respectively,  $C_{OX}$  is the oxide capacitance, and  $C_{GSO}$  is the gate-to-source overlap capacitance per unit channel width.

### 2.3.6 Reduced Bandwidth

Utilising bulk-driven devices also causes in speed reduction. For a gate-driven MOSFET in saturated region, its transitional frequency,  $f_{T, gate-driven}$ , is given by

$$f_{T, gate-driven} \approx \frac{g_m}{2\pi C_{gs}} \quad (2-10)$$

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At the frequency beyond  $f_{T, gate-driven}$ , the device no longer provides signal gain. In a case of a bulk-driven MOSFET in saturated region, its transitional frequency  $f_{T, bulk-driven}$  can be approximated by

$$f_{T, bulk-driven} \approx \frac{g_{mb}}{2\pi(C_{bs} + C_{ssub})} = \frac{\eta g_m}{2\pi(C_{bs} + C_{ssub})} \quad (2-11)$$

By dividing Equation 2-11 by Equation 2-10, the following relationship can be obtained:

$$f_{T, bulk-driven} = \frac{\eta C_{gs}}{C_{bs} + C_{ssub}} f_{T, gate-driven} \quad (2-12)$$

As discussed in Section 2.3.1 and 2.3.3,  $\eta$  is typically around 0.1 to 0.3 and  $(C_{bs} + C_{ssub}) > C_{gs}$ . Thus in summary, the speed performance becomes significantly slow with the bulk-driven approach.

### 2.3.7 Noise

The noise performance also becomes severe with the bulk-driven approach. The channel noise current of a MOSFET  $\overline{di_{DS}^2}$  is given by

$$\overline{di_{DS}^2} = 4kT \left(\frac{2}{3} g_m\right) df \quad (2-13)$$

where  $k$  is the Boltzmann's constant ( $1.381 \times 10^{-23}$  J/K),  $T$  is the temperature in Kelvin, and  $2/3$  is the coefficient factor for long-channel MOSFET. The equivalent input noise voltage of a gate-driven MOSFET  $\overline{dv_{ieq\_gate-driven}^2}$  can be worked out by dividing Equation (2-13) with  $g_m^2$ , which turns out to

$$\overline{dv_{ieq\_gate-driven}^2} = 4kT \left(\frac{2}{3}\right) \frac{1}{g_m} df \quad (2-14)$$

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and the equivalent input noise voltage of a bulk-driven MOSFET  $\overline{dv_{ieq\_bulk-driven}^2}$  can be worked out by dividing Equation (2-13) with  $g_{mb}^2$ ,

$$\overline{dv_{ieq\_bulk-driven}^2} = 4kT \left(\frac{2}{3}\right) \frac{g_m}{g_{mb}^2} df = 4kT \left(\frac{2}{3}\right) \frac{1}{g_m} \frac{1}{\eta^2} df = \frac{1}{\eta^2} \overline{dv_{ieq\_gate-driven}^2} \quad (2-15)$$

Thus in summary,  $\overline{dv_{ieq\_bulk-driven}^2}$  is  $1/\eta^2$  times larger than  $\overline{dv_{ieq\_gate-driven}^2}$ .

### 2.3.8 New Layout Design Techniques

From the layout design viewpoint, bulk-driving a MOSFET brings a new challenge especially when a matched pair of the devices is needed (e.g. for differential pair applications) because the n-well needs to be separated per every device. Consequently, the conventional common-centroid layout technique is not possible for matching. To the author's best knowledge, the layout techniques of a bulk-driven pair have not been reported in publications yet. Hence, the layout designers must develop their own layout techniques with no (or very little) references to achieve precise matching as possible.

## 2.4 Chapter Conclusion

In this chapter an overview of the bulk-driven approach has been presented. A bulk-driven MOSFET acts like a JFET-like transistor and therefore allows the ICMR to achieve rail-to-rail operation and thus the dynamic range can be expanded under the low supply voltage constraint. However, due to the device physics of CMOS technology, this approach also introduces many drawbacks. Each drawback is thoroughly examined in this chapter.

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In order to utilise the bulk-driven approach in CMOS analogue circuit design, novel design techniques need to be developed to overcome those drawbacks.

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## Chapter 3      Bulk-Driven Differential Pairs

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Differential pairs are perhaps mostly widely used two-transistor subcircuits in analogue circuit design [GRA01]. In CMOS analogue circuit design, a differential pair consists of two MOSFETs that are coupled at their sources. Hence a differential pair is also referred as a source-coupled pair [BAK08]. In many literatures, the concept of differential pairs is taught after studying single-ended amplifiers in order to emphasise the high immunity of the signal to noise and interferences [RAZ01], [SAN06], [SED11], [BAK08], [GRA01], [ALL02], [JOH97].

This chapter reports on the author's achievements relating to the development of new circuit design techniques of a bulk-driven differential pair, in order to overcome the drawbacks described in Chapter 2 as much as possible. Two types of a bulk-driven differential pair are proposed in this chapter, which the author has named them as Bulk-Driven Double Replica-Biased (BDDRB) input stage [HAG06] and Bulk-Driven Flipped Voltage Differential Pair (BDFVDP) [HAG10].

*A Comment Concerning the Naming Convention – “bulk-driven” or “body-driven”?*

It is worth reviewing the publications concerning the invention of a bulk-driven differential pair. According to [YAN00], A. Guzinski *et al* invented a “body-driven” differential pair in 1987 for the Operational Transconductance Amplifier (OTA) design [GUZ87]. In 1991, the invented pair was used in an OTA-C filter of a CMOS telephone circuit in [DIE91]. The original purpose of the invented pair was to yield the small transconductance and to improve linearity. (Interestingly, there are few

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circuit blocks where the small transconductance characteristic is appreciated.) Later on, B. Blalock *et al* studied the depletion characteristics of the “bulk-driven” MOSFET and proposed a “bulk-driven” differential pair in an operational amplifier design to achieve rail-to-rail input common-mode range (ICMR) under the supply voltage as low as 1-volt [BLA98].

From this historical background, two different names appeared to describe the same circuit block – “body-driven” and “bulk-driven” differential pair, named by Guzinski *et al* and Blalock *et al*, respectively [BIA99]. In this thesis, the author shall use the same name used by Blalock *et al* throughout, i.e. “bulk-driven”, since the research objective was to develop new circuit design techniques that utilise the depletion characteristics of the MOSFET and overcome the drawbacks identified by Blalock *et al* in [BLA98]. In another words, this research work is the further improvement of [BLA98].

#### *A Comment Concerning MOSFET symbol*

From this Chapter and on, many transistor-level circuit diagrams are presented. Therefore it is worth taking a moment to comment concerning MOSFET symbols beforehand. In many literatures [RAZ01], [SAN06], [SED11], [BAK08], [GRA01], [ALL02], [JOH97], a MOSFET symbol is simplified to a three-terminal device, since in most circuits the bulk of pMOS and nMOS devices are tied to the positive supply rail (VDD) and the negative supply rail (VSS, or GND if it is the least voltage potential), respectively. The simplified symbols for pMOS and nMOS transistors are depicted in Figure 3-1(a) and (b), respectively. For MOSFET where the bulk connection needs to be explicitly identified, the symbols shown in Figure 3-1(c) and (d) are often used for the pMOS and nMOS transistors, respectively.

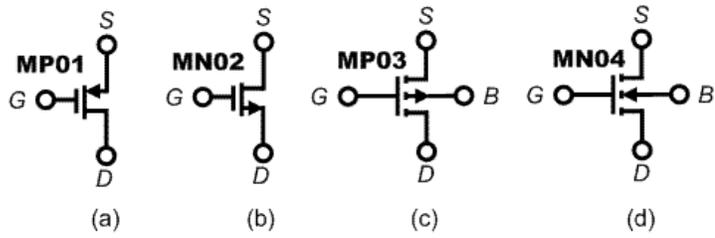


Figure 3-1 MOSFET symbols for (a) pMOS (its bulk tied to VDD and not shown), (b) nMOS (its bulk tied to VSS and not shown), (c) pMOS (its bulk shown explicitly), and (d) nMOS (its bulk shown explicitly)

In this thesis, the symbols shown in Figure 3-1(a) and (b) are used to represent pMOS and nMOS transistors, respectively, and for bulk-driven devices Figure 3-1(c) and (d) are used to represent pMOS and nMOS transistors, respectively. In addition, all transistors are identified as MP and MN in the circuit diagrams to represent the pMOS and nMOS transistors, respectively, so that the readers can easily realise the polarity of the transistors.

### 3.1 Bulk-Driven Double Replica-Biased Input Stage

#### 3.1.1 Introduction

The primary concern of utilising a bulk-driven device in a differential pair is that its transconductance  $g_{mb}$  is dependent to the bulk-to-source voltage  $V_{BS}$ .  $g_{mb}$  can be expressed by

$$g_{mb} = \frac{g_m \gamma}{2\sqrt{2|\Phi_F| - V_{BS}}} \quad (3-1)$$

where  $g_m$  is the transconductance of the gate-driven MOSFET,  $\gamma$  is the body-effect coefficient, and  $2|\Phi_F|$  is the Fermi potential. In differential pair applications, it is essential that its effective transconductance  $g_m(eff)$  is nearly constant over the rail-to-



sub 1-volt ( $V_{T0}+3V_{DSsat}$ ) to the maximum allowed by the CMOS process, and also eliminates the latch-up problem.

### 3.1.2 Proposal

The idea of our bulk-driven input stage comes from utilizing two pairs of the RBS to cover all portions of the rail-to-rail ICMR. Figure 3-3 illustrates the topology of our approach, which we call the Bulk-Driven Double Replica-Biased (BDDR) input stage [HAG06].

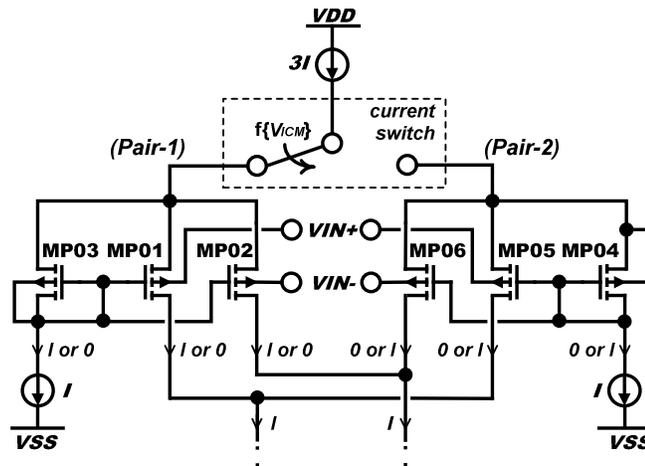


Figure 3-3 Topology of the BDDR input stage

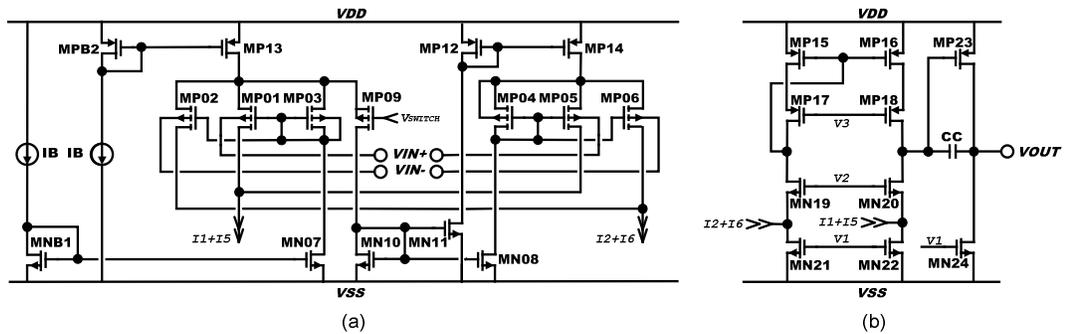
The BDDR input stage consists of pair-1 (MP01~MP03) and pair-2 (MP04~MP06), which are assigned for the low and high portions of the ICMR, respectively, and a current switch.

The device sizes of pair-1 are all the same, and the same dc current runs through each device when the pair is selected. This leads MP03 to be the replica of the input pair, and  $V_{BS1,2}$  to be equal to  $V_{GS3}$  (= constant). The same argument goes to pair-2 except that  $V_{BS5,6}$  would be zero instead. The pair-1 would be operational for the ICMR between  $VDD-V_{SDsat}-V_{SG3}$  and  $VSS+V_{DSsat}$ , and for pair-2 the operational range would

be between  $VDD - V_{SDsat}$  and  $VSS + V_{DSsat} + V_{SG4}$ . To maximize the ICMR a current switch is implemented so that the effective ICMR would be between  $VDD - V_{SDsat}$  and  $VSS + V_{DSsat}$ .

### Operation Principle

Figure 3-4(a) illustrates how the BDDR input stage can be realized as a transistor circuit. Again, MP01~MP03 (pair-1) and MP04~MP06 (pair-2) are the replica-biased input pairs for the low and high portions of the ICMR, respectively. MP09~MN12 form a current switch and work as a function of  $V_{ICM}$ . This input stage is configured such that it normally operates with pair-1. When  $V_{ICM}$  becomes high and causes  $V_{SG9}$  to be greater than the threshold voltage ( $|V_{T0}|$ ), the switch deactivates pair-1 and activates pair-2 instead. Conversely, when  $V_{ICM}$  becomes low and causes  $V_{SG9} < |V_{T0}|$ , pair-1 turn on and pair-2 turns off. The bias-voltage,  $V_{SWITCH}$ , controls the crossover voltage between the two points.



**Figure 3-4** An application example of the BDDR input stage in a folded-cascode two-stage op-amps (a) the BDDR input stage, and (b) a folded-cascode two-stage op-amps

To verify the operation of the BDDR input stage, it was necessary to implement it in an op-amp. For this we chose a folded-cascode two-stage op-amp, as illustrated in Figure 3-4(b), to present as an application example.

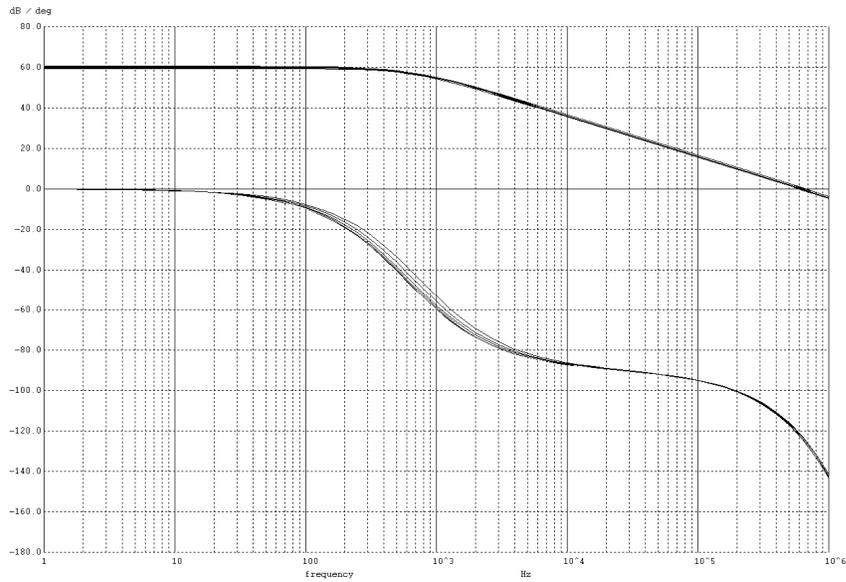
### 3.1.3 Simulation Results

Using the BSIM3 MOSFET models of a 0.18 $\mu$ m CMOS process, the op-amp of Figure 3-4 has been simulated in the typical mode with a supply voltage of 0.8-volt and a load resistance and capacitance of 1M $\Omega$  and 5pF, respectively. Table 3-1 shows the summary of the simulation results.

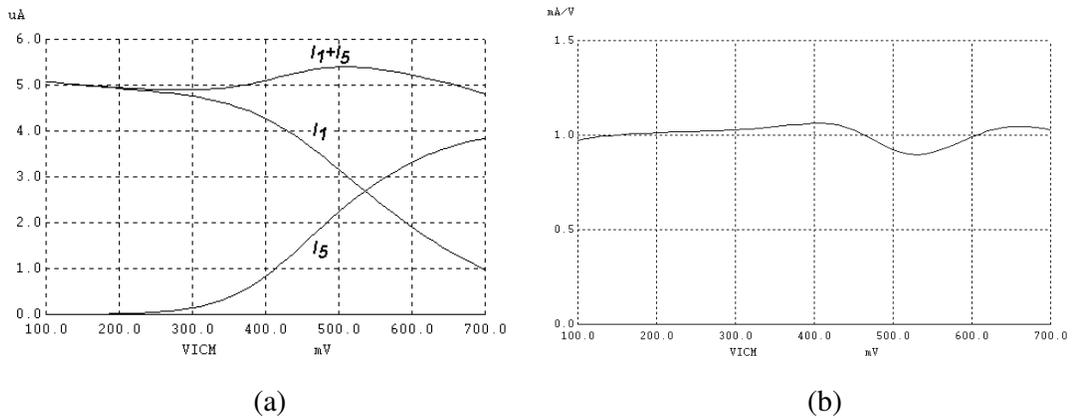
**Table 3-1 Simulation Results of the Overall Performance of the Proposed Op-amp in Figure 3-3**

| Characteristics  | Simulated Results   |
|--|---|
| Open-loop DC gain  | 60dB  |
| Unity-gain frequency   | 0.6MHz  |
| Phase margin   | 58°   |
| ICMR   | 0.6V  |
| Total current consumption  | 61~74 $\mu$ A ( $V_{ICM}$ dependent)  |
| SR   | SR+ = 1.0V/ $\mu$ s, SR- = -0.5V/ $\mu$ s   |
| Output voltage swing   | 0.6V  |
| Common-mode rejection ratio  | 63dB  |
| Power Supply Rejection Ratio (PSRR)  | PSRR+ = 58dB, PSRR- = 79dB  |
| Input referred noise voltage   | 160nV/ $\sqrt$ Hz (white noise only)  |
| Total harmonic distortion,<br>$A_{VCL}=+1V/V$  | 0.014% (-77.1dB)<br>for 0.6Vp-p, 1kHz sine wave<br>0.093% (-60.6dB)<br>for 0.6Vp-p, 10kHz sine wave |
| Setup: $V_{DD} = 0.8V$ , $V_{SS} = 0V$ , $V_{switch} = V_{DD} - 0.5V$ , $C_L = 5pF$ , $R_L=1M\Omega$ |   |

The simulation confirmed the rail-to-rail ICMR operation ( $V_{DD}-V_{SDsat14}$  to  $V_{SS}+V_{Dssat07}$  precisely). Figure 3-5 and Figure 3-6(a) show the simulation results of the open-loop gain frequency response and the effective tail current of the op-amp in Figure 3-4, which indicate that both characteristics are nearly  $V_{ICM}$  independent. Figure 3-6(b) gives the simulation results of  $g_m(eff)$  of the op-amp versus  $V_{ICM}$ .



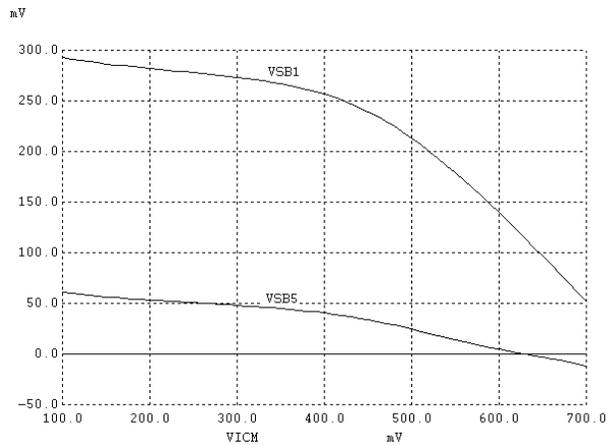
**Figure 3-5 Simulated frequency response of the op-amps for  $V_{ICM}$  varying from 0.1 to 0.7V with a 0.1V step**



**Figure 3-6 Simulated plots for (a) tail current versus  $V_{ICM}$  and (b)  $g_m(eff)$  versus  $V_{ICM}$**

Figure 3-6(b) indicates that the  $g_m$  variation is approximately 10% over the rail-to-rail ICMR operation. This variation peaks at the transition point between the two pairs, i.e. when the pairs are partially on and off. It is worth noting that the source-to-bulk voltage of the input pairs ( $V_{SB1}$  and  $V_{SB5}$ ) changes at the transition stage, which should also have created a major impact in the  $g_m$  variation according to [HOG92].

Figure 3-7 shows the simulation results of  $V_{SB1}$  and  $V_{SB5}$  versus  $V_{ICM}$ .



**Figure 3-7 Simulated  $V_{SB1}$  and  $V_{SB5}$  versus  $V_{ICM}$**

### *Advantages and Disadvantages*

An important practical advantage of the BDDRP input stage is that it requires no special CMOS process. Other advantages are  $g_m(\text{eff})$  and SR of the op-amp remain relatively constant with respect to  $V_{ICM}$ , and the circuit is immune from latch-up. Conventional BDDP techniques require very low supply voltage [BLA98], otherwise the rail-to-rail ICMR operation would cause the bulk terminals to be strongly forward-biased. With the BDDRB input stage, the bulk-to-source voltages remain as the same condition as the replica device regardless of the supply voltage condition. For confirmation, we simulated the circuit of Figure 3-4 with a 3-volt power supply and observed that the rail-to-rail ICMR operations did not result an increase in the supply current consumption.

However, the rest of the disadvantages of a bulk-driven MOSFET remain unchanged. The  $g_{mbs}$  is low (resulting relatively low gain-bandwidth products and poor noise performance), and also the conventional layout matching techniques cannot be applied because of the circuit structure.

The input impedance is also known to be another disadvantage of a bulk-driven MOSFET. However, this is controllable by circuit designers as it is directly related to its source-to-bulk voltage. Reducing the forward-bias of the bulk-terminal results in increased input resistance and decreased source-to-bulk and source-to-drain capacitances ( $C_{sb}$  and  $C_{sd}$ ). With the BDDR input stage, this can be easily achieved by decreasing the source-to-bulk voltage of the replica device ( $V_{SB3}$  of Figure 3-4(a), which is equivalent to  $V_{SG3}$ ). Figure 3-8 illustrates the simulation results of the input impedance measurements for the op-amp in Figure 3-4.

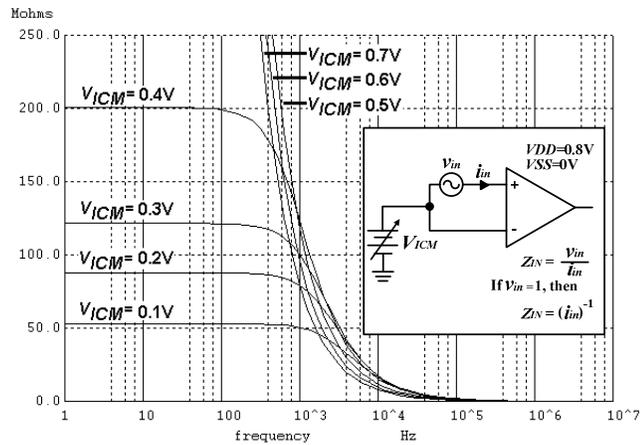


Figure 3-8 Simulation results of the circuit-level input impedance characteristic

### 3.1.4 Section Conclusion

In this section a new approach for the bulk-driven input stage called BDDRP to achieve rail-to-rail ICMR operation has been presented. This approach leads the operational supply voltage to be from under 1-volt to the maximum allowed by the CMOS process used, as well as completely removing the latch-up problem. SPICE simulations indicate that  $g_m(eff)$  is nearly constant (within 10%) over the entire ICMR whilst the effective tail current remains almost unchanged. The additional hardware implemented to achieve this performance is only a replica circuit for each pairs and a current switch.

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## ***3.2 Bulk-Driven Flipped Voltage Differential Pair***

### **3.2.1 Introduction**

The BDDRP proposed in the previous section consists of a novel circuit design technique that can efficiently overcome the non-linearity and the latch up problems, however it still does not solve the issue of the degraded input impedance characteristics of a bulk-driven MOSFET, in particular the increased input capacitance caused by the diffusion capacitance and the well-to-substrate capacitance as described in Chapter 2.

This section reports the author's achieved work on development of a new circuit design technique that can particularly solve the issue of the degraded input impedance of a BDDP.

### **3.2.2 Design Approach**

#### *Low-Power Differential Pair*

In prior to developing a new BDDP, at first the author reviewed previous works of a differential pair that achieves low-power high-performance, and drew an attention to a novel circuit block called Flipped Voltage Follower Pseudo Differential Pair (FVFDP) which was proposed by Carvajal *et al* in [CAR05]. Figure 3-9(a) and (b) illustrates the transistor realization of the FVFDP, and the simulated plot with  $I_B$  set to 1 $\mu$ A using a 0.35 $\mu$ m CMOS process.

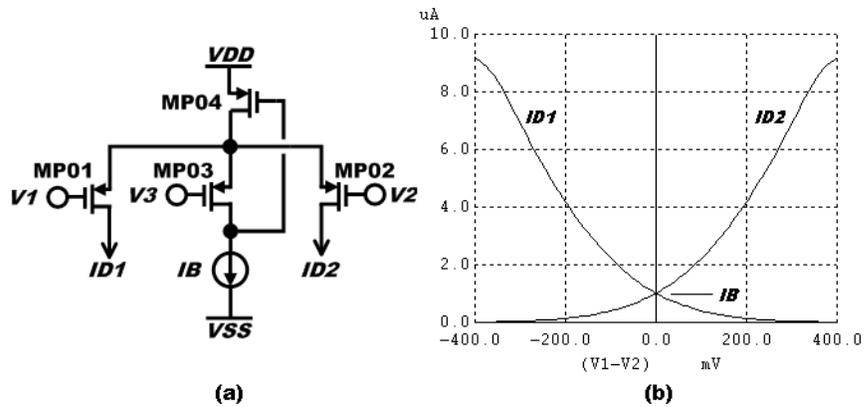


Figure 3-9 (a) (pMOS) FVFDP proposed in [CAR05], and (b) simulating the DC transfer characteristics using a 0.35 $\mu$ m CMOS process

In Figure 3-9(a),  $V_1$  and  $V_2$  are the differential input, and  $V_3$  is the common-mode voltage of  $V_1$  and  $V_2$ , i.e.  $(V_1+V_2)/2$ . As can be observed from Figure 3-9(b), when no differential signal is applied (i.e.  $V_1=V_2=V_3$ , steady condition) the drain current of MP01 and MP02 ( $I_{D1}$  and  $I_{D2}$ ) become equal to  $I_B$ , and when the differential signals are applied then  $I_{D1}$  and  $I_{D2}$  can become much larger than the twice of  $I_B$ . This low-static high-dynamic power performance is not possible to achieve with a conventional differential pair.

For the development of the new BDDP design, the author selected the FVFDP as the base. This section reports a new circuit design technique that bulk-drives the FVFDP so that rail-to-rail low-power high-driving performances can be all achieved, but without facing the issue of the degraded input impedance characteristics caused by the bulk-driven MOSFET.

#### *A Bulk-Driven MOSFET with the Reverse-Biased Diode*

In order to avoid the issue of the degraded input impedance characteristics of a bulk-driven MOSFET, the author came up with an idea of utilising a reverse-biased diode. Figure 3-10(a) and (b) illustrate the circuit diagram of a bulk-driven pMOS device

connected with the reverse-biased diode, and a sketch of a diode realized in CMOS technology, respectively.

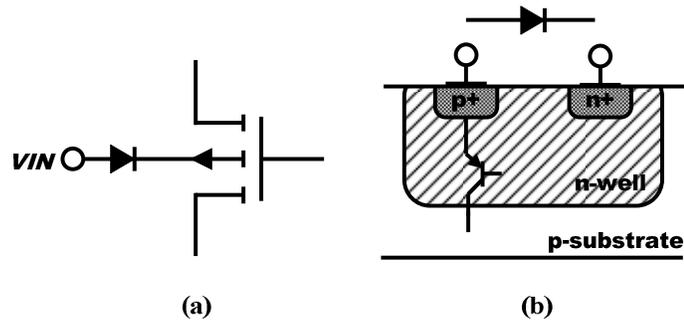
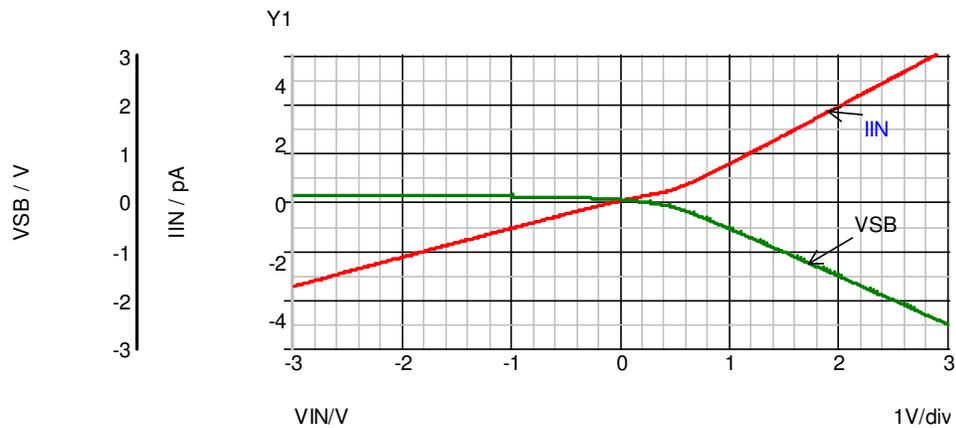


Figure 3-10 (a) a bulk-driven pMOS device with the reversed-biased diode, and (b) a diode realised in CMOS technology

Figure 3-11 shows the simulated plot of the DC sweep analysis of Figure 3-10(a) using a 0.35  $\mu\text{m}$  CMOS process, where the transistor width and length are 2 $\mu\text{m}$  and 1.4 $\mu\text{m}$ , and source, drain, and gate voltages of the pMOS device are fixed at 0V, -0.2V, and -0.8V, respectively. For the diode the minimum size is used. As can be observed from the plot, only a few pico-ampere of the DC input current  $I_{IN}$  flows at any operation point of the input voltage  $V_{IN}$ , since the body-diode of the pMOS and the added diode are in reversely connected to each other and thus only the leakage current passes through. Consequently, the source-to-bulk voltage  $V_{SB}$  of the PMOS does not become strongly forward-biased since the forward current of the diode is extremely small. It is worth noting that the added diode does not become strongly forward-biased either, so that the parasitic vertical bipolar illustrated in Figure 2(b) remains off.



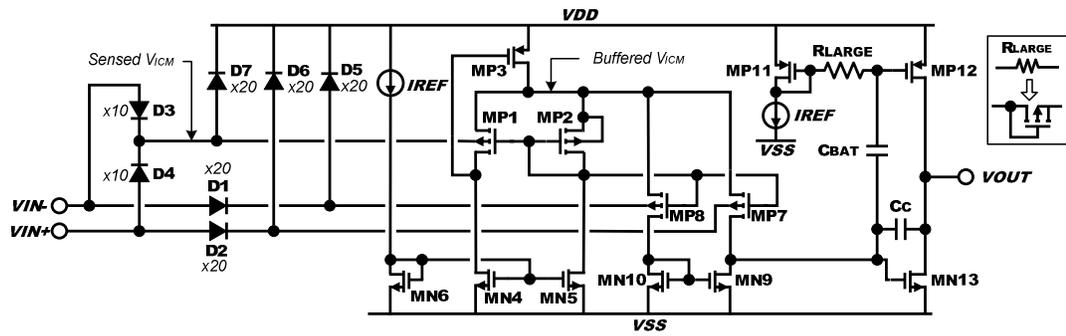
**Figure 3-11 Simulated  $I_{IN}$  and  $V_{SB}$  of Figure 2(a)**

Interestingly, with Figure 3-10(a) the input at  $V_{IN}$  is fed into p+ implant, whereas it would have been n+ implant for a conventional bulk-driven MOSFET. This means that  $V_{IN}$  indirectly sees the pn-junction (from n-well to p-substrate), and thus the effective input capacitance can be significantly reduced.

In results the input resistance and capacitance can both be drastically improved with this approach, the author further worked on with this approach to come up with a new proposal of BDDP design, which is described in the next subsection.

### 3.2.3 Proposal

Based on the analysis shown in the previous section, the author proposes a rail-to-rail low-power operational amplifier (op-amp) using a new design technique which we named as Bulk-Driven Flipped Voltage Differential Pair (BDFVDP). Figure 3-12 illustrates the circuit diagram of the proposal.



**Figure 3-12 Proposed CMOS buffer using Bulk-Driven Flipped Voltage Differential Pair**

The operation principle of the circuit in Figure 3-12 is simple to follow. From MP1 to MN5 form a circuit block called Bulk-Driven Flipped Voltage Follower (BDFVF) [HAG09]. MP1 and MP2 are equally sized and biased with identical drain current with MN4 and MN5. Since the bulk-terminal of MP2 is physically shorted to the coupled source node (i.e.  $V_{SB2}=0$ ), MP1 becomes the replica of MP2, and hence the source-to-bulk voltage of MP1 becomes virtually shorted (i.e.  $V_{SB1}\approx 0$ ). In another words, the coupled source voltage follows the bulk input voltage of MP1. If MP3 is sized wide enough such that it is in linear region, then the coupled source node becomes low impedance and hence it becomes the buffered signal of the bulk input of MP1. In the design of the proposed op-amp, BDFVF is utilized to buffer the common-mode signal of the differential input  $V_{ICM}$ .

From MP7 to MN10 forms the first stage of the operational amplifier. The input devices of this stage are bulk-driven, and when the differential signals  $V_{IN+}$  and  $V_{IN-}$  are identical then the drain current of the input devices,  $I_{D7}$  and  $I_{D8}$ , settle to the bias current  $I_{REF}$ . When large differential signals are applied, then  $i_{D7}$  and  $i_{D8}$  can become much greater than twice the current of  $I_{REF}$ , since the coupled source node has very low impedance and MP3 can supply a source current that is bigger than  $2 \times I_{REF}$ .

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From MP11 to MN13 forms the second stage of the operational amplifier, which has been converted to class-AB operation using the Quasi-Floating Gate (QFG) technique [LOP09]. As can be observed, the gate of MP12 is connected to the gate of MP11 with a large resistor  $R_{LARGE}$ , and also to the gate of MN9 with a capacitor  $C_{BAT}$ . In terms of DC characteristics, there exists no current flow through  $R_{LARGE}$  and therefore the gate voltage of MP12 and MP11 are the same, and thus the static drain current  $I_{D12}$  is  $I_{REF}$ . In terms of AC characteristics, a high pass filter is formed at the gate of MP12 with a cutoff frequency of  $1/(2\pi R_{LARGE} C_{BAT})$ , and therefore MP12 achieves not only static but also dynamic operation, which in turn leads to class-AB operation. It is remarkable to realize that a unity-size diode-connected MOSFET but in the cutoff region can form a substantially large resistance of  $R_{LARGE}$ , thus a low cutoff frequency can be achieved with a moderately small capacitance of  $C_{BAT}$ .

From D1 to D4 are the reverse-biased diodes to the bulk-driven devices. D3 and D4 are used to detect for  $V_{ICM}$ . In Figure 3, those diodes have been sized to 20 times of the minimum size of the diode for D1 and D2, and 10 times for D3 and D4, to prevent from further reduction of the transconductance as possible. The transconductance of a bulk-driven MOSFET with the reverse-biased diode  $g_{mb\_VR}$  can be expressed as:

$$g_{mb\_VR} = \alpha g_{mb} \quad (3-2)$$

where  $\alpha$  is the attenuation factor of the signal and  $g_{mb}$  is the transconductance of the bulk-driven MOSFET.  $\alpha$  can be expressed as:

$$\alpha = C_{diode} / (C_{diode} + C_{db}) \quad (3-3)$$

where  $C_{diode}$  is the junction capacitance of the reverse-biased diode, and  $C_{SB}$  is the source-to-bulk capacitance of the MOSFET.  $C_{diode}$  given by

$$C_{diode} = C_{j0\_diode} / (1 + V_R/V_0)^{0.5} \quad (3-4)$$

where  $C_{j0\_diode}$  is the zero-biased junction capacitance of the reverse-biased diode,  $V_R$  is the reversed-biased DC voltage, and  $V_0$  is the built-in bulk junction potential. Similarly,

$$C_{sb} = C_{j0\_mosfet} / (1 + V_{SB}/V_0)^{0.5} \quad (3-5)$$

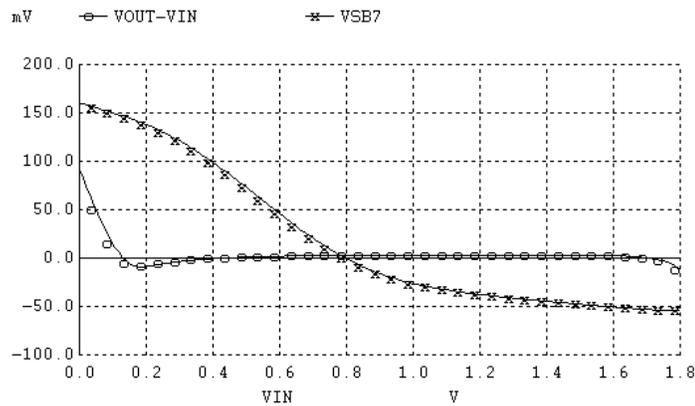
where  $C_{j0\_mosfet}$  is the zero-biased junction capacitance of the MOSFET, and  $V_{SB}$  is the source-to-bulk DC voltage.

### 3.2.4 Simulated Results

To verify the proposed solution of Figure 3-12, we designed it using a 0.35um CMOS process to operate with a 1.8V supply voltage. This section provides simulated results using the BSIM3 MOSFET models.

#### *DC-Sweep Analysis*

This subsection provides the simulation results of the DC-sweep analysis. Figure 3-12 has been setup in a unity-gain configuration with a 1.8V supply voltage, and the input voltage  $V_{IN}$  is swept from rail to rail. Figure 3-13 shows the simulated behaviour of the source-to-bulk voltage of the bulk-driven device MP7  $V_{SB7}$  and the potential difference between the output  $V_{OUT}$  and  $V_{IN}$ .

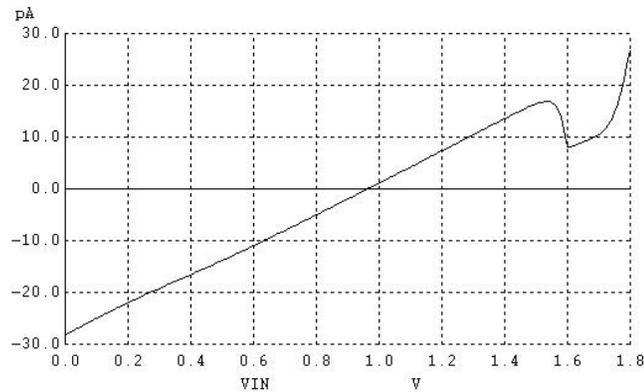


**Figure 3-13 Simulated  $V_{OUT}-V_{IN}$  and  $V_{SB7}$  of Figure 3-12 in unity-gain configuration**

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As can be noticed from Figure 3-13,  $V_{SB7}$  does not become strongly forward biased which indicates that latch up does not occur, and  $V_{OUT} - V_{IN}$  remains small which confirms that the proposed buffer is operational in rail-to-rail.

Figure 3-14 is the simulated plot of the input DC current  $I_{IN}$  of the same setup. It indicates that only  $\pm 30\text{pA}$  of DC current flows from rail to rail, suggesting that the input resistance would be as large as  $30\text{G}\Omega$ . This superior result is expected since the diodes are connected in reverse-bias to the body-diode of the MOSFET.



**Figure 3-14 Simulated  $I_{IN}$  of Figure 3-12 in unity-gain configuration**

### *Transient Analysis*

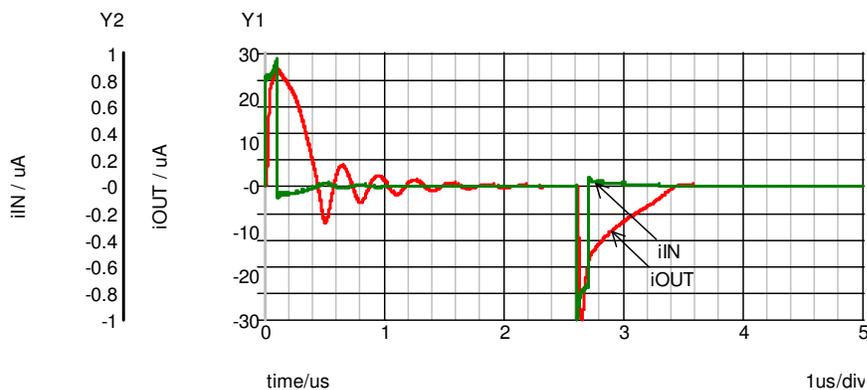
This subsection provides the simulation results of the transient analysis. Figure 3-12 has been setup in a unity-gain configuration with a 1.8V supply voltage and a capacitive load of 5pF, and a step input from 0.2V to 1.6V and vice versa is applied. Figure 3-15 is the simulated plot of the input voltage  $v_{IN}$ , the output slew rate  $v_{OUT}$ , and the transient behavior of the source-to-bulk voltage of the bulk-driven device MP7,  $v_{SB7}$ . The key observation of Figure 3-15 is the  $v_{SB7}$  behavior when a large step-down input is applied. Appreciating to the protection capability of the diodes from D5

to D7,  $v_{SB7}$  does not even instantaneously become forward biased by more than 0.3V and therefore the latch up problem has been prevented.



**Figure 3-15 Simulated  $v_{SB7}$  and slew rate of  $v_{out}$  of Figure 3-12 in unity-gain configuration with  $CL=5pF$  ( $v_{IN}$  stepping between 0.2V and 1.6V)**

Figure 3-16 is the simulated transient analysis plot of the input and output instantaneous current,  $i_{IN}$  and  $i_{OUT}$ , indicating that  $i_{IN}$  never achieves more than  $1\mu A$  and  $i_{OUT}$  current reaches over  $20\mu A$ . This suggests that the  $i_{IN}$  would always be in the nano-ampere range for an AC input slower than the Gain-Bandwidth (GBW), which proves the effectiveness of the Figure 3-12. This low  $i_{IN}$  has been achieved because the well-to-substrate capacitance is indirectly seen by the input and also the effective input capacitance has been lowered by the attenuation factor  $\alpha$ .



**Figure 3-16 Simulated  $i_{IN}$  and  $i_{OUT}$  of Figure 4 in unity-gain configuration with  $CL=5pF$  ( $v_{IN}$  stepping between 0.2V and 1.6V)**

*Observation*

To further observe our proposal of Figure 3-12, we designed another CMOS buffer as shown in Figure 3-17 for comparison purposes. This circuit block is the gate-driven type of Figure 3-12, and all transistors are sized identically. Table 3-2 shows the summary of the overall performance of the two circuit blocks.

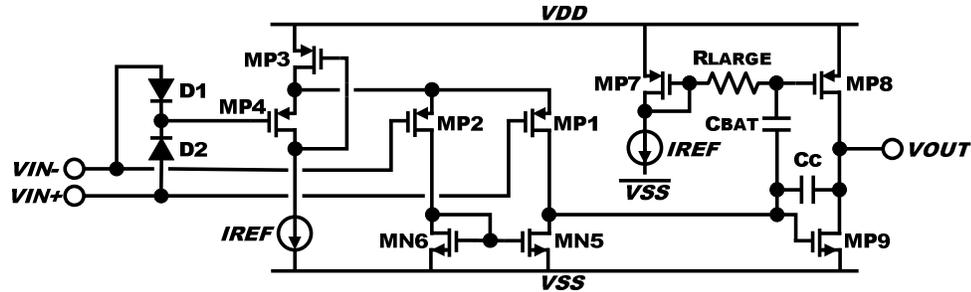


Figure 3-17 Gate-driven Flipped Voltage Differential Pair

Table 3-2 Simulated Results of the Overall Performance

| Parameter  | Simulated results                    |  |
|--|--------------------------------------|--|
|  | Figure 3-17                          | Figure 3-12                            |
| Open-loop gain $A_{OL}$  | 60dB                                 | 50dB                                   |
| Gain bandwidth (GBW) at $C_L=5pF$  | 9MHz                                 | 3MHz                                   |
| Total static current consumption $I_{CC}$  | $7\mu A$                             | $9\mu A$                               |
| Slew Rate (SR) at $C_L=5pF$  | SR+= $5.2V/\mu s$<br>SR-= $7V/\mu s$ | SR+= $5.2V/\mu s$<br>SR-= $2.3V/\mu s$ |
| Input referred noise   |                                      |  |
| $V_{IN}=VDD$ 1/f @ 1kHz  | MP1 & MP2<br>in cut off              | $11\mu V/\sqrt{Hz}$                    |
| Wideband   | $70\mu V/\sqrt{Hz}$                  | $600nV/\sqrt{Hz}$                      |
| $V_{IN}=0.9V$ 1/f @ 1kHz   | $9\mu V/\sqrt{Hz}$                   | $15\mu V/\sqrt{Hz}$                    |
| Wideband   | $600nV/\sqrt{Hz}$                    | $600nV/\sqrt{Hz}$                      |
| $V_{IN}=VSS$ 1/f @ 1kHz  | $1.5\mu V/\sqrt{Hz}$                 | $22\mu V/\sqrt{Hz}$                    |
| Wideband   | $100nV/\sqrt{Hz}$                    | $600nV/\sqrt{Hz}$                      |
| Total Harmonic Distortion<br>( $A_{CL}=1$ , $1.4V_{pp}$ sinewave)                            |                                      |  |
| CL=5pF @ 100kHz  | $1.4V_{pp}$                          | -40dB                                  |
| CL=10pF @ 100kHz   | Operation not<br>achievable          | -33dB                                  |
| CL=5pF @ 200kHz  |                                      | -33dB                                  |
| CL=5pF @ 300kHz  |                                      | -27dB                                  |
| Unless stated, the set up condition is:<br>$VDD=1.8V$ , $VSS=0V$ , $V_{IN}=0.9V$ , $C_L=5pF$ |                                      |  |

---

As expected, the open-loop gain  $A_{OL}$  and the GBW of the bulk-driven one is smaller and slower in comparison to the gate-driven one due to reduced transconductance of the input device, however  $A_{OL}=50\text{dB}$  GBW (at  $C_L=5\text{pF}$ ) = 3MHz is relatively efficient for the total static current consumption of only  $9\mu\text{A}$ . It is important to realize that the input referred noise of Figure 3-12 is moderately independent to the input condition since no transistors change the operation region. This property suggests that the single-pair approach is worthy of further improving than the double-pair approach which changes the operation region.

On the other hand, there is a significant drawback with the proposal that the  $A_{OL}$  is not constant to  $V_{ICM}$ , where the dominant root cause is that  $\alpha$  in Equation (3-2) varies significantly with the reverse voltage of the diode.

### 3.2.5 Section Conclusion

In this section a new low power consumption high-speed op-amp has been proposed. The new circuit block consists of a FVFDP and a QFG type of class-AB second stage, which delivers high-speed at 3MHz GBW operation for a 5pF load whilst maintaining the static current consumption as small as  $9\mu\text{A}$ . This paper also addresses the latch up problem by having reverse-bias connected diodes to the body diode of the bulk-driven MOSFET, so that only the diode's leakage current flows and forward biasing of the diodes can be prevented.

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### ***3.3 Chapter Conclusion***

In this chapter two types of new BDDP, called BDDRB and BDFVDP, have been proposed. The BDDRB input stage uses the RBS so that the effective transconductance becomes almost constant over the entire ICMR and hence solves the non-linearity and latch up issues. On the other hand, with the BDFVDP low-power high-speed operation can be achieved with the use of FVFDP and QFG techniques, and also solves the issue of degraded input impedance characteristics by utilising the reverse-bias connected diodes. For both BDDRB and BDFVDP, the hardware implementation is simple.

From this work, it is evident that circuit designers can contribute to solving many of the device physics limitations of a bulk-driven MOSFET described in Chapter 2. At least, the non-linearity and latch up issues can be solved by controlling the DC voltage across the bulk and the source of the MOSFET, and the degraded input capacitance concern can become less affected by indirectly applying the signal to the bulk (e.g. with a diode). With the use of novel circuit design techniques that were previously proposed by other authors, for instance FVFDP and QFG techniques, low-power high-speed performances can be achieved too.

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## Chapter 4 Bulk-Driven Source Followers

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Source followers are one of the fundamental circuit blocks that are introduced by many literatures of analogue IC design [RAZ01], [SAN06], [SED11], [BAK08], [GRA01], [ALL02], [JOH97]. In most cases they are discussed in the section of single stage amplifier design, and sometimes they are referred with different names, such as common drain amplifiers, voltage buffers, or voltage followers. These circuit blocks are particularly applied for DC level shifting purposes, for instance, at the input stage of operational amplifiers to achieve rail-to-rail operation [CAR03], [SHE09], [HAG08], and in current mirrors to reduce the voltage headroom consumption of the input device [RAM94]. Other types of applications include sensing the common-mode signal of fully differential amplifiers [BAN88], and cutting off the unwanted feed-forward path of the compensation circuits in multi-stage amplifiers [TSI76]. There is even a recent study which provides the high-frequency harmonic distortion analysis of source followers using a large-signal model, in order to derive an optimisation design technique for wide-bandwidth low-distortion operation [FAN05]. As its applications are very wide, there are many journals and conference papers published today relating to this field.

This chapter reports the achievement of the author's research work relating to source followers. In many conventional design techniques, cascaded complementary source followers (i.e. shift-up and -down level shifters being cascaded) are often utilised in order to eliminate the DC level shift [FAN05]. This chapter demonstrates that the bulk-driven approach leads to constructing the source followers with much simpler

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hardware, and allows the DC level shift not only to be eliminated but even programmable.

From the next section, new circuit blocks which the author has given the names as bulk-driven flipped voltage follower, bulk-driven super source follower, and bulk-driven DC level shifter are proposed and thoroughly discussed.

## ***4.1 Bulk-Driven Flipped Voltage Follower***

### **4.1.1 Introduction**

Source followers are often used as voltage buffers, which play an essential role in driving large capacitive loads at high speeds. The ideal performance of a voltage buffer is not only to drive the large load as fast as possible but also with minimal power consumption, which means that the buffer needs to have high slew rate and low static power consumption. Furthermore the input capacitance of the buffer would also need to be as small as possible so that the weak signal input is not affected under any circumstances. Today, it is evident that the Flipped Voltage Follower (FVF) proposed by Carvajal *et al* in [CAR05] is one of the closest to the ideal voltage buffer, as many recent proposals are utilizations and/or modifications of the FVF [PAD06], [PAD07], [MAN08], [RAM06].

Recently, the new version of the class-AB FVF that is free from the DC level-shift has been proposed by Ramirez-Angulo *et al* [RAM06]. This section proposes a much simpler technique which can eliminate the DC level shift and convert into class AB

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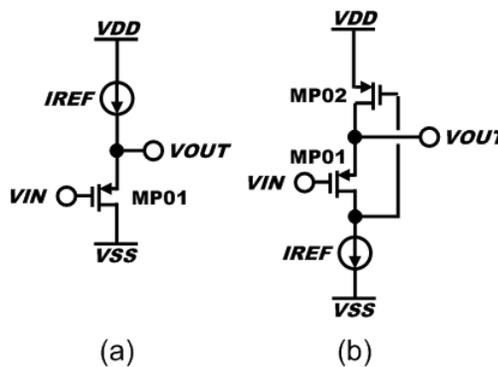
operation, whilst preserving the advantages of the FVF approach – low-power consumption with high-power drive.

#### 4.1.2 Previous Essential Works

This section covers a brief review of voltage followers and the bulk-driven MOSFETs used in a differential pair, which have been utilized to form the essential part of the proposal.

##### *Voltage Followers*

Figure 4-1 illustrates two types of voltage followers. Figure 4-1(a) is the conventional type of a voltage follower. The input device MP01 is biased with the drain current of  $I_{REF}$ , therefore the gate-to-source voltage  $V_{GS MP01}$  becomes constant if the body-effect is neglected, and therefore the output voltage  $V_{OUT}$  is equal to  $V_{IN} + V_{GS MP01}$ . Figure 4-1(b) illustrates the FVF, in which  $V_{OUT}$  is also shifted up by  $V_{GS MP01}$  from  $V_{IN}$ , however, in contrast to Figure 4-1(a), the beauty of the FVF is that it has current sourcing and sinking capabilities at the output, which can lead to delivering both high-power driving as well as low-power consumption simultaneously.

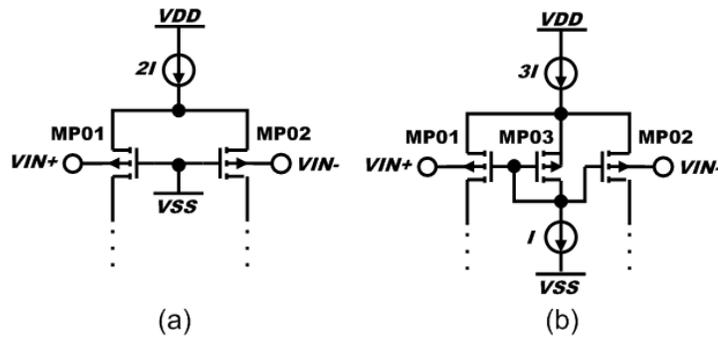


**Figure 4-1** Voltage followers (a) common-drain amplifier (voltage follower) and (b) FVF proposed in [CAR05]

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*Bulk-driven MOSFETs used in differential pairs*

In low-voltage rail-to-rail operational amplifier designs, there exists a design technique called the bulk-driven approach. The traditional design technique for rail-to-rail operational amplifiers is the deployment of complementary differential pairs with the tail current being controlled with current switches to keep the transconductance  $g_m$  constant [HOG92]. However, due to the fact that the mobility ratio of the complementary pairs ( $\mu_n/\mu_p$ ) is process and temperature dependent, causing the  $g_m$  variation to deviate by approximately 12% [CAR03], there exist circuit topologies which use only a single type of the differential pair, where one of them is the bulk-driven one. Figure 4-2(a) illustrates a bulk-driven differential pair that uses p-type devices only.



**Figure 4-2 Bulk-driven differential pair (a) pMOS input pair and (b) the replica-biased scheme proposed in [BLA00]**

The primary problem of Figure 4-2(a), however, is that the transconductance of a bulk-driven MOSFET  $g_{mb}$  is dependent on the bulk-to-source voltage  $V_{BS}$ . The level-1 model of the  $g_{mb}$  is given by:

$$g_{mb} = \gamma (2\beta I_{DS})^{0.5} / 2 (2|\Phi_F| - V_{BS})^{0.5} \quad (4-1)$$

where  $\gamma$  is the bulk-threshold parameter,  $\beta$  is the small-signal transconductance parameter,  $I_{DS}$  is the drain current, and  $2|\Phi_F|$  is the surface potential.

To overcome the concern of  $g_{mb}$  dependency over the  $V_{BS}$ , Blalock *et al* [BLA00] proposed the Replica-Biased Scheme (RBS) as illustrated in Figure 4-2(b). The pMOS device identified as MP03 is the replica device biasing the gates of the pair. Since the bulk of MP03 is shorted with its source, the  $V_{BS}$  of the pair is kept at zero.

The author has noted the advantage from Blalock’s approach namely that the condition of  $V_{BS} = 0$  is kept constant, meaning  $V_B = V_S$ , and chose to apply this to the FVF illustrated in Figure 4-1(b) to remove the DC level shift.

### 4.1.3 Proposal

Figure 4-3 illustrates the proposal of the modified FVF, which the author has named as “Bulk-Driven Flipped Voltage Follower (BDFVF)”. As mentioned previously this is the FVF for which the input device has been modified to a bulk-driven MOSFET biased by the replica circuit to eliminate DC level shift.

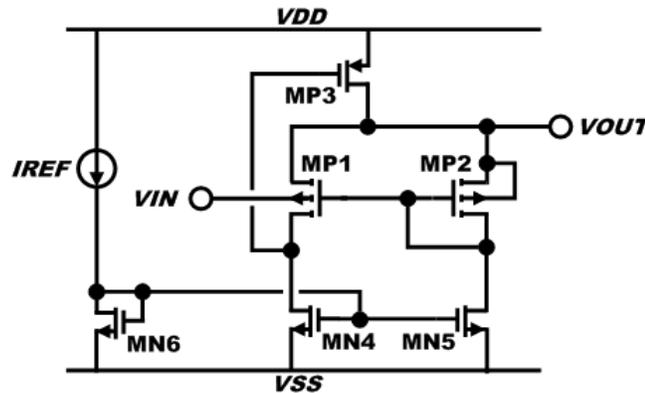
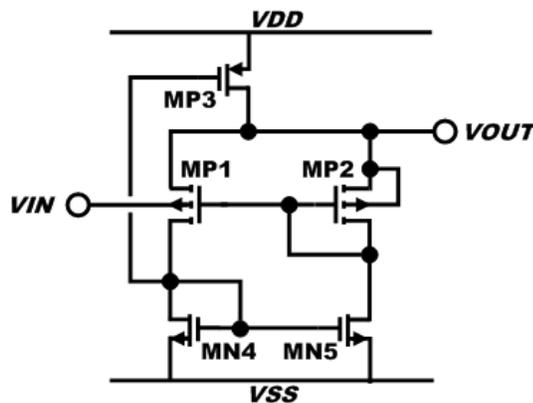


Figure 4-3 Bulk-driven flipped voltage follower (class-A)

The operation principle of the BDFVF of Figure 4-3 is very simple to follow. MP1, MP3, and MN4 form the FVF. MP1 is the input device, which its bulk is utilized to feed the input. MP2 and MN5 are the replica devices for MP1 and MN4 respectively.

Note that the bulk of MP2 is physically shorted to its source, which is the output node. Since the gate of MP1 is biased with the diode-connected MP2, as well as the drain current of MP1 and MP2 are equally set to  $I_{REF}$ ,  $V_B$  and  $V_S$  of MP1 becomes virtually shorted (i.e.  $V_{BSMP1} = 0$ ), and in effect the output voltage  $V_{OUT}$  becomes equal to  $V_{IN}$ .

The proposal of Figure 4-3 works well, however since it is class-A type, there is a limitation in its sink capability to  $2I_{REF}$ , which leads to poor pull capability in driving large loads at high speed. To overcome this problem, the circuit of Figure 4-3 can be modified to class-AB type as shown in Figure 4-4.



**Figure 4-4 Proposed class-AB bulk-driven flipped voltage follower**

The difference of Figure 4-4 from Figure 4-3 is that only MN4 has been modified to diode-connected instead of the constant bias to  $I_{REF}$ . In this way, MP1 and MP2 can also have the same drain current and hence the replica-biased scheme remains valid. This simple change has led to significant improvement in the sink capability of the output without the need of widening MN4 or MN5 or increasing  $I_{REF}$ . In the next section, simulation results are provided.

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#### 4.1.4 Simulated Results

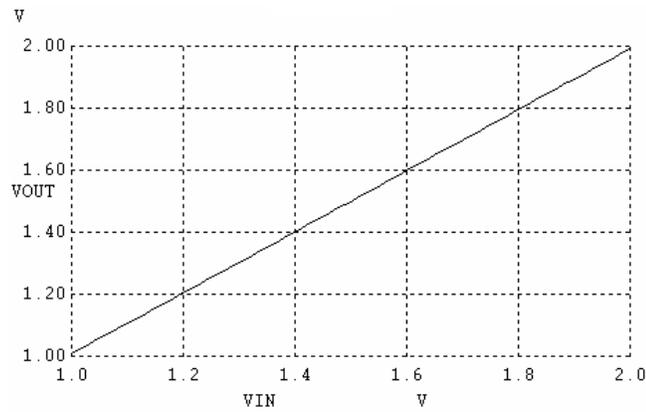
##### A. Overall Performance

Using the BSIM3 MOSFET models of a 0.35 $\mu$ m CMOS process, the BDFVF of Figure 4-4 is verified by simulation. Table 4-1 shows the simulation results summarising the overall performance.

**Table 4-1 Simulation Results of the Overall Performance of the Class AB DBFVF Circuit of Figure 4-4**

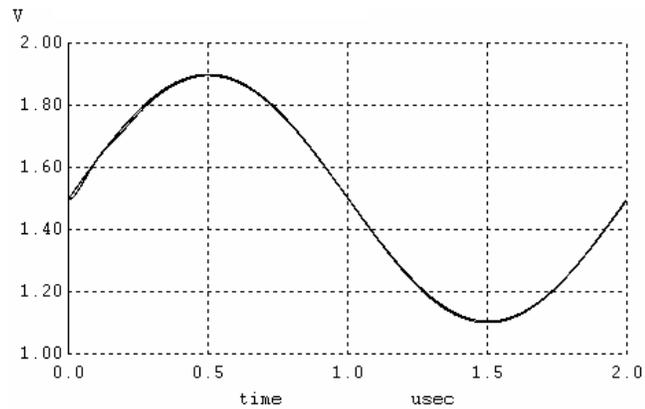
| Parameter   | Simulated results  |
|---|--|
| 3dB frequency   | 2.8MHz   |
| Total current consumption (when $I_L=0$ )   | 2.5 $\mu$ A  |
| Slew rate ( $V_{DD}=2V$ , $V_{SS}=0V$ , $CL=10pF$ , $V_{IN}=1V \leftrightarrow 2V$ )                            | 1.9V/ $\mu$ s  |
| PSRR+ / PSRR-   | 41.7dB / 42.0dB<br>(dc to 100kHz)  |
| 1/f noise at 1kHz   | 880nV/ $\sqrt{Hz}$   |
| THD ( $V_{pp}=0.8V$ $V_{DD}=1.5V$ , $V_{SS}=0V$ , $CL=10pF$ )   | 0.0747% when $f=1kHz$<br>0.0794% when $f=100kHz$<br>0.501% when $f=500kHz$ |
| Input voltage range ( $V_{DD}=2V$ , $V_{SS}=0V$ )   | 1V to 2V for offset $\leq 10mV$  |
| Load regulation   | $\pm 15\mu A$ for offset $\leq 10mV$                                       |
| Input current   | 1.5pA  |
| Input capacitance   | 9.3fF  |
| Unless stated, the set up condition is:<br>$V_{DD}=1.2V$ , $V_{SS}=0V$ , $V_{IN}=1V$ , $CL=10pF$ , $I_L=0\mu A$ |  |

Figure 4-5 illustrates the simulated plot of  $V_{OUT}$  versus  $V_{IN}$  with the setup of  $V_{DD} = 2V$  and  $V_{SS} = 0V$ . The simulation results indicate that the offset between  $V_{OUT}$  and  $V_{IN}$  was 10mV for the input range from 1V to 2V.



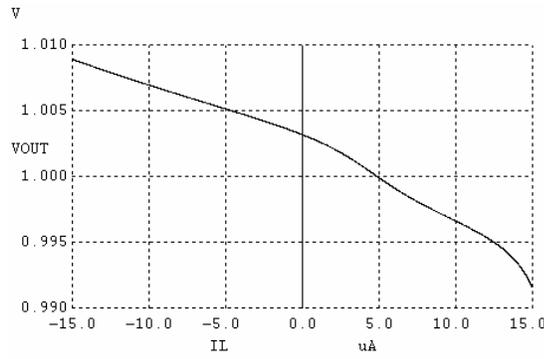
**Figure 4-5  $V_{OUT}$  vs  $V_{IN}$  ( $V_{DD}=2V$ ,  $V_{SS}=0V$ )**

Figure 4-6 illustrates the simulated plot of  $V_{OUT}$  with a sinusoidal  $V_{IN}$  input with 0.8V peak-to-peak magnitude and 500kHz frequency, and with the setup of  $V_{DD} = 2V$ ,  $V_{SS} = 0V$ , and  $CL = 10pF$ . The simulation results indicate that the Total Harmonic Distortion (THD) was 0.5%.



**Figure 4-6  $V_{OUT}$  and  $V_{IN}$  with 0.8Vpp 500kHz sinusoidal input ( $V_{DD}=2V$ ,  $V_{SS}=0V$ ,  $CL=10pF$ )**

Figure 4-7 illustrates the simulated plot of  $V_{OUT}$  regulation capability against the load current  $I_L$ . With the setup of  $V_{DD} = 1.5V$ ,  $V_{SS} = 0V$ , and  $V_{IN} = 1V$ , the simulation results indicate that  $V_{OUT}$  kept on regulated within 10mV until the load current reaches to  $\pm 15\mu A$ .



**Figure 4-7 Load regulation ( $V_{DD}=2V$ ,  $V_{SS}=0V$ ,  $V_{IN}=1V$ )**

### ***B. Input impedance***

Using bulk-driven MOSFETs in a differential pair of the operational amplifier is known to be a disadvantage in input current and capacitance [BLA98]. This subsection describes that the theoretical overview as well as the simulated results to state that this disadvantage is not the case with the BDFVF.

#### *Input current*

With a bulk-driven MOSFET as an input device, the input signal is fed into the pn-junction of the MOSFET. The current through the pn-junction  $I_{Dpn}$  is modelled by Equation 4-2:

$$I_{Dpn} = I_S \exp(V_D/V_t) \quad (4-2)$$

where  $I_S$  is the pn-junction current, which is also known as the scale current, when the voltage across the pn-junction  $V_D$  is zero.  $V_t$  is the thermal voltage, which is modelled as

$$V_t = kT/q \quad (4-3)$$

where  $k$  is the Boltzmann constant ( $=1.38 \times 10^{-23} \text{JK}^{-1}$ ),  $T$  is the temperature in Kelvin, and  $q$  is the charge of an electron ( $=1.602 \times 10^{-19} \text{C}$ ). At room temperature,  $V_t$  is approximately 26mV.

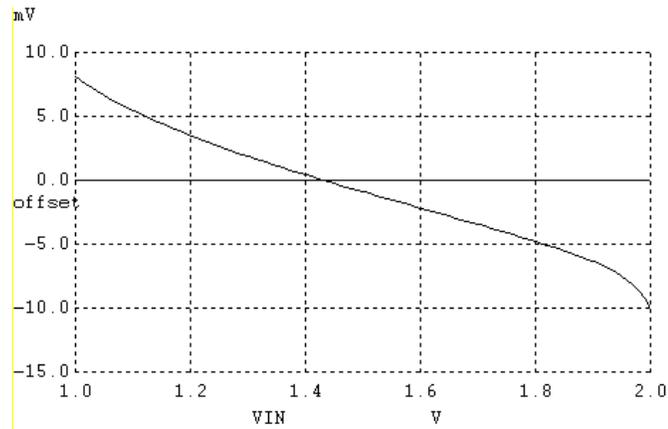
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$I_s$  can be described as in Equation (4-4):

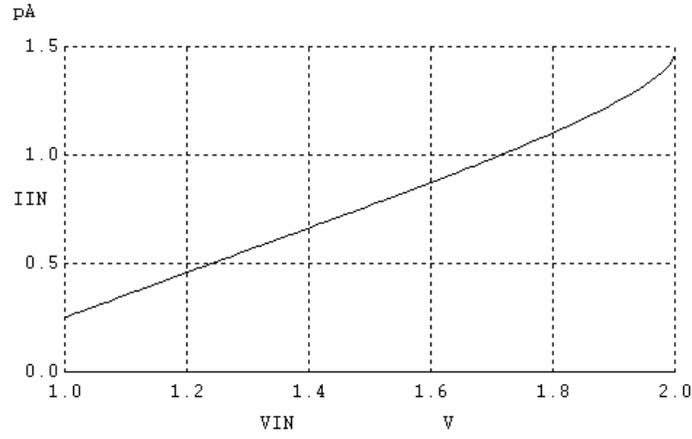
$$i_s = A_s q n_i^2 \left( \frac{D_p}{L_p N_D} + \frac{D_n}{L_n N_A} \right) \quad (4-4)$$

where  $A_s$  is the active area of the source of the MOSFET,  $N_A$  and  $N_D$  are the doping concentrations of the acceptors and donors respectively,  $L_n$  and  $L_p$  are the diffusion length of holes and electrons respectively,  $D_p$  and  $D_n$  are the diffusion constant of holes and electron respectively, and  $n_i$  is the number of free electrons and holes in a unit volume of intrinsic temperature at a given temperature ( $\approx 1.5 \times 10^{10}$  carriers/cm<sup>3</sup> at room temperature).

In the case of a bulk-driven differential pair, the input current is expected to be large because of the bulk being forward-biased. On the other hand for BDFVF, a large input current is not expected since the aim is to achieve a virtual short between the input and output. The simulated results of the offset behaviour and the input current are shown in Figure 4-8 and 4-9 respectively.



**Figure 4-8 Offset voltage**



**Figure 4-9 Input current ( $V_{DD}=2V$ ,  $V_{SS}=0V$ )**

The simulated result of Figure 4-9 shows that the input current remains at less than 1.5pA.

#### *Input capacitance*

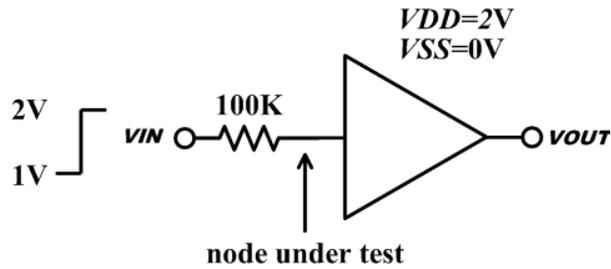
The depletion capacitance of the pn-junction  $C_j$  can be modelled by Equation 4-5:

$$C_{sb-depletion} = \frac{CJ_{nwell-p+}}{\left(1 - \frac{V_{SB}}{V_0}\right)^{MJ_{nwell-p+}}} AS + \frac{CJSW_{nwell-p+}}{\left(1 - \frac{V_{SB}}{V_0}\right)^{MJSW_{nwell-p+}}} PS \quad (4-5)$$

where  $CJ_{nwell-psub}$  is the zero-bias (i.e.  $V_{nwell-psub}=0$ ) body-junction capacitance per unit area over the n-well and p-substrate region,  $CJSW_{nwell-psub}$  is the zero-bias body-junction capacitance per unit length along the sidewall of the n-well and p-substrate region,  $MJ_{nwell-psub}$  and  $MJSW_{nwell-psub}$  are the grading coefficient for area and sidewall components respectively,  $V_0$  is the body-junction built-in potential, and  $A_{nwell}$  and  $P_{nwell}$  are the area and the perimeters of the n-well respectively. In the case of a bulk-driven differential pair, the input capacitance is expected to be large because of the bulk being forward-biased. On the other side for BDFVF, a large input capacitance is not expected since the aim is to achieve a virtual short between the input and output and hence only the depletion capacitance is introduced (i.e. the

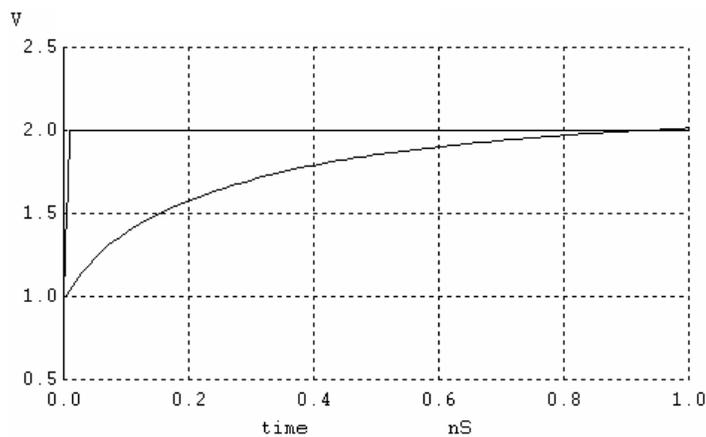
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diffusion capacitance can be avoided). To affirm this theoretical consideration further, the simulation condition as shown in Figure 4-10 was used.



**Figure 4-10 Simulation setup for the input capacitance**

The simulated plot of the setup in Figure 4-10 is given in Figure 4-11.



**Figure 4-11 Simulation results for the Figure 10 setup**

From Figure 4-11, the time constant  $\tau$  was found to be 0.93ns. Hence, the input capacitance was determined as 9.3fF ( $\tau=RC$ ).

#### **4.1.5 Section Conclusion**

A new type of FVF called BDFVF has been presented. This proposal utilizes a bulk-driven MOSFET with the replica-biased scheme as the input device to eliminate the DC level shift. The theoretical overview of the input current and capacitance has been provided, and the simulation results showed that the input current and capacitance are in the pico-amp and femto-Farad ranges. The attractive and

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advantageous performances of the FVF, such as high-power driving and low-power consumption were retained. The BDFVF is a powerful block of the FVF family which is free of level shift.

## ***4.2 Bulk-Driven Super Source Follower***

### **4.2.1 Introduction**

The BDFVF proposed in the previous section leads to achieving small input capacitance so that the weak signal input can remain unaffected, and also a high slew-rate performance so that the output signal can remain driven with large capacitive loads, while the static power consumption can remain low. In overall, the BDFVF is a strong candidate in buffer applications.

Based on this work the author has undertaken further studies and discovered that the same circuit design technique can be applied to Super Source Followers (SSF) as well. This section proposes a circuit modification technique of a SSF, and its application example that can achieve not only power-efficient (low-power high-speed) performance with a low input capacitance but also an additional feature of rail-to-rail operation.

### **4.2.2 Previous Essential Works**

This subsection briefly describes the previous works [GRA01] [LOP09] [RAM04] [HAG09A] using Figure 4-12, which the author has utilised to form the core part of our proposed CMOS buffer – a class-AB bulk-driven super source follower (BDSSF).

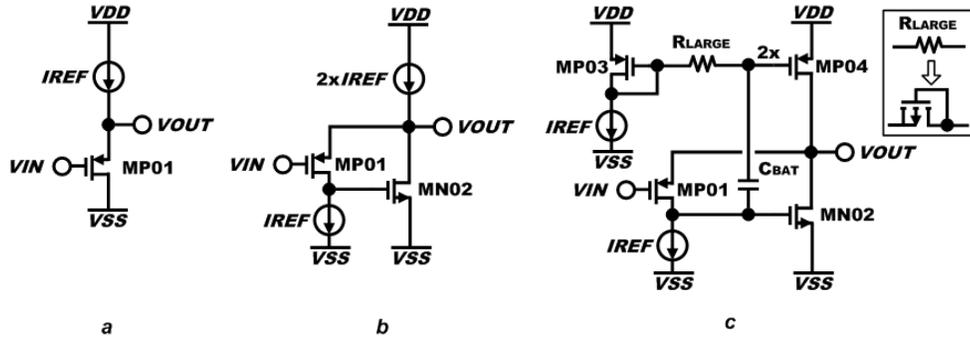


Figure 4-12 (a) class-A source follower, (b) class-A SSF, and (c) class-AB SSF proposed by Lopez-Martin *et al* [LOP09]

Figure 4-12(a) illustrates a conventional pMOS source follower, widely used as a level-shifted voltage buffer. If the body-effect is neglected, then the output voltage  $V_{OUT}$  follows the input voltage  $V_{IN}$  with an upward DC shift, i.e.  $V_{OUT} = V_{IN} + V_{SGMP01}$ , where  $V_{SGMP01}$  is the source-to-gate voltage of the transistor MP01. In case of an nMOS source follower,  $V_{OUT}$  is instead shifted down from  $V_{IN}$ . This conventional source follower is widely used, however the drawback is that it is sensitive to resistive loads. Since the drain current of MP01 is affected by the output current, the DC-level  $V_{SGMP01}$  cannot be kept constant. To overcome this concern, there exists a buffer which is often referred to as a Super Source Follower (SSF) [GRA01], as shown in Figure 4-12(b). The topology of Figure 4-12(b) is the same as Figure 4-12(a), but since the drain current through MP01 is biased with a constant current  $I_{REF}$  and is independent of the output current,  $V_{SGMP01}$  is also held constant against the output current. Today, many published proposals using this SSF can be found.

Recently, A.J. Lopez-Martin *et al* emphasized in their work in [LOP09] that despite the output becoming much insensitive to resistive loads with the SSF, the Slew-Rate (SR) remains in class-A operation. In the case of a pMOS SSF as shown in Figure 4-12(b), the positive SR is limited to  $I_{REF}/C_L$ , where  $C_L$  is the load capacitance. Hence

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increasing  $I_{REF}$  leads to one possible approach for the SR improvement, but at a cost of larger static power consumption. To avoid this trade-off, A.J. Lopez-Martin *et al* proposed a class-AB SSF in [LOP09] by using a quasi-floating gate (QFG) technique presented in [RAM04]. Their proposed circuit diagram is depicted in Figure 4-12(c).

In Figure 4-12(c), the gate of MP04 is weakly connected to the gate of MP03 with a large resistor  $R_{LARGE}$ , and also to the gate of MN02 with a capacitor  $C_{BAT}$ . In terms of DC characteristics, there exists no current flow across  $R_{LARGE}$  and therefore the gate voltage of MP03 and MP04 are the same. Thus the static power dissipation between Figure 4-12(b) and Figure 4-12(c) remains the same. In terms of AC characteristics, a high pass filter is formed with a cutoff frequency of  $1/(2\pi R_{LARGE} C_{BAT})$ , when observed from the gate of MN02 to the gate of MP04. Thus the ac element of the signal at the gate of MN02 can propagate to the gate of MP04, which in turn achieves class-AB operation without introducing any extra static current consumption. Furthermore, it is remarkable to realize in [LOP09] and [RAM04] that a unity-size diode-connected MOSFET but in the cutoff region can form a substantially large resistance of  $R_{LARGE}$ , which leads to achieving a low cutoff frequency  $1/(2\pi R_{LARGE} C_{BAT})$  with a moderately small capacitance of  $C_{BAT}$ . In [LOP09], A.J. Lopez-Martin *et al* discuss the  $C_{BAT}$  value in terms of attenuation factor  $\alpha$  ( $\approx 1/(1+C_{GS4}/C_{BAT})$ ). A  $C_{BAT}$  greater than 5 times  $C_{GS4}$  leads  $\alpha > 0.83$ , which is enough to propagate almost all frequencies except the DC component of the signal.

### 4.2.3 Class-AB Bulk-Driven Super Source Follower

Figure 4-13(a) illustrates the bulk-driven version of the SSF, which is the same type of circuit-design technique that was proposed in Section 4.1. As can be observed, the

input is connected to the bulk terminal of MP01 instead of its gate. MP02 is the replica of the input device MP01, i.e. MP02 and MP01 having equal transistor sizing and are biased with the identical drain current and the gate voltage. Since the bulk-terminal of MP02 is directly shorted to its source-terminal, MP01 tends to replicate the conditions of MP02 and hence the source-terminal follows the input voltage with no DC voltage in between, thus  $V_{OUT} = V_{IN}$ . Remarkably, the input capacitance  $C_{IN}$  of this type of buffer can be small because of the small junction capacitance of MP01. The expression of the junction capacitance of a MOSFET  $C_j$  can be simplified from Equation (4-5), which is given by

$$C_j = C_{j0} / (1 + (V_{SB} / V_0)^{0.5}) \quad (4-6)$$

where  $C_{j0}$  is the zero-bias ( $V_{SB}=0$ ) junction capacitance,  $V_{SB}$  is the bulk-to-source voltage, and  $V_0$  is the bulk junction potential. Since  $V_{SB}$  of MP01 in Figure 4-13(a) is designed to be zero, the junction capacitance of MP01 is constant at  $C_{j0}$ . The simulated value of  $C_{IN}$  is discussed in the next subsection.

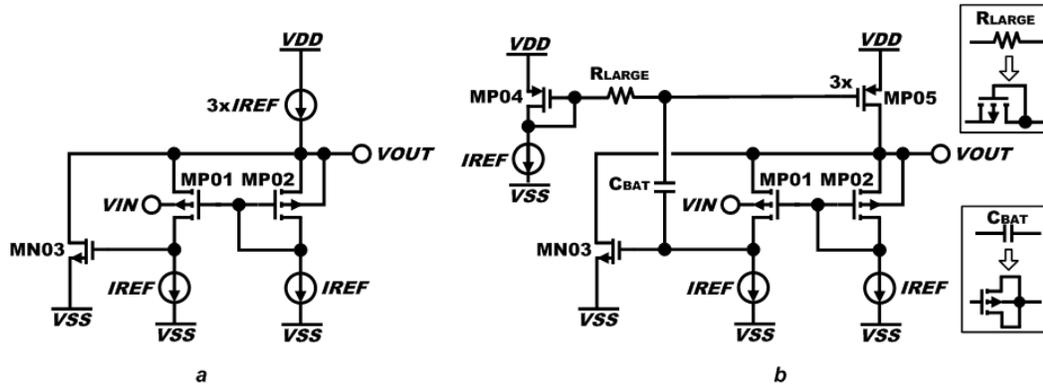


Figure 4-13 BDSSF (a) class-A operation, and (b) converting into class-AB operation using the QFG technique proposed by Ramìrez-Angulo *et al* [LOP09] [RAM04]

Figure 4-13(b) shows a class-AB BDSSF, where the class-AB operation has been implemented to Figure 4-13(a) with the same technique proposed by A.J. Lopez-Martin *et al* in [LOP09]. However, the author has chosen a modified approach for implementing the  $C_{BAT}$ . Ramìrez-Angulo *et al* stated the significance of the QFG

technique in [RAM04] that the actual value of  $C_{BAT}$  does not need to be highly accurate, as long as even a low frequency signal can be coupled. Owing to and appreciating this fact, the author attempted to eliminate the need for a poly-poly capacitor, and chose to form the  $C_{BAT}$  with a MOSFET as shown in Figure 4-13(b).

*Application Example - Rail-to-Rail Class-AB CMOS Buffer*

As an application example of the BDSSF, this block has been utilised in order to propose a rail-to-rail power-efficient CMOS voltage buffer. Figure 4-14 illustrates the circuit diagram of the proposal.

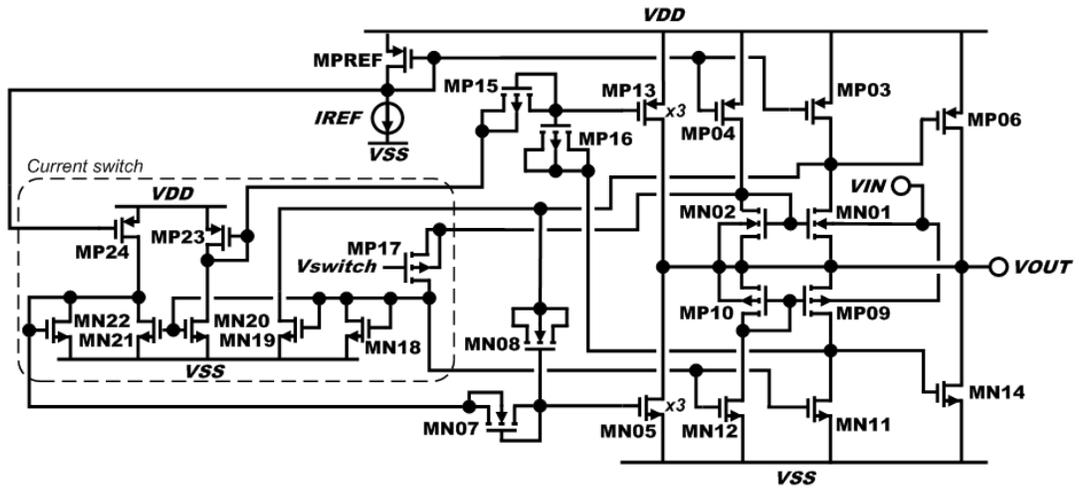


Figure 4-14 Class-AB rail-to-rail CMOS analogue buffer using a complementary pair of BDSSF

The operation principle of Figure 4-14 is as follow. From MN01 to MN08 and from MP09 to MP16 form a nMOS-type and pMOS-type of the BDSSF, respectively, and from MP17 to MP24 forms a current switch. The  $V_{switch}$  at the gate of MP17 determines the switching point between the two types of follower. When  $V_{IN}$  (and thus  $V_{OUT}$ ) is close to  $V_{SS}$  the pMOS follower is active while the nMOS follower is off, and when  $V_{IN}$  moves towards  $V_{DD}$ ,  $V_{OUT}$  and the drain voltage of MN02 also increase and eventually MP17 turns on to reduce the drain current of MN01, MN02 and MN05 (i.e. to shut off the nMOS follower) and instead to increase the drain

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current of MP09, MP10 and MP13 (i.e. to activate the pMOS follower) to continue the buffer operation.

#### 4.2.4 Simulated Results

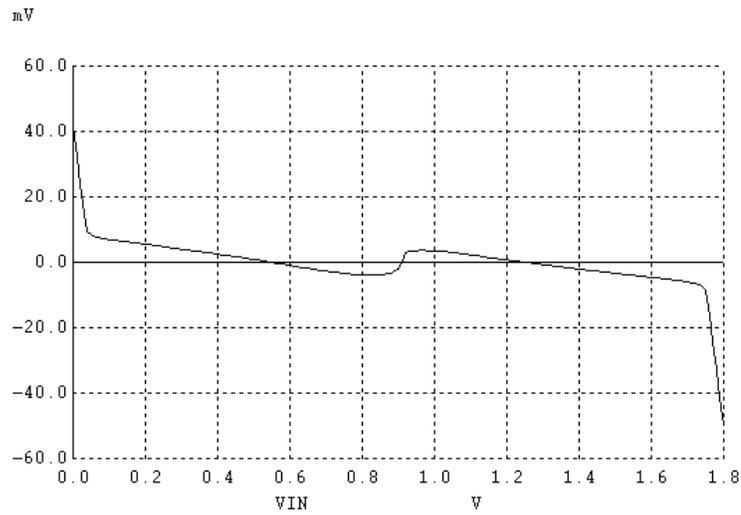
Using a 0.35 $\mu$ m CMOS process, the circuit of Figure 4-14 has been designed to operate at 1.8V supply voltage and simulated with the BSIM3 MOSFET models.

Table 4-2 shows the simulation results summarizing the overall performance.

**Table 4-2 Simulated results of the overall performance of Figure 4-14**

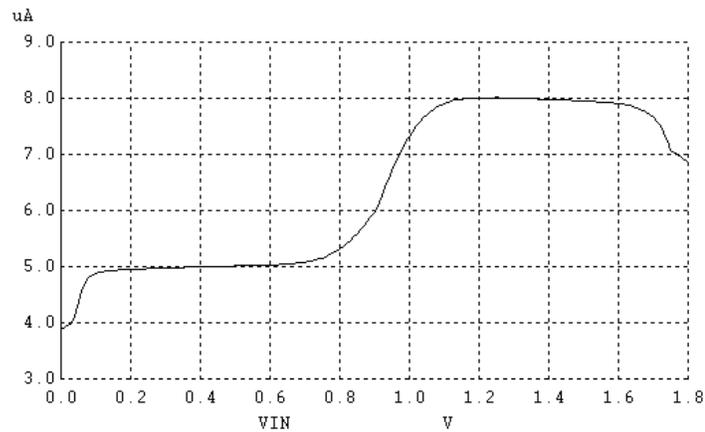
| Parameter   | Simulated Results  |
|---|--|
| -3dB frequency  | 6MHz   |
| Static current dissipation  | 5 $\mu$ A to 8 $\mu$ A for $V_{IN}$ sweeping between $V_{DD}$ and $V_{SS}$   |
| Slew rate   | SR+ = 9.3V/ $\mu$ s, SR- = 13.7V/ $\mu$ s  |
| Input capacitance   | 17fF   |
| THD   | -52dB (1.6Vpp@100kHz, CL=10pF)<br>-50dB (1.6Vpp@100kHz, CL=22pF)<br>-47dB (1.6Vpp@100kHz, CL=47pF)<br>-46dB (1.6Vpp@100kHz, CL=68pF) |
| Simulated condition: $V_{DD}$ =1.8V, $V_{SS}$ =0V, $V_{SW}$ =0.9V, CL= 10pF |  |

From Table 4-2 it is apparent that the proposed buffer of Figure 4-14 meets the demands which were discussed in Section 4.2.1. The input capacitance is as small as 17fF, the SR is very high such that the buffer can deliver a 1.6Vpp 100kHz signal with a total harmonic distortion as low as -46dB when the capacitive load is as large as 68pF, whilst the static current consumption remains under 8 $\mu$ A. Figure 4-15 is the simulated results of DC-sweeping the  $V_{IN}$ , which indicates that the offset remains small throughout the rail-to-rail operation.



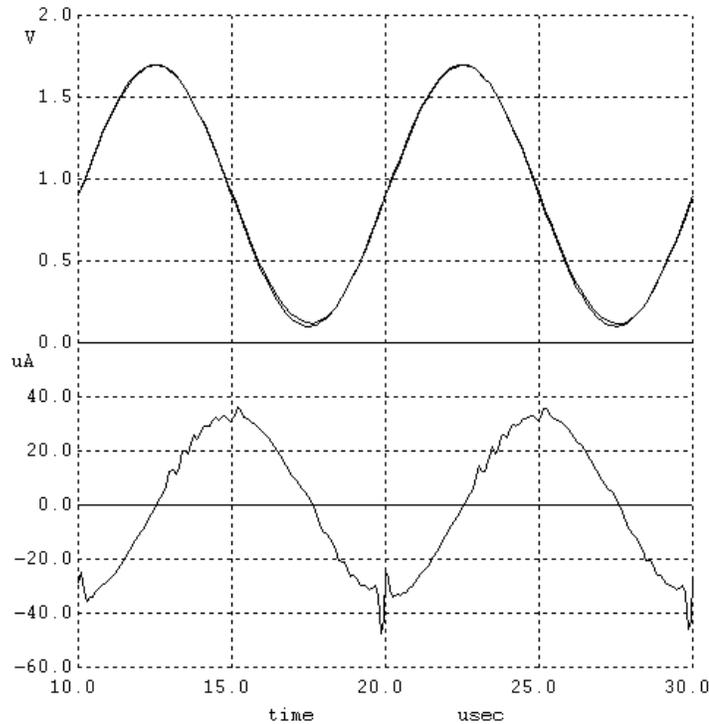
**Figure 4-15 Simulated results of the DC offset voltage versus  $V_{IN}$  ( $V_{DD}=1.8V$ ,  $V_{SS}=0V$ ,  $V_{switch}=0.9V$ )**

Figure 4-16 indicates the simulated results of the static current dissipation with DC sweeping the  $V_{IN}$  between  $V_{DD}$  and  $V_{SS}$ .



**Figure 4-16 Simulated results of the static current dissipation ( $V_{DD}=1.8V$ ,  $V_{SS}=0V$ ,  $V_{switch}=0.9V$ )**

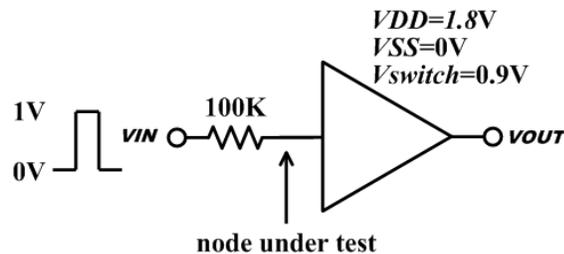
Figure 4-17 illustrates the simulated results of the  $V_{OUT}$  and the  $I_{OUT}$  with  $V_{IN}$  having 1.6V peak-to-peak 100kHz sine wave signal and a capacitive load CL of 68pF.



**Figure 4-17  $V_{OUT}$  vs  $V_{IN}$  and  $I_{OUT}$  with  $V_{IN} = 1.6V_{pp}$  100kHz sine wave and  $CL = 68pF$  ( $V_{DD} = 1.8V$ ,  $V_{SS} = 0V$ ,  $V_{switch} = 0.9V$ )**

Figure 4-16 and Figure 4-17 show clearly that the goal of excellent power efficiency is achieved – during the static mode the current dissipation of the proposed buffer remains under  $8\mu A$ , whereas  $I_{OUT}$  can be pushed and pulled to approximately  $\pm 40\mu A$  during the dynamic  $V_{IN}$  so that the Total Harmonic Distortion (THD) of  $V_{OUT}$  can be as small as -46dB even the  $CL$  is as large as 68pF.

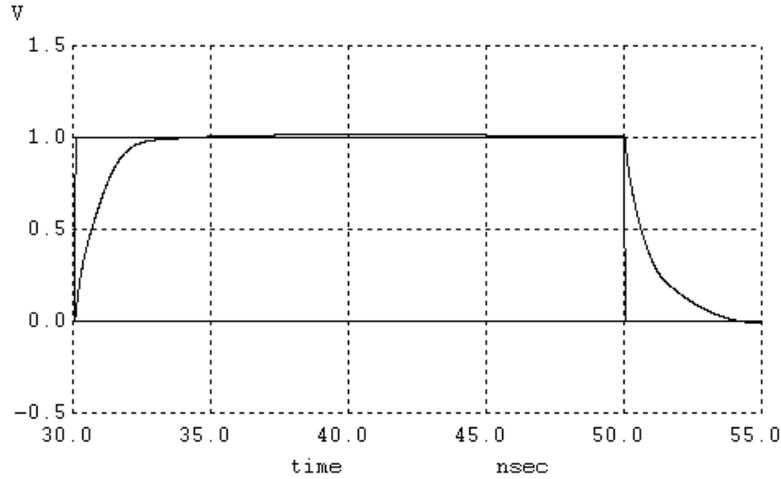
To verify the input capacitance of the proposed buffer shown in Figure 4-14, the simulation condition as shown in Figure 4-18 has been set up.



**Figure 4-18 Simulation setup for the input capacitance of Figure 4-13**

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The simulated plot of the setup in Figure 4-18 is given in Figure 4-19.



**Figure 4-19 Simulation results for the Figure 4-18 setup**

From Figure 4-19, the time constant  $\tau$  was found to be 1.7ns. Hence, the input capacitance was determined as 17fF ( $\tau=RC$ ).

#### **4.2.5 Section Conclusion**

A new circuit block called BDSSF and a new type of CMOS buffer using the complementary pair of BDSSF have been presented. Utilizing the bulk-driven MOSFETs with the replica-biased scheme and the QFG techniques into the buffer enabled us to have a few femto-Farad range of the input capacitance so that the weak input signals are minimally affected, whilst delivering the signal without much distortion even if the capacitive load is very large. The static current consumption can remain small too. The proposed buffer can become a serious contender for portable electronics needing to deliver weak analogue signals into large capacitive loads with as little distortion as possible.

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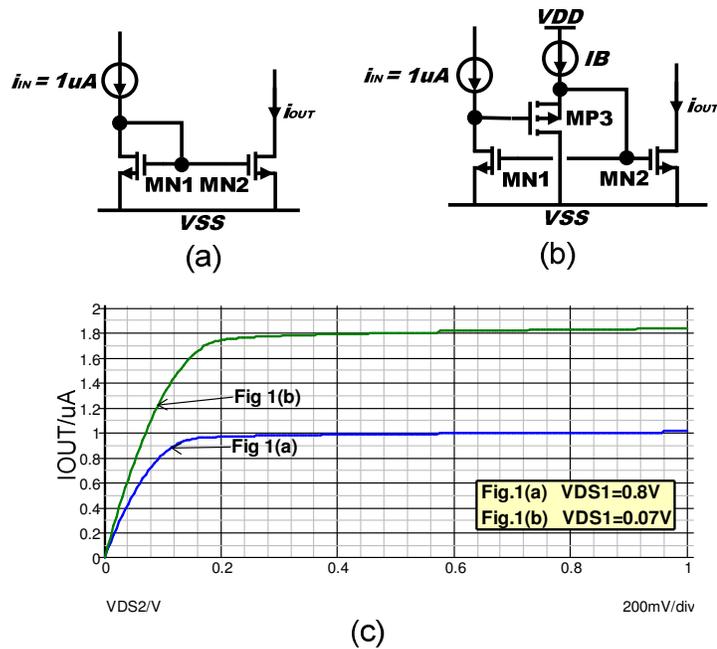
## **4.3 Bulk-Driven DC Level Shifter**

### **4.3.1 Introduction**

The BDFVF and the BDSSF proposed in Section 4.1 and 4.2, respectively, lead to achieving small input capacitance so that the weak signal input can remain unaffected, and also a high slew-rate performance so that the output signal can remain driven with large capacitive loads, while the static power consumption can remain low. In overall, both BDFVF and BDSSF are strong candidates in buffer applications.

Based on these works the author has undertaken further studies and discovered that BDFVF and BDSSF can lead to not only eliminating the DC level shift, but in fact the amount of the constant DC level can be easily programmed. The detail description of this new finding is given in the next subsection.

As to move on further, current mirrors, which are widely used for biasing and as active loads in analogue amplifiers, have been considered. Suppose that the current mirrors need to be operational in a low-voltage system. Under the limited supply voltage available, the designers must firstly confront the large voltage headroom consumed at the input device. One popular approach that can overcome this problem is by utilising a DC level shifter in-between the drain and the gate of the input device [RAM94], [RAJ02]. Figure 4-20 shows a couple of examples of CMOS circuit diagrams to describe this approach.



**Figure 4-20(a) Simple current mirror with  $I_{IN}=1\mu A$ , (b) with a DC level shifter, and (c) the  $V_{DS2}$  DC-sweep simulated results**

Figure 4-20(a) and (b) depict a simple nMOS current mirror and utilisation of a DC level shifter, respectively, and Figure 4-20(c) shows the simulated results of the two blocks using the BSIM3 MOSFET models of a  $0.35\mu m$  CMOS process. From Figure 4-20(c), it is clear that a significant offset in the DC current is observed for Figure 4-20(b). This is because the circuit block formed by MP3 and  $IB$  generates a DC level shift upward by more than the threshold voltage of MP3 and causes MN1 to leave the saturated region and enter into the linear region. To avoid this undesirable side effect, a DC level shifter that can be programmed to operate at a level less than the threshold voltage of a MOSFET is rather in favour of the novel technique, which to the best knowledge of the author has not been reported in any open literature of today's circuit design techniques.

This section provides the detail investigation report of utilising the BDSSF that can overcome the concern mentioned above.

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### 4.3.2 Proposal

The design objective in this section, which is to have a constant DC level shift less than the threshold voltage of a MOSFET, is simple to achieve by utilising the BDSSF of Figure 4-13(a) and (b). The source to bulk terminal of MP01,  $V_{SBI}$ , becomes reverse-biased by having a wider transistor width for MP01 and/or reducing its drain current  $I_{DSI}$ . The operation principle can be understood using the conventional square law model of a MOSFET. Whether the transistor size or the drain current of MP01 changes, this device maintains as the replica of MP02 and thus it operates in the saturated region. Let's suppose that MP01 is sized to have a relatively long length to minimize the effect of the channel length modulation, so that its drain current  $I_{DSI}$  can be approximated by:

$$I_{DSI} = (\mu_p C_{OX}/2) (W1/L1) (V_{SG1} - V_{TI})^2 \quad (4-7)$$

where  $\mu_p$  is the surface mobility of the pMOS transistor,  $C_{OX}$  is the capacitance of the gate oxide,  $W1$ ,  $L1$ ,  $V_{SG1}$ ,  $V_{TI}$  are the width, the length, the source-to-gate voltage, and the threshold voltage of MP01, respectively. If for instance  $W1$  is increased and/or  $I_{DSI}$  is decreased, then the overdrive voltage  $V_{SG1} - V_{TI}$  needs to be decreased to satisfy the above equation. However, since  $V_{SG1}$ , which is identical to the source-to-gate voltage of MP02, remains unchanged,  $V_{TI}$  needs to be increased.  $V_{TI}$  can be expressed by:

$$V_{TI} = V_{T0} + \gamma \{ (2|\Phi_F| + V_{SBI})^{0.5} - (2|\Phi_F|)^{0.5} \} \quad (4-8)$$

where  $V_{T0}$  is the zero-bias threshold voltage,  $\gamma$  is the body effect parameter,  $2|\Phi_F|$  is the Fermi potential, and  $V_{SBI}$  is the source-to-bulk voltage of MP01. As can be realized from this equation, to increase  $V_{TI}$ ,  $V_{SBI}$  needs to be increased. Thus in summary, increasing  $W1$  and/or decreasing  $I_{DSI}$  makes MP01 propagate a constant shift down voltage from the input to the output. Figure 4-21 shows the simulated

parametric sweep analysis of the width of MP01 and the length of MN05, denoted by W1 and L5, respectively.

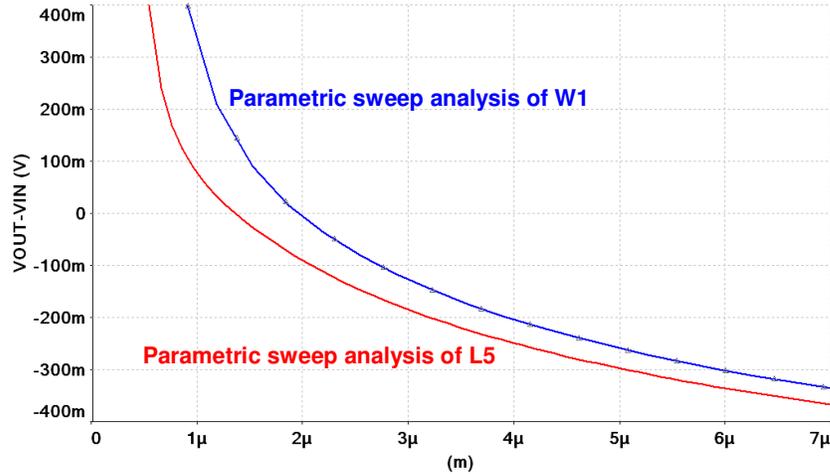


Figure 4-21 Parametric sweep simulation of Figure 4-13(a) and (b)

It is worth noting from Figure 4-21 that it is in theory feasible to level shift the input voltage upward as well as downward using the BDSSF of Figure 4-13(a) and (b), however from the view point of the effective input capacitance the authors recommend keeping the bulk-driven device MP01 in reverse biased operation. The description of the reverse biased junction capacitance, which is also known as the depletion capacitance  $C_j$ , is given by the following model:

$$C_j = C_{j0} / (1 + (V_{SB}/V_0))^{0.5} \quad (4-9)$$

where  $C_{j0}$  is the zero-bias ( $V_{SB}=0$ ) junction capacitance,  $V_{SB}$  is the bulk-to-source voltage, and  $V_0$  is the bulk junction potential. However, if the bulk of MP01 is in forward biased operation, then another capacitance model called the diffusion capacitance  $C_d$  would be introduced, which can be expressed by:

$$C_d = \tau_T (I_D/V_t) \quad (4-10)$$

where  $\tau_T$  is the transit time of the junction diode,  $I_D$  is the amount of current through the diode, and  $V_t$  is the thermal voltage ( $\approx 26\text{mV}$  at room temperature). Thus in the results for the forward biased operation of the bulk-driven device, the total input capacitance  $C_T$  would then be expressed as:

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$$C_T = C_j + C_d \quad (4-11)$$

Therefore, in order to avoid introducing the diffusion capacitance at the input, the author recommends using the proposed level shifter by configuring the bulk-driven device in reverse bias operation, i.e. using Figure 4-13(b) to shift down the voltage. For shifting up operation, the author recommends the use of an nMOS bulk-driven transistor for the input device.

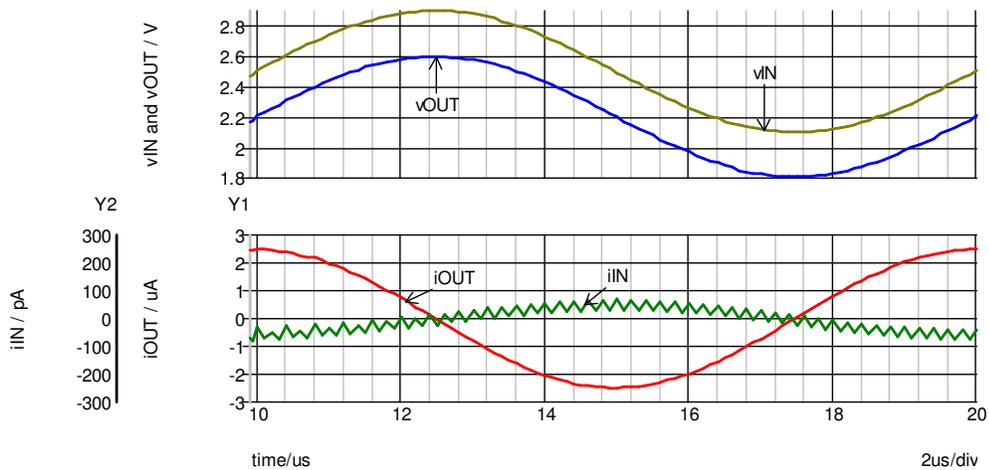
### 4.3.3 Simulated Results

Table 4-3 shows the simulated results of Figure 4-13(b) using the BSIM3 MOSFET models of a 0.35 $\mu$ m CMOS process. To see how different level shift settings and design approaches affect the overall performances, several BDSSF blocks of Figure 4-13(b) have been designed for comparison. The overall performance of the BDSSF blocks with 0-volt DC shift, 0.3-volt DC shift down achieved by increasing W1, 0.3-volt DC shift down achieved by decreasing  $I_{DS1}$ , 0.6-volt DC shift down effected by modifying both W1 and  $I_{DS1}$  are summarised in Table 4-3.

**Table 4-3 Simulated results of the overall performance of Figure 4-13(b) with different level shift configurations**

| Parameter  | Vshift =0V | Vshift =0.3V* | Vshift =0.3V** | Vshift =0.6V |
|--|------------|---------------|----------------|--------------|
| -3dB frequency   | 6.5MHz     | 8MHz          | 4.5MHz         | 5.5MHz       |
| Total current consumption  | 5.2μA      | 5.2μA         | 5.2μA          | 5.2μA        |
| Slew Rate+   | 2.0V/μs    | 2.1V/μs       | 2.1V/μs        | 2.2V/μs      |
| Slew Rate-   | 6.2V/μs    | 5.3V/μs       | 5.0V/μs        | 5.5V/μs      |
| PSRR   | 53dB       | 55dB          | 62dB           | 62dB         |
| 1/f noise at 1kHz  | 3.7μV/√Hz  | 3.7μV/√Hz     | 3.8μV/√Hz      | 4.0μV/√Hz    |
| THD:   |            |               |                |              |
| 0.8Vpp 100kHz  |            |               |                |              |
| CL=10pF  | -67.7dB    | -66.6dB       | -67.1dB        | -63.6dB      |
| CL=22pF  | -62.0dB    | -62.5dB       | -64.1dB        | -61.7dB      |
| CL=47pF  | -55.0dB    | -56.7dB       | -59.7dB        | -58.6dB      |
| 0.8Vpp 500kHz  |            |               |                |              |
| CL=10pF  | -51.6dB    | -53.4dB       | -48.1dB        | -50.1dB      |
| 0.8Vpp 1MHz  |            |               |                |              |
| CL=10pF  | -35.4dB    | -38.8dB       | -31.5dB        | -34.4dB      |
| * W1=3W2, L5=L6    ** W1=W2, L5=3.5L6  |            |               |                |              |
| Unless stated, the setup condition is as follows:<br>VDD=3.3V, VSS=0V, VIN=2.5V, CL=10pF |            |               |                |              |

The simulated results for the circuit of Figure 4-13(b) where the DC level shift is adjusted to 0.3V downward by modifying W1, and the input signal of 0.8Vpp at 100kHz is applied to the circuit with a load capacitance  $C_L$  of 10pF is as shown in Figure 4-22.

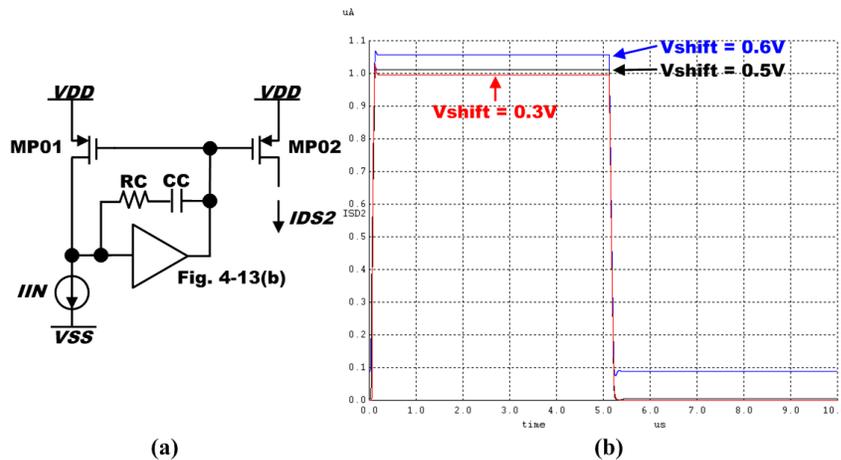


**Figure 4-22 Simulated results of Fig. 2(b) with W1=3W2 and  $I_{DS1}=I_{DS2}$ , where  $v_{IN} = 0.8V_{pp}$ , 100kHz sinusoidal wave and  $C_L$  with 10pF**

As can be observed from Figure 4-22, the input current of only  $\pm 70\text{pA}$  is necessary to apply a  $0.8\text{V}_{\text{pp}}$   $100\text{kHz}$  sinusoidal input voltage. It is worth remembering that this low input current would not have been possible to achieve if the bulk-driven input device MP01 was in the forward biased operation due to the significant increase in its input capacitance.

*Application Example*

As described in Section 4.3.1, a DC level shifter applied in a current mirror can be useful in reducing the voltage headroom consumption of the input device. Figure 4-23(a) illustrates the BDSSF of Figure 4-13(b) applied in a simple pMOS current mirror. RC and CC have been added between the input and the output of the BDSSF to minimize the output overshoot against the transient input signal. Given that  $V_{T0}$  of the pMOS transistor for the  $0.35\mu\text{m}$  CMOS process is approximately  $0.6\text{V}$ , the BDSSF of Figure 4-13(b) has been redesigned with a DC shift down of  $0.2\text{V}$ ,  $0.5\text{V}$  and  $0.6\text{V}$  and applied it to the current mirror as shown in Figure 4-23(a) to compare the overall performance. Figure 4-23(b) and Table 4-4 shows the simulated plots of the step response and the summary of the simulation results of Figure 4-23(a), respectively.



**Figure 4-23 (a) A pMOS current mirror with level shifted BDSSF and (b) simulated plot of  $1\mu\text{A}$  step response**

Table 4-4 Summary of the simulation results of Figure 4-23(a)

| Parameter  | Fig. 5(a)<br>without<br>Fig. 2(b) | Fig. 5(a)<br>with Vshift<br>= 0.2V | Fig. 5(a)<br>with Vshift<br>= 0.5V | Fig. 5(a)<br>with Vshift<br>= 0.6V |
|--|-----------------------------------|------------------------------------|------------------------------------|------------------------------------|
| Static current consumption of Fig. 2(b)                                | ---                               | 5.1 $\mu$ A                        | 5.0 $\mu$ A                        | 5.1 $\mu$ A                        |
| -3dB frequency   | 90MHz                             | 70MHz                              | 100MHz                             | 100MHz                             |
| THD 1 $\mu$ App  |                                   |                                    |                                    |                                    |
| 1MHz   | -53.3dB                           | -53.6dB                            | -53.2dB                            | -57.1dB                            |
| 10MHz  | -41.3dB                           | -37.0dB                            | -37.2dB                            | -38.1dB                            |
| Setup condition: $VDD=1.8V$ , $VSS=0V$ , $IIN=1\mu A$ , $VD2=VDD-0.5V$ |                                   |                                    |                                    |                                    |

As can be observed from Table 4-4, until 1MHz operation none of the BDSSF adds distortion noticeably. However, as can be realized from Figure 4-23(b) a caution is necessary to determine the amount of DC level shift. A DC level shift too close to  $V_{T0}$  would cause a noticeable offset in the DC current. In the case of the simulated plot of Figure 4-23(b), when the level shift is almost identical to  $V_{T0}$  ( $=0.6V$ ) a DC offset current of approximately 60nA and 90nA is introduced when the input current is 1 $\mu$ A and 0 $\mu$ A, respectively. Even though the level shift was approximately 100mV below  $V_{T0}$  (i.e. when the level shift is set to approximately -0.5V), the offset current of 10nA and 4nA is drawn when the input current is 1 $\mu$ A and 0 $\mu$ A, respectively. Therefore it is advisable not to set the DC level shift too close to  $V_{T0}$ .

#### 4.3.4 Section Conclusion

A novel design approach for a DC level shifter that can be programmed to a level less than the threshold voltage of a MOSFET has been presented. This technique is

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based on utilising the power efficient BDSSF, with the bulk-driven input device forced to be reverse-biased to generate the constant DC voltage. SPICE simulations of the proposed block set up in a current mirror demonstrated that until 1MHz operation the proposed block does not introduce additional distortion, whilst the extra static current consumption spent is as little as  $5\mu\text{A}$ . This proposed block has been shown to be an excellent solution for reducing the voltage headroom consumption of a current mirror but without introducing DC offset current.

#### ***4.4 Chapter Conclusion***

In this chapter, new circuit design techniques that can convert the FVF [CAR05] and the SSF [GRA01] into the bulk-driven approach, which the author has given the names as BDFVF and BDSSF, respectively, have been presented. These two newly developed blocks still possess the load regulation capability so that the output becomes insensitive to resistive loads, but the bulk-driven approach allows implementing an additional feature such that the DC level shift can be eliminated and even programmable. The QFG technique [RAM04], that can convert the output slew rate from class-A to class-AB operation [LOP09], has also been investigated with the BDSSF and demonstrated that low-power high-speed performances can be achieved. Furthermore, it was verified that the degraded input impedance, which comes along with the bulk-driven approach, was not the case with BDFVF or BDSSF.

To further extend, two application examples of the BDSSF have been also demonstrated. One example was a design of a CMOS buffer using the complementary pair of BDSSF, which leads to achieving low-power (static current consumption of less than  $8\mu\text{A}$ ) high-drive (THD as low as  $-46\text{dB}$  with a  $1.6\text{V}_{\text{pp}}$

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100kHz sine wave signal and a 68pF load) performances. The other application example was an implementation of the level-shifted BDSSF in a current mirror. Since the DC level shift of the BDSSF can be programmed at a level less than the threshold voltage of a MOSFET, the voltage headroom consumption of the input device of the current mirror can be reduced but without having the DC offset current at the output. The BDSSF in a current mirror does not introduce additional distortion until 1MHz operation, whilst the extra static current consumption spent is as little as 5 $\mu$ A.

In overall the newly developed BDFVF and BDSSF are powerful building blocks of source followers that can contribute achieving low-power high-speed performances of analogue circuit design.

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## Chapter 5      Bulk-Biased Cascodes

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Cascode devices play essential roles in analogue systems, and many literatures discuss the properties in details [RAZ01], [SAN06], [SED11], [BAK08], [GRA01], [ALL02], [JOH97]. Adopting cascode devices in analogue amplifiers leads to increasing the output resistance and hence the small-signal gain as well. When a differential amplifier is used in a negative feedback configuration, its overall precision improves with the large open-loop small-signal gain of the amplifier, and thus implementing cascode devices helps a lot in this sense. In current mirror applications, cascode devices allow to suppress the effect the channel-length modulation of the MOSFET and hence the output current becomes insensitive to the voltage at the output node. It is interesting to note the way Razavi describes the operation behaviour of cascode devices in his literature book in [RAZ01]. Quoting from his literature in the single-stage cascode amplifier section, *in a sense the cascode transistor “shields” the input device from voltage variation at the output.* Allen and Holberg book in [ALL02] provides the detail performance analysis for different operational amplifier (op-amp) topologies, and states that *the Power Supply Rejection Ratio (PSRR) of the folded-cascode op-amp has been greatly improved over the two-stage op-amp.* In Razavi’s language, this statement can be alternatively described that the cascode device also “shields” the output node from the power supply noise.

This chapter presents a circuit design technique such that the output resistance of a cascode device can be further increased using its bulk-terminal. This technique was

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developed by the author while tackling the problem of the low transconductance of a bulk-driven MOSFET  $g_{mb}$  which results to small open-loop gain of the op-amp when a bulk-driven differential pair (BDDP) is applied.

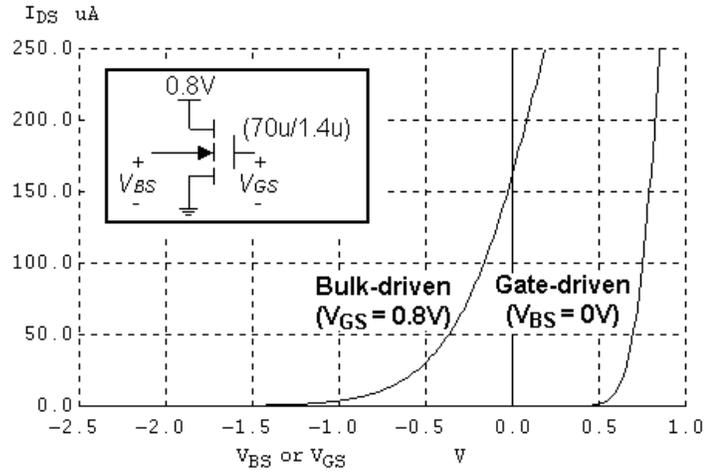
To demonstrate the effect of the developed circuit design approach of a cascode device, a complete set of a 0.8-volt rail-to-rail fully differential folded-cascode Operational Transconductance Amplifier (OTA) is designed using a 0.35 $\mu$ m twin-well CMOS technology having a threshold voltage of 0.6-volt. Taking this design as an opportunity, some other previous works of the bulk-driven approach are also adopted in the other part of the OTA for review. In this OTA, a complementary pair of BDDP [TER02] is implemented at the input stage to achieve a constant effective transconductance  $g_m(eff)$ . In the Common-Mode Feedback (CMFB) design, not only that the BDDP is applied at the input stage but also bulk-driven cascode current mirrors [TER02] have been adopted to reduce the voltage headroom consumption. The simulated results of the overall performance of the OTA are provided.

## ***5.1 A 0.8-Volt Fully-Differential CMOS OTA Design***

### **5.1.1 Introduction**

As discussed in Chapter 2 a BDDP leads to achieving rail-to-rail Input Common-Mode Range (ICMR) operation under the low-supply voltage constraint, however many drawbacks are associated with this approach. One of the severe concerns is that the transconductance of a bulk-driven MOSFET is  $g_{mb}$  is less than the transconductance of a gate-driven MOSFET is  $g_m$ . This advantage and the

disadvantage can be visually realised by performing a simulation plot for  $g_{mb}$  and  $g_m$ , as shown in Figure 5-1.



**Figure 5-1 Simulating transconductance characteristics of gate-driven and bulk-driven nMOS transistors using a  $0.35\mu m$  CMOS technology**

As can be seen in Figure 5-1, the bulk-driven MOSFET is still in the active region at the zero-bias voltage which results to wider operation range than the gate-driven MOSFET. On the other hand  $g_{mb}$  is less than  $g_m$ . ( $g_m$  and  $g_{mb}$  are the slopes of its drain current versus its input voltage at the bias point). Thus implementing a BDDP in the op-amp design causes the open-loop small-signal gain of the op-amp to be reduced.

Another severe concern that needs to be addressed is that  $g_{mb}$  is dependent to the DC operating point of the bulk-driven MOSFET, namely its bulk-to-source voltage  $V_{BS}$ .  $g_{mb}$  can be expressed by

$$g_{mb} = \frac{\mathcal{K}_m}{2\sqrt{2|\Phi_F| - V_{BS}}} \quad (5-1)$$

where  $2|\Phi_F|$  is the Fermi potential and  $\gamma$  is the body-effect coefficient. Thus a BDDP causes a large variation in the effective transconductance of the op-amp  $g_m(eff)$ , which results to introducing signal distortion and creating difficulty in the frequency compensation of the multi-stage op-amps [HOG92], [WU94].

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There are some previous works that address the above issues. The work presented by Terry *et al* in [TER02] addresses the issue the  $g_m(\text{eff})$  variation of a BDDP, and the work presented by Rosenfeld *et al* in [ROS04] addresses the issue of low  $g_{mb}$  of a BDDP adopted in folded-cascode OTA design by utilising the gain boosting technique. However, as studying further this gain boosting technique the author came up with an alternative design idea which leads to increasing the output resistance without introducing an additional hardware or extra power consumption in the core OTA block.

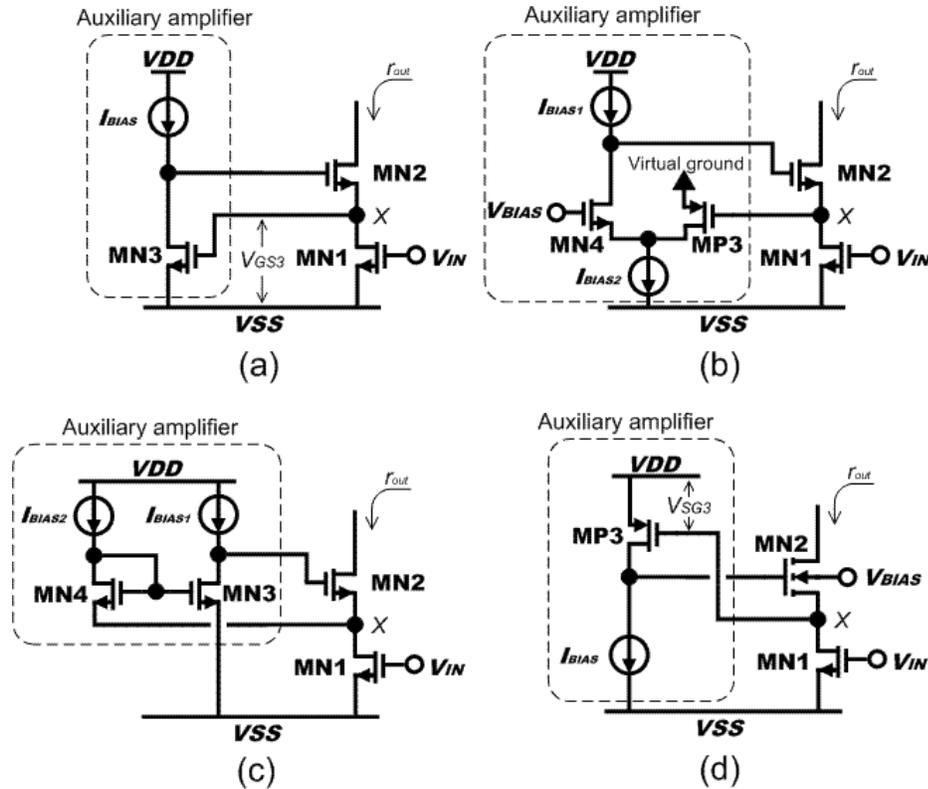
In this section the design of a 0.8 volt fully differential rail-to-rail folded-cascode OTA using a 0.35 $\mu\text{m}$  twin-well CMOS technology having a threshold voltage of 0.6 volt is presented. This OTA consists of not only a complementary pair BDDP for achieving rail-to-rail operation with constant  $g_m(\text{eff})$ , but also the author's original design idea for the cascode devices of the OTA so that the output resistance is increased and hence the open-loop gain is enhanced to over 60dB.

### **5.1.2 Previous Essential Works**

As the design task for achieving high-performance OTA that can be operated with a 0.8 volt supply voltage using a CMOS technology having a threshold voltage of 0.6 volt was not easy, many previous essential works have been referred and utilised in the OTA design. This subsection provides the brief review of those previous essential works.

## Gain-Boosting Technique

According to the literature in [RAZ01], the topology of the gain-boosting technique was first invented in 1976 in [HOS79] and applied to boost the gain of the op-amps in 1989 in [BUL90] and [SAC90]. The concept of this topology is illustrated in Figure 5-2.



**Figure 5-2** Gain-boosting topology with different auxiliary amplifiers, (a) common-source stage [HOS79] (b) folded-cascode [RAZ01], (c) common-source stage with a level shifter [COB94], and (d) complementary common-source stage [ROS04]

Figure 5-2(a) shows the circuit realisation of the gain-boosting topology using a common-source type of auxiliary amplifier placed in the feedback loop [HOS79], [BUL90], [SAC90]. This feedback amplifier regulates the voltage at node-X so that the output current remains more constant, which results to achieving a higher output resistance  $r_{out}$ . This approach, however, causes a limitation in the output voltage swing since the regulated voltage at node-X  $V_X$  becomes equal to the gate-to-source voltage of MN3  $V_{GS3}$ , which is too much voltage consumption for low-voltage

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applications. To overcome this concern, there are some known alternative design approaches today. Razavi's literature in [RAZ01] discusses utilising the folded-cascode type of auxiliary amplifier, as shown in Figure 5-2(b), as this concept allows pMOS and nMOS combination in the small-signal path. John and Martin's literature in [JOH97] on the other hand introduces Coban *et al*'s approach presented in [COB94], which is shown in Figure 5-2(c). This approach is identical to the one shown in Figure 5-2(a) except that a diode-connected MOSFET MN4 is additionally included for level-shifting purposes. In Rosenfeld *et al*'s work in [ROS04] presented an approach as shown in Figure 5-2(d), which its auxiliary amplifier is in the pMOS version of a common-source amplifier as shown in Figure 5-2(a). However, Zabihian *et al* in [ZAB07] provides the large-signal analysis of Figure 5-2(d) and states that it is not simple to operate the transistor MP3 in saturation under the low-supply voltage environment unless the threshold voltage of MN2 is reduced by  $V_{BIAS}$ . Also,  $V_X$  may be sensitive to  $V_{DD}$  noise since the auxiliary amplifier in Figure 5-2(d) is not a differential amplifier (as  $V_X$  and  $V_{DD}$  are directly related by  $V_{SG3}$ ).

While studying further the approaches mentioned above, the author noticed an important property of a cascode device using its bulk-terminal. This chapter reports an OTA design without the use of auxiliary amplifiers but instead utilising only the bulk-terminal of the cascode devices for increasing the output resistance.

#### *Bulk-Driven Current Mirror*

The bulk-driven current mirror that was developed by Blalock *et al* in [BLA95], as shown in Figure 5-3(a), can eliminate the large voltage drop across the input device. This is because the voltage drop across the input device MN1  $V_{DS1}$ , which is equal to the bulk-to-source voltage of MN1  $V_{BS1}$ , does not need to be greater than the threshold voltage  $V_{T0}$  for proper operation. The cascode configuration [BLA96], as shown in

Figure 5-3(b), can be used to improve current matching and increase the finite output impedance of the current mirror. In this configuration, the voltage drop across the input devices MN1 and MN3, i.e.  $V_{DS1} + V_{DS3} (=V_{BS1} + V_{BS3})$ , still remains below  $V_{T0}$ .

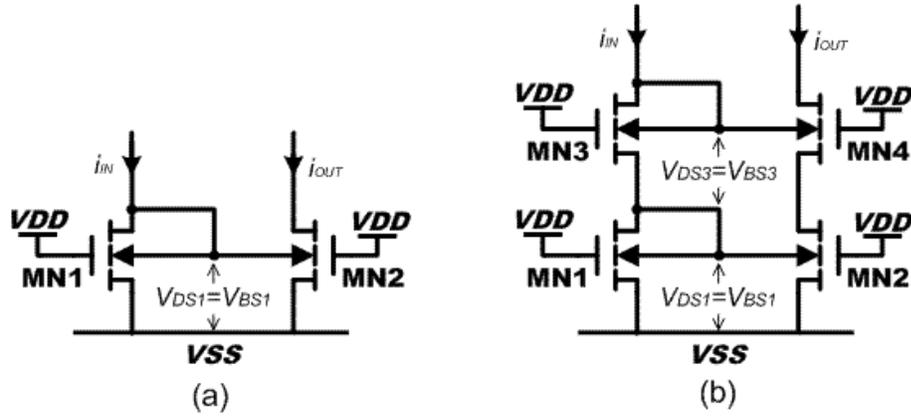


Figure 5-3 Bulk-driven current mirror (a) simple [BLA95] and (b) cascode [BLA96]

Taking the advantage of this low drop voltage property of the bulk-driven current mirror, the OTA design reported in this chapter utilises the Bulk-Driven Cascode Current Mirror (BDCCM) as shown in Figure 5-3(b) in the Common-Mode Feedback (CMFB) block.

### Complementary BDDP

As discussed in the Introduction in Section 5.1.1, a BDDP applied in an op-amp design leads to achieving rail-to-rail IMCR operation but suffers from large  $g_m(\text{eff})$  variation. To overcome this concern a design technique called the complementary BDDP, which has been proposed by Terry *et al* in [TER02], has been applied in the OTA design reported in this chapter. Detail analysis results are given in the next section.

### Supply-Independent Bias Circuit

To design an OTA that can be operated with a 0.8 volt supply voltage using a CMOS technology having a threshold voltage of 0.6 volt, a bias circuit block that can be also

operated with the 0.8 volt supply voltage was also needed. To accomplish this need, a supply-independent bias circuit block that can operate at a minimum supply voltage of  $V_{T0}+2V_{DSsat}$ , which was proposed by Dong *et al* in [DON02], has been applied in the OTA design reported in this chapter. Detail analysis results are given in the next section.

### 5.1.3 Proposal

#### Core OTA

Figure 5-4 illustrates the core part of the low-voltage fully-differential OTA, which utilises the folded-cascode topology and the bulk-driven approach at the input stage for achieving rail-to-rail ICMR operation.

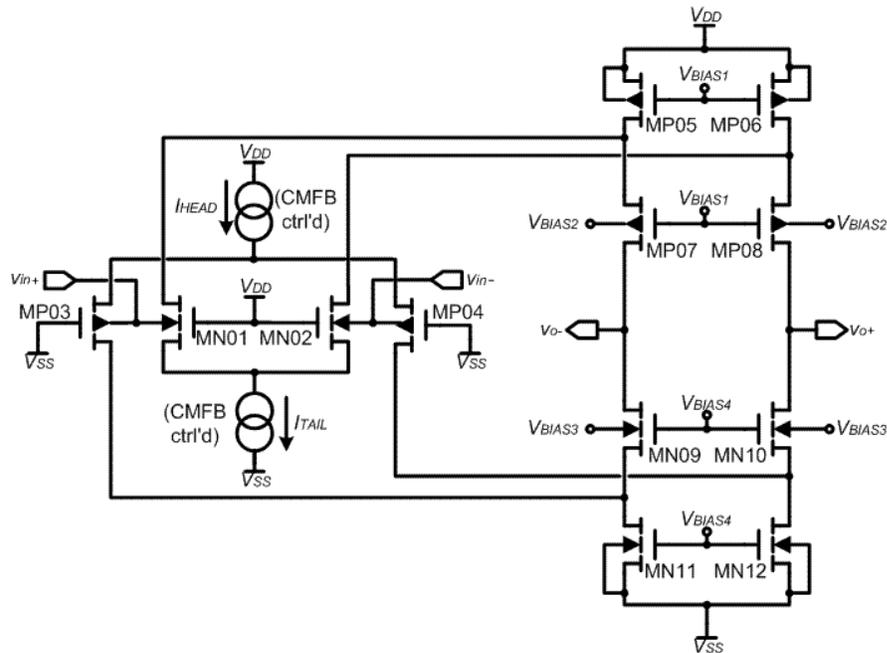


Figure 5-4 Proposed core OTA

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Complementary BDDP

As mentioned in Section 5.1.1, the depletion characteristics of an nMOS transistor allow the ICMR to extend below the negative power supply. The transconductance of an nMOS transistor, however, increases by increasing the ICMR [BLA98].

This effect can be illustrated by simulating the transconductance of an nMOS transistor with the set-up shown in Figure 5-5(a). The results of the simulation are shown in Figure 5-6. The variance of the input transconductance causes the op-amp open-loop gain and also the phase margin to vary with ICMR. For a pMOS transistor with the setup illustrated in Figure 5-5(b), the complementary characteristics can be observed as illustrated in Figure 5-6.

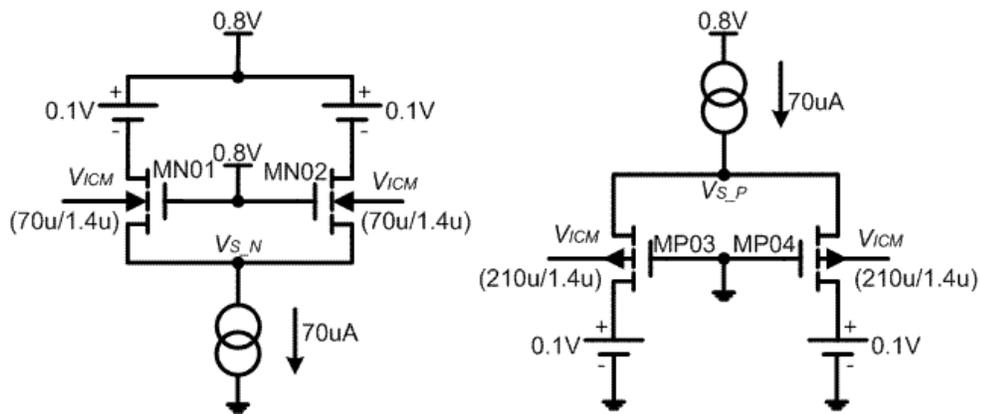
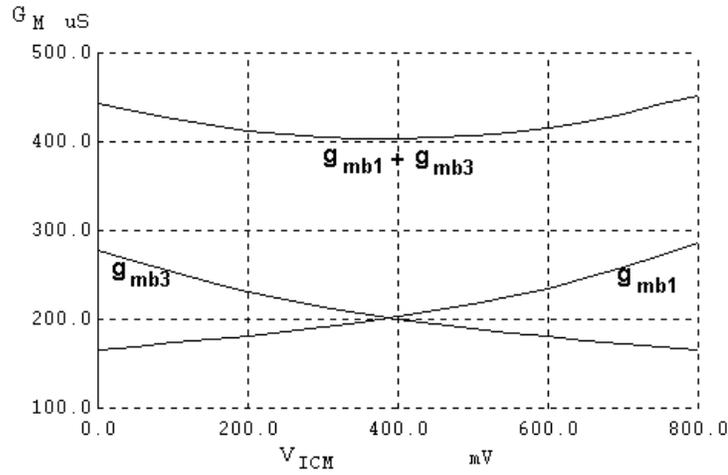


Figure 5-5 Setup for simulating (a)  $g_{mb1}$  and (b)  $g_{mb3}$



**Figure 5-6 Simulation plots of  $g_{mb1}$  and  $g_{mb3}$**

In order to reduce the variance of the input transconductance, complementary BDDP can be utilised [TER02], as the results demonstrate in Figure 5-6. The overall transconductance variation, which is the sum of the transconductance of the nMOS and pMOS transistors, is improved by approximately 50%. To achieve a transconductance with minimum variations, a proper W/L ratio for the nMOS and pMOS transistors should be carefully selected.

### *Cascode Devices*

As can be realized from Figure 5-1, the transconductance of a bulk-driven differential pair is less than that of a gate-driven differential pair, causing a challenge in achieving high open-loop gain for the amplifier. One possible method to increase the open-loop gain is to increase the output resistance. The output resistance of the core OTA in Figure 5-4 can be approximated to:

$$r_{out} \approx (g_{m7} + g_{mb7})r_{o7}(r_{o5} // r_{o1}) // (g_{m9} + g_{mb9})r_{o9}(r_{o11} // r_{o3}) \quad (5-2)$$

From Equation (5-2) it can be realized that  $g_{mb7}$  and  $g_{mb9}$  can be increased as the bulks are slightly forward-biased. Therefore if a twin-well process is available, the bulks of cascode transistors could be slightly forward-biased. As an numerical example, for the term  $(g_m + g_{mb})$ , which equals to  $(1 + \eta)g_m$ , the  $\eta$  can be increased by

approximately 0.04 when  $V_{BS}$  of the nMOS and pMOS cascode transistors are increased from -0.1V to 0.2V in a 0.35 $\mu$ m CMOS technology.

### Common-Mode Feedback

To stabilise the CML of the two outputs to be midway between the power-supply voltages, a CMFB block is required. Figure 5-7 illustrates typical circuit diagrams of continuous-time CMFB circuits [ALL02], [RAZ01].

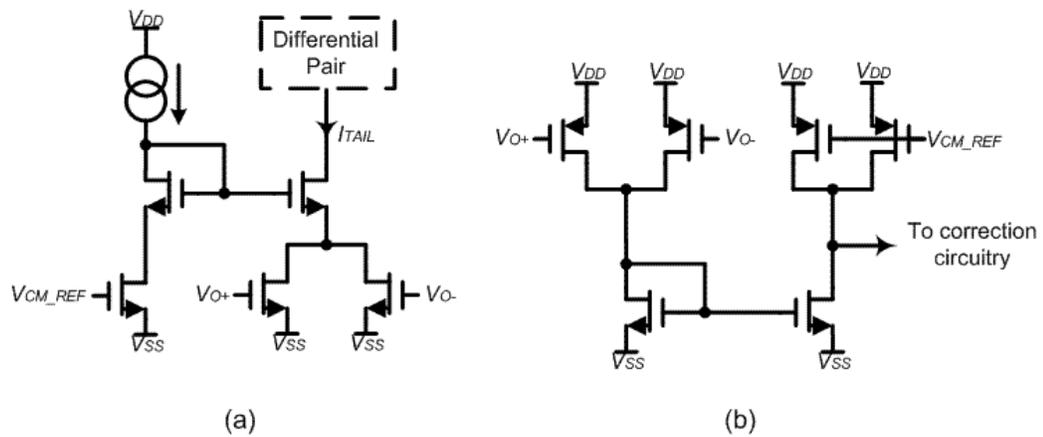


Figure 5-7 Typical CMFB circuit (a) current output and (b) voltage output

The problem of using the CMFB circuit shown in Figure 5-7 in a low-supply-voltage environment is that the reference input  $V_{CM\_REF}$  and the output CML of the OTA have to be greater than the threshold voltage for the circuit to operate in the active region. To overcome this problem, the bulk-driven approach can be utilised. The proposed CMFB circuit is illustrated in Figure 5-8.

These proposed CMFB circuits are simply the same as Figure 5-7(b) with the bulk-driven differential pairs and current mirrors included.  $M_{C05P}$  and  $M_{C22N}$  are added extra to improve the input range of operation, which is the output range of the core OTA. Simulation results of this proposal are shown in Figure 5-9.

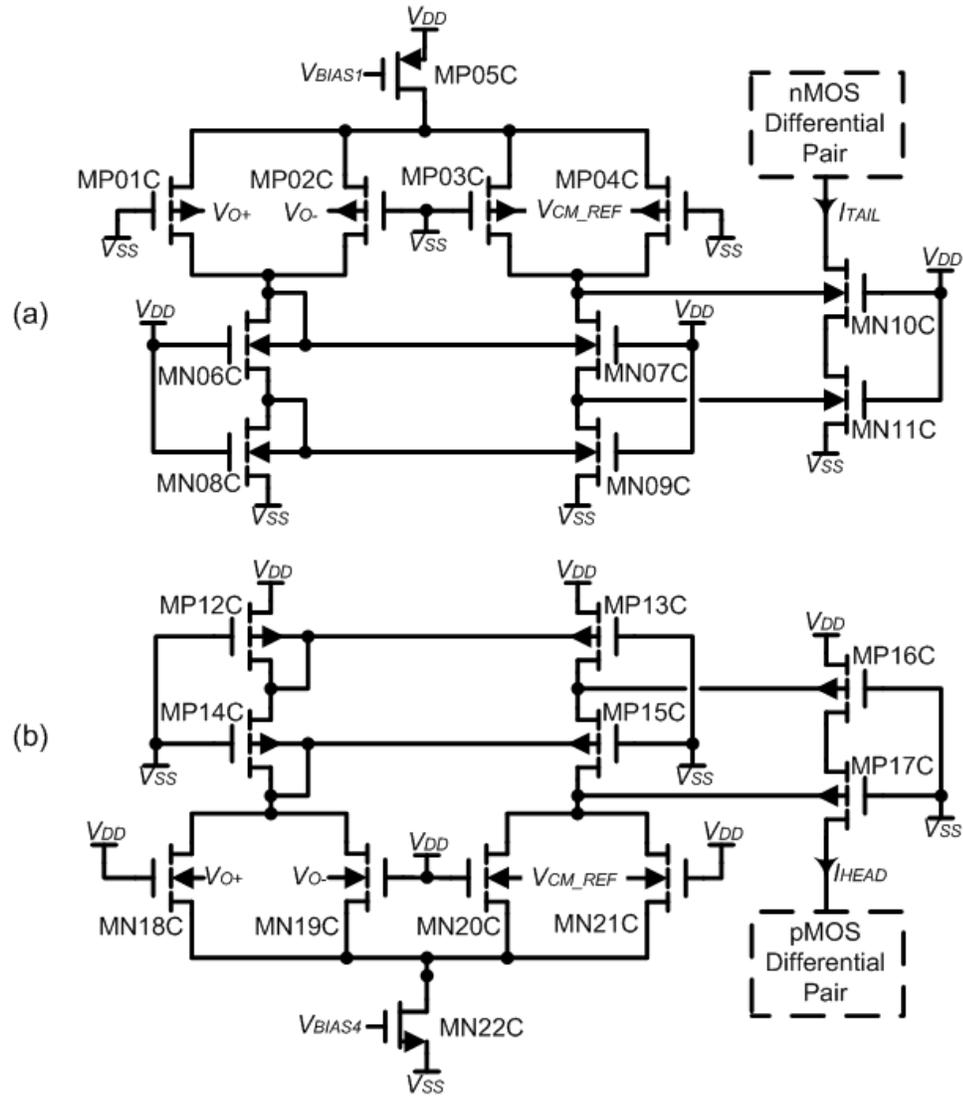


Figure 5-8 Proposed (a) nMOS driven CMFB and (b) pMOS driven CMFB

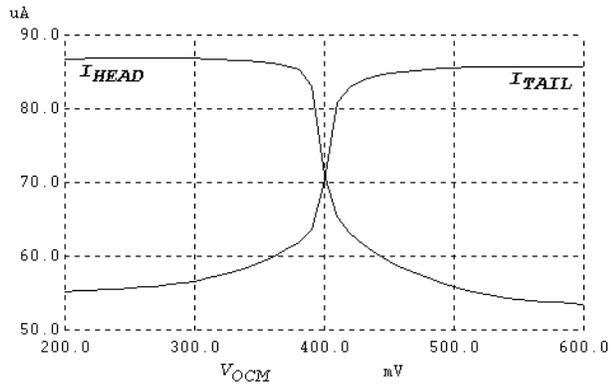


Figure 5-9 Verification of the proposed CMFB circuitry

The simulation results shown in Figure 5-9 imply that the bulk-driven technique can also be a candidate for low-voltage rail-to-rail CMFB design.

### Supply-Independent Bias Circuit

The supply independent bias circuit presented in [DON02], as shown in Figure 5-10(a), can be operated at a minimum supply voltage of  $V_{T0}+2V_{DSsat}$ . This is very suitable for low-voltage systems and therefore applied for generating  $V_{BIAS1}$  and  $V_{BIAS4}$ . For generating  $V_{BIAS2}$  and  $V_{BIAS3}$ , which have to be less than  $V_{T0}$ , bulk-driven devices can be utilised as shown in Figure 5-10(b).

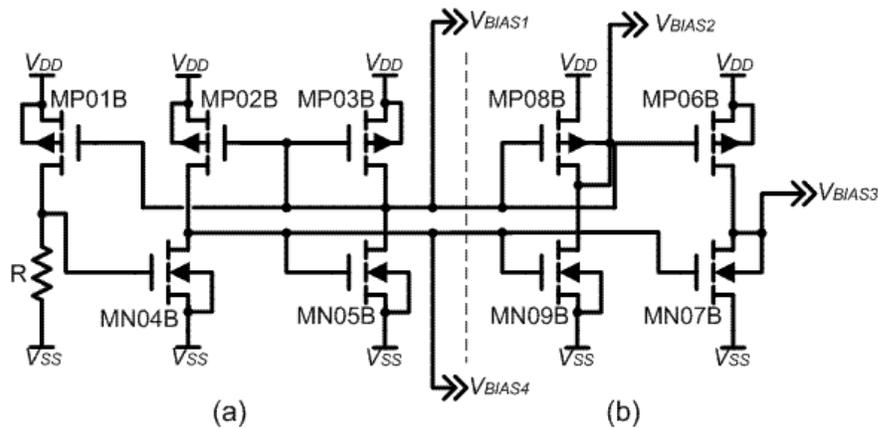


Figure 5-10 (a) Using the supply-independent bias circuit presented in [6] for generating  $V_{BIAS1}$  and  $V_{BIAS4}$  and (b) bias voltage generator for  $V_{BIAS2}$  and  $V_{BIAS3}$

Simulation results of Figure 5-10 are illustrated in Figure 5-11.

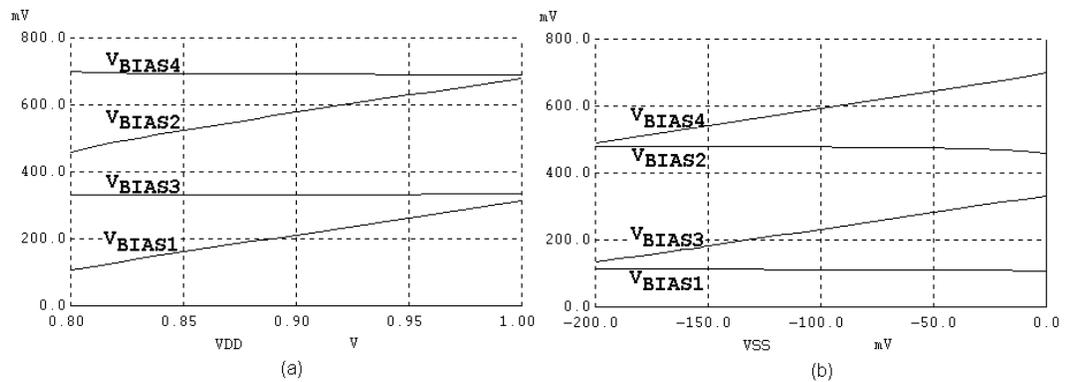
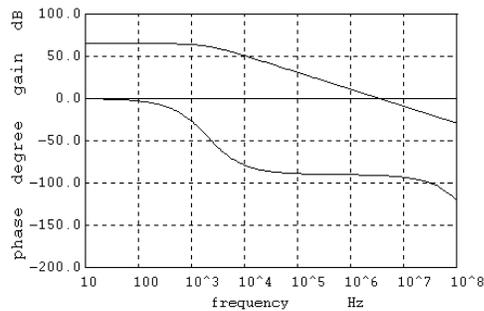


Figure 5-11 Effects of bias voltages with respect to (a) VDD and (b) VSS

As expected and seen in Figure 5-11,  $V_{BIAS1}$  and  $V_{BIAS2}$  are independent of  $V_{SS}$  and therefore suitable for biasing pMOS devices. Similarly,  $V_{BIAS3}$  and  $V_{BIAS4}$  are independent of  $V_{DD}$  and therefore suitable for biasing nMOS devices.

### 5.1.4 Simulation Results

A 0.35 $\mu$ m CMOS twin-well technology was used to verify the proposal. The Bode plot of the OTA with a load capacitance of 5pF is depicted in Figure 5-12. The overall OTA characteristics are shown in Table 5-1.



**Figure 5-12 Simulated plots of open-loop gain and phase margin**

**Table 5-1 Summary of the proposed OTA Performance**

| Characteristics  | Simulated Value                      |
|--|--------------------------------------|
| Open-loop DC gain  | 66dB                                 |
| Unity gain-bandwidth   | 3.4MHz                               |
| Total current consumption                                      | 243 $\mu$ A                          |
| Phase margin   | >80°                                 |
| Differential output voltage swing                              | 1V                                   |
| Slew rate  | SR+=4.7V/ $\mu$ s, SR-=5.1V/ $\mu$ s |
| ICMR   | 0.8V                                 |
| $V_{DD} = 0.8V$ , $V_{SS}=0V$ , $V_{ICM} = 0.4V$ , $C_L = 5pF$ |                                      |

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### 5.1.5 Section Conclusion

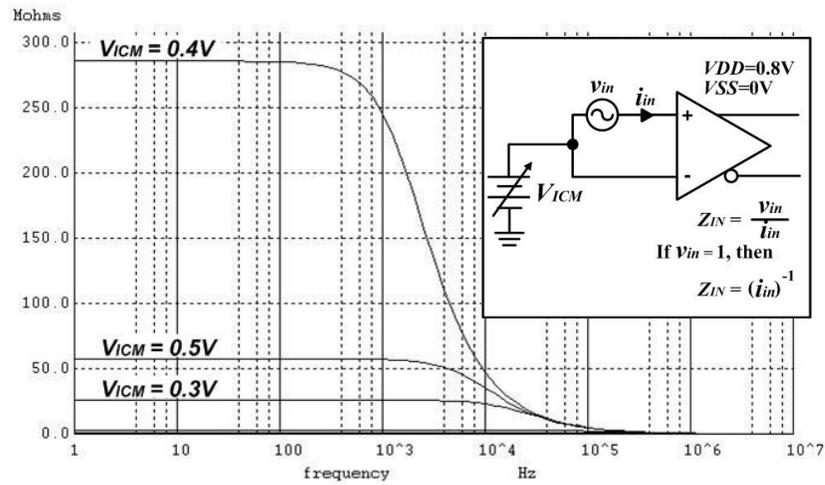
This paper explored the approach of low-voltage OTA design using the bulk-driven technique. The observed advantages are:

- As previously pointed out by [BLA98], BDDP can provide rail-to-rail ICMR operation, and bulk-driven current mirrors can be operated with less voltage headroom consumption.
- With the use of bulk- and gate-biased cascodes, the output resistance of a folded-cascode fully differential OTA can be increased with no additional circuit or extra power consumption.
- Bulk-driven CMFB can sense the input common-mode voltage smaller than the threshold voltage.

### ***5.2 Input Impedance of the Complementary BDDP***

Utilising the design work given in Section 5.1 as an opportunity, it is worth analysing the input impedance characteristics of the complementary BDDP stage utilised in the proposed OTA and compare with the differential pair design given in Chapter 3.

Figure 5-13 shows the simulated ac characteristics of the input impedance.



**Figure 5-13 Simulation results of the circuit-level input impedance characteristics of the proposed OTA utilising the complementary BDDP stage**

In comparison to Figure 3-8, it is apparent from Figure 5-13 that the input impedance of the BDDRB stage proposed in Section 3.1 is far better than the complementary BDDP. As can be observed from Figure 5-13, the input resistance maintains as high as 300M $\Omega$  for  $V_{ICM}$  around the mid-point of the supply voltage, but it considerably decreases to few-M $\Omega$  when  $V_{ICM}$  moves away by more than 200mV from the mid-point of the supply voltage. Therefore, in this aspect, it is evident that the BDDRB stage far advances.

### 5.3 Chapter Conclusion

Throughout the complete design of the proposed OTA, it was verified that the bulk-driven approach sees many advantages in low supply voltage analogue amplifier design. The BDDP and the BDCM can be applied not only at the core part of the amplifier but also at the CMFB block as well. Furthermore, it has been demonstrated that forward-biasing the bulk of cascode devices of the OTA helps enhancing the output resistance and hence the open-loop gain. Apparently, the bulk-driven

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approach is a strong candidate that makes the low-voltage CMOS analogue amplifier design realisable.

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## Chapter 6 The BSIM3 Simulation and the Measurement of the Input Capacitance of a Bulk-Driven Buffer

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So far this thesis has proposed several analogue CMOS design techniques using the bulk-driven approach, and for the verification the Berkeley Short-Channel Insulated-Gate Field Effect Transistor (IGFET) Model Version-3 (BSIM3), which is a widely used MOSFET model in the semiconductor industry [ALL02] [SED11], has been utilised in the SPICE simulations. However several works have been published recently that provide the comparison results of several popular MOSFET models with the measurement data of the fabricated bulk-driven devices, and report that Enz-Krummenacher-Vittoz (EKV) [ENZ95] is the most suitable MOSFET model for the nanometre bulk-driven applications [HE08] [WAN09] [WAN10].

The author finds the need for further extending this study for two reasons. Firstly, it may not always be the case that the fabrication services support EKV model for the available CMOS processes, and circuit designers may rather prefer to use the MOSFET model which the parameters have been already extracted by the fabrication services. Another reason is that circuit designers may need to size the length of the bulk-driven devices larger than the minimum, in particular in differential pair applications where good matching and reduced  $1/f$  noise are important [TER03]. The work reported in [HE08] [WAN09] [WAN10] all focuses on a bulk-driven device that is sized in a sub-micron channel length.

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To further extent the author was particularly keen to focus on the study of the input capacitance of a bulk-driven CMOS buffer, because throughout the author's experiences in presenting the research works at conferences the author noticed the audiences' high interests in the input capacitance of the proposals.

Taking into an account of the viewpoint mentioned above, this chapter reports the research work on the use of the BSIM3 MOSFET model for determining the input capacitance of a CMOS bulk-driven buffer. To validate the accuracy of the BSIM3 simulation, a bulk-driven CMOS buffer has been designed and fabricated with On-Semiconductor's 0.35 $\mu\text{m}$  CMOS process in order to obtain the measurement results for comparison.

This chapter is structured as follows. In Section 6.1, a bulk-driven CMOS buffer that has been designed and fabricated using On-Semiconductor's 0.35 $\mu\text{m}$  CMOS process is described. Section 6.2 demonstrates the postlayout simulation results using the BSIM3 MOSFET model. Section 6.3 describes the taken procedure for the input capacitance measurement, and examines the obtained results by comparing with the simulated results. Lastly, in Section 6.4, the concluding remarks are stated.

The supplementary information to this chapter is also listed in Appendix B and C. Appendix B lists the other prepared materials, such as the SPICE code used for the simulation, the IC layout of the whole die and the bonding diagram, more snapshots of the microphotograph, and the used test board for the measurement. Appendix C provides all the logs of the measurement results presented in Section 6.3.

## 6.1 Designing a Bulk-Driven CMOS Buffer for Fabrication

Figure 6-1 shows the circuit diagram of a bulk-driven CMOS buffer that has been designed for fabrication using On-Semiconductor's 0.35 $\mu\text{m}$  CMOS process, and Table 6-1 shows the size information for each devices.

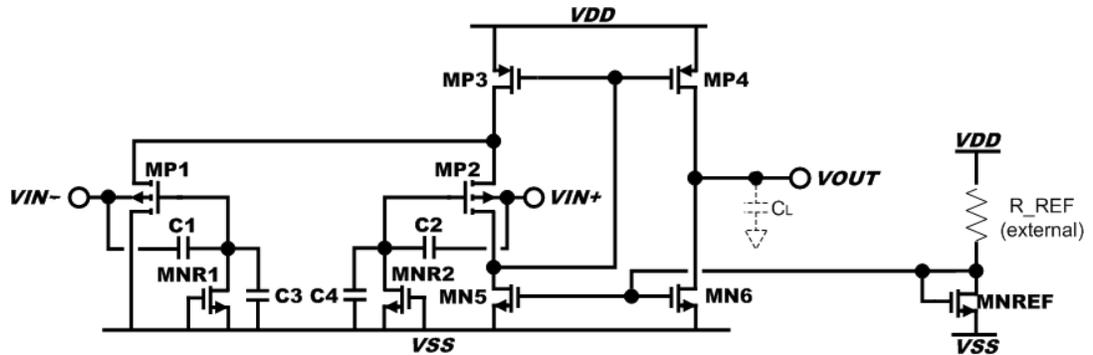


Figure 6-1 Circuit Diagram of the Bulk-Driven CMOS Buffer for Fabrication

Table 6-1 Device Dimensions for Figure 6-1

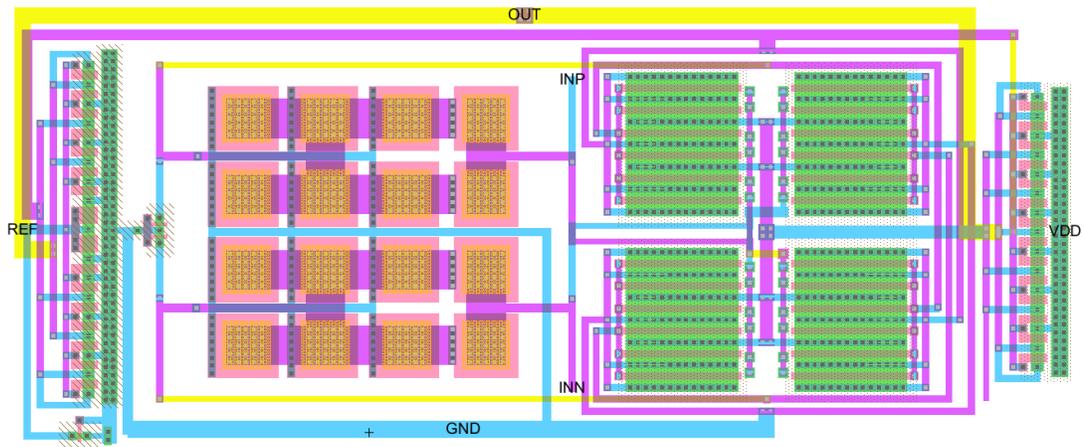
| Device Name     | Width             | Length            |
|-----------------|-------------------|-------------------|
| MP1, MP2        | 60 $\mu\text{m}$  | 1.4 $\mu\text{m}$ |
| MP3             | 20 $\mu\text{m}$  | 1.4 $\mu\text{m}$ |
| MP4             | 10 $\mu\text{m}$  | 1.4 $\mu\text{m}$ |
| MN5, MN6, MNREF | 10 $\mu\text{m}$  | 1.4 $\mu\text{m}$ |
| MNR1, MNR2      | 1.5 $\mu\text{m}$ | 0.7 $\mu\text{m}$ |
| R_REF           | 220K              |                   |
| C1, C2          | 0.2pF             |                   |
| C3, C4          | 0.8pF             |                   |

The operation principle of Figure 6-1, which is simply the bulk-driven version of the differential voltage amplifier that was proposed in [SAN98], is as follows. Since MP2 is biased with a constant DC current, the AC current generated by the differential voltage input flows from MP3 to MP1, which is mirrored by the current mirror MP3/MP4 to the output. The key feature of Figure 6-1 is that the AC current is not limited by any DC current, and furthermore only three transistors MP1/MP3/MP4 carry the AC current which is clearly an advantage for high-frequency low-power design [SAN06]. In addition, the Quasi-Floating Gate (QFG)

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technique [RAM04] has been applied at the gate of the input devices MP1 and MP2 instead of DC-biasing them with the negative supply rail  $V_{SS}$ . With the QFG technique, capacitive voltage dividers have also been implemented in order to avoid MNR1 and MNR2 to be reversely biased during the rail-to-rail operation.

The layout of the buffer circuit of Figure 6-1 has been generated using a freeware tool called Electric which is available for download from [ELE11] (and free video tutorials are available for view from [BAK11]). Figure 6-2 shows the layout design, which the overall size turned out to be  $199\mu\text{m} \times 84\mu\text{m}$ .



**Figure 6-2 Layout Design of the Bulk-Driven CMOS Buffer of Figure 6-1**

For the packaging, a DIL16 package, which consists of 16 pins and is the cheapest one available from the fabrication site, has been chosen. Also, since the mask cost of the chip remains the same for the chip area until  $2\text{mm}^2$ , two of the same buffers have been integrated in the same chip. Figure 6-3 shows the pin assignment of the integrated two buffers.

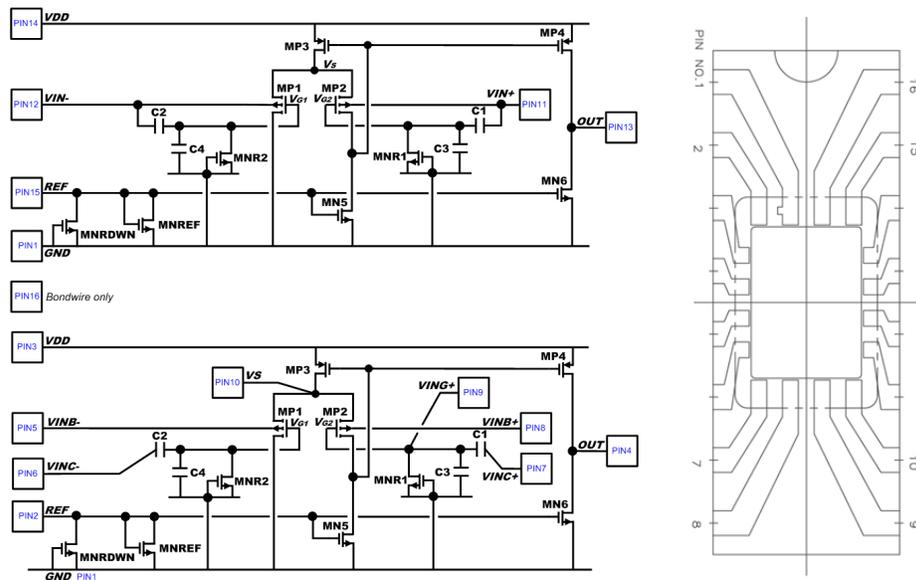


Figure 6-3 Pin Assignment

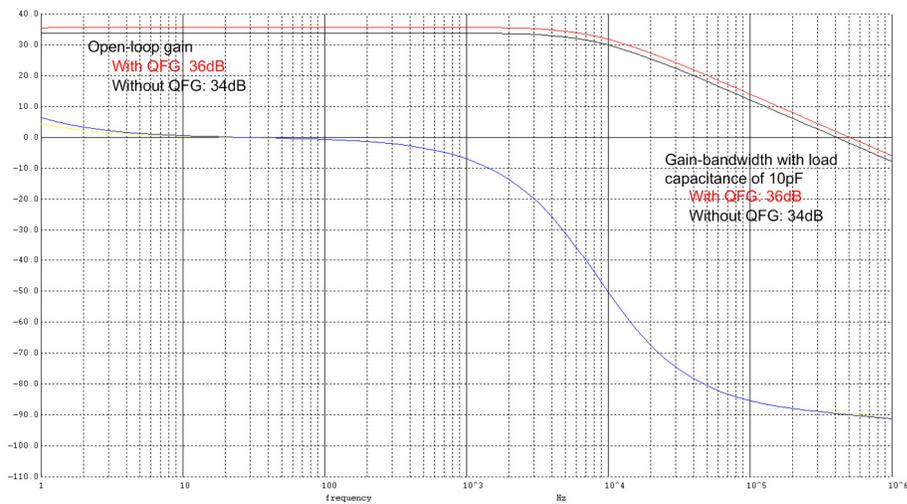
From Figure 6-3, please also remark that more pins have been assigned for the bottom buffer so that further measurements can be taken upon the need. Pin-5 is assigned at the coupled source of the differential pair so that  $V_{SB1,2}$  can be measured. Pin-9 is connected to the gate of MP2 so that the output waveform of the QFG block with the capacitive divider can be measured. Pin-6 and pin-7 are the input pins for the QFG block with the capacitive divider, which are intended to be shorted to pin-5 and pin-8 respectively, but upon the need these pins can be left open instead to verify the effectiveness of the QFG block. Pin16 is connected to only the pad so that the characteristics of the pad itself, such as its parasitic capacitance, can be measured if necessary.

The other prepared materials, such as the IC layout of the whole die and the bonding diagram, and the prepared test board, are listed in Appendix B.

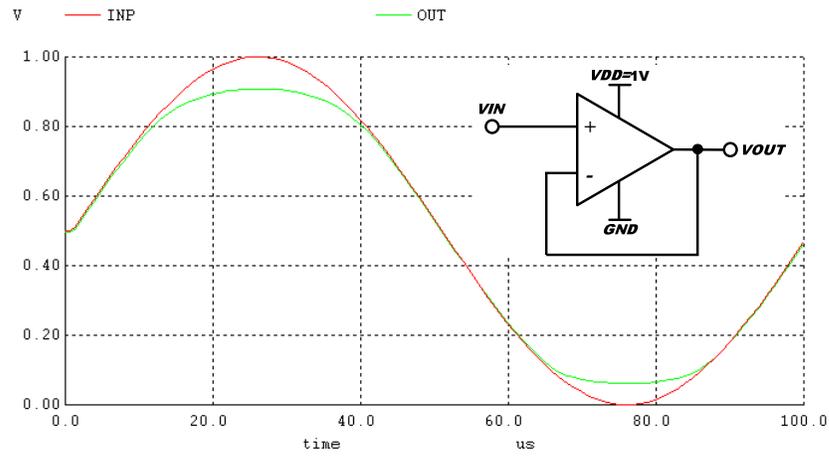
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## 6.2 Postlayout Simulation

Using the extracted postlayout netlist of Figure 6-2, the bulk-driven buffer has been simulated with a supply voltage of 1-volt. With R\_REF of 220K, the reference current that is flowing through MNREF becomes approximately 1 $\mu$ A and hence the overall DC current consumption of the buffer turns out to be approximately 4 $\mu$ A. Figure 6-4 and 6-5 show the BSIM3 simulation results of the open-loop frequency response with a load capacitance of 10pF, and the output waveform of the buffer in unity-gain configuration with a 1-volt peak-to-peak 10kHz sinusoidal input, respectively.



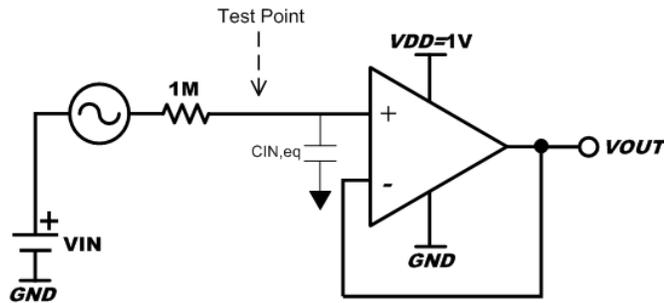
**Figure 6-4 Postlayout Simulation Results of the Frequency Response (VDD=1V, VSS=0V, CL=10pF)**



**Figure 6-5 Postlayout Simulation Result of the Output Waveform with a 1Vp-p 10kHz Sinusoidal Input**

*Procedure for Simulating the Input Capacitance*

The setup illustrated in Figure 6-6 shows the applied procedure for simulating the equivalent input capacitance  $C_{IN,eq}$ .



**Figure 6-6 The Setup for Simulating  $C_{IN,eq}$**

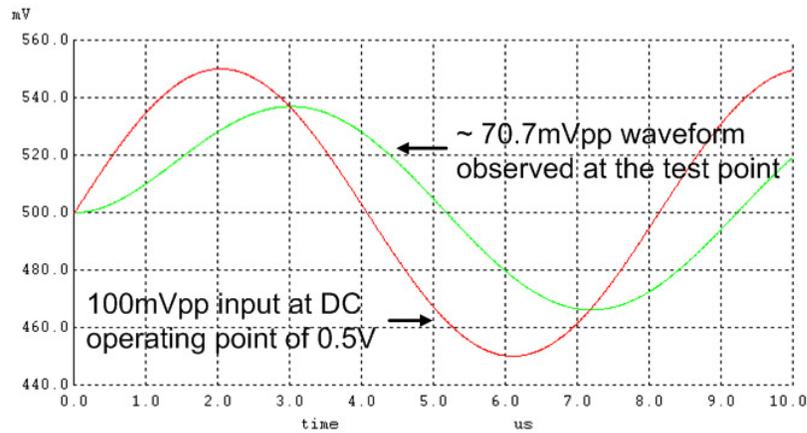
The  $1M\Omega$  resistor shown in Figure 6-6 leads to constructing a low-pass filter at the test point, with a cut-off frequency  $f_{-3dB}$  as expressed in Equation (6-1):

$$f_{-3dB} = \frac{1}{2\pi C_{IN,eq} (1M\Omega)} \quad (6-1)$$

Thus once  $f_{-3dB}$  is determined then  $C_{IN,eq}$  can be worked out by using Equation (6-2):

$$C_{IN,eq} = \frac{1}{2\pi f_{-3dB} (1M\Omega)} \quad (6-2)$$

From the theoretical observation expressed in Equation (6-2), the procedure for determining  $C_{IN,eq}$  has been defined. A 100mV peak-to-peak sinusoidal input is applied at the input of the filter, and the frequency is adjusted to the cut-off frequency  $f_{-3dB}$ , i.e. the magnitude of the waveform at the test point becomes at  $100mV \times (1/2)^{0.5}$  ( $\approx 70.7mV$ ) so that  $C_{IN,eq}$  can be calculated using Equation (6-2). Figure 6-7 shows the postlayout simulation results of the determined  $f_{-3dB}$  point, where the DC operation point of the input is 0.5V.



**Figure 6-7 Postlayout Simulation of Figure 6-6 with the Input DC Operating Point at 0.5V**

As discussed in Chapter 2, since the capacitance of the bulk of a MOSFET is bias-dependent of the DC operating point, the author decided to repeat Figure 6-7 with the DC operating point of the input  $V_{IN}$  from 0.1V to 0.9V in a 0.1V step. The SPICE code for performing this simulation is provided in Appendix B.

Figure 6-8 shows the determined  $C_{IN,eq}$  per operation point  $V_{IN}$ .

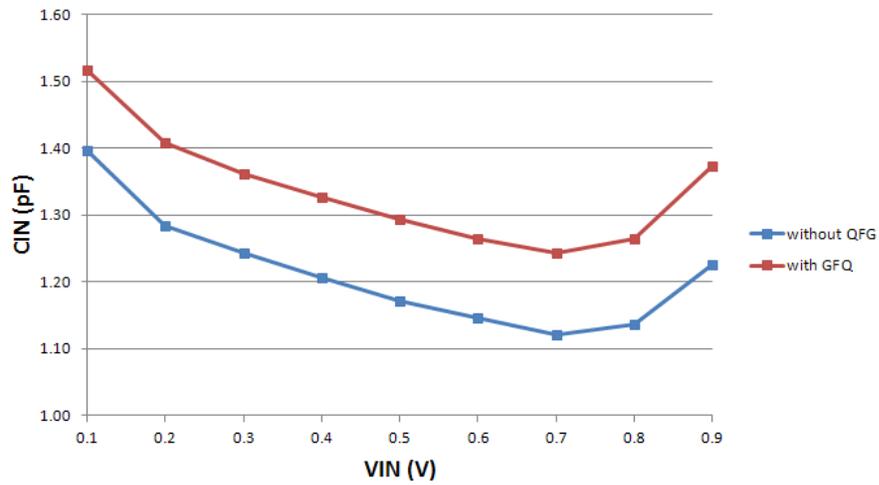


Figure 6-8 Postlayout Simulation Results of  $C_{IN,eq}$

### 6.3 Measuring the Input Capacitance of the Fabricated Bulk-Driven Buffer

The buffer presented in Section 6.1 has been fabricated. Figure 6-9 shows the microphotograph of the fabricate buffer.

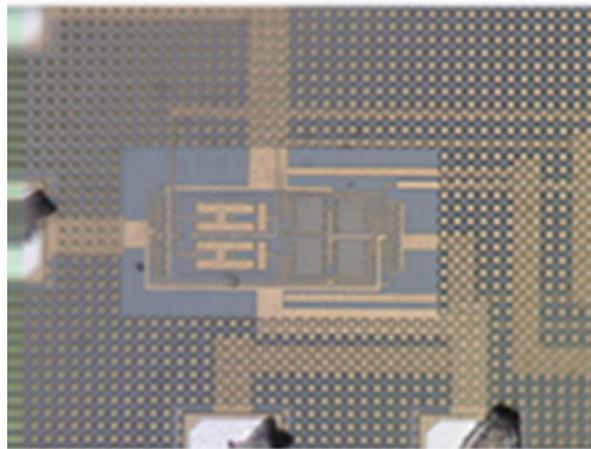
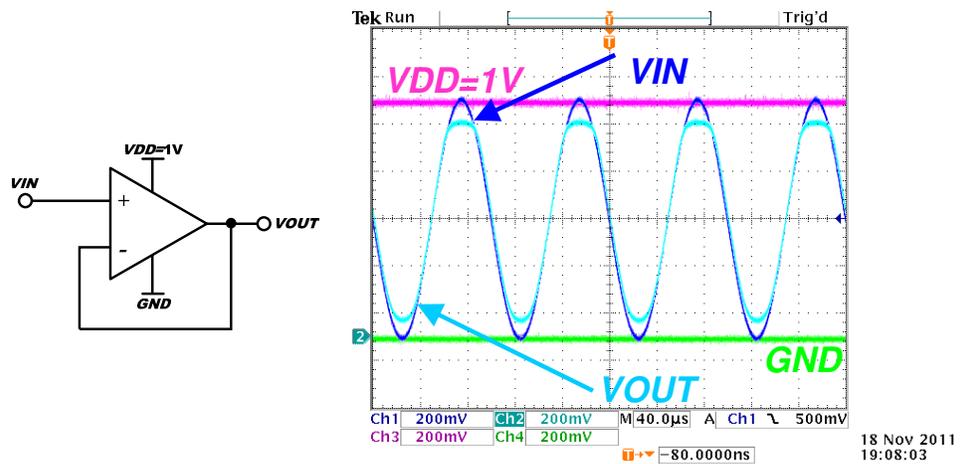


Figure 6-9 The microphotograph of the bulk-driven buffer presented in Section 6-1

In prior to assessing the input capacitance of the fabricated buffer shown in Figure 6-9, firstly the author verified that it is operational by configuring it in the same setup as described in Figure 6-5. Figure 6-10 shows the measurement result, which has become identical to the simulation result shown in Figure 6-5. Hence the fabricated buffer is ready to be tested for determining the input capacitance.



**Figure 6-10 The Measurement Result of the Output Waveform with a 1Vp-p 10kHz Sinusoidal Input**

### *Measurement Procedure*

This sub-section describes the applied procedure for measuring the input capacitance of the fabricated buffer, where the DC operating point of the input voltage  $V_{IN}$  is from 0.1V to 0.9V in a 0.1V step, i.e. the same setup as shown in the simulation in Section 6.2.

It was in fact originally planned to use a LCR meter Wayne Kerr 4300, which is capable to measure the capacitance in femto-Farad range. However when this measuring equipment was set up with the fabricated buffer, the measured value shown in the LCD display did not turn out to be stable. The tendency was that the measured value became less instable when the test applied signal has larger amplitude like 1Vp-p and faster frequency (the highest frequency Wayne Kerr 4300 can produce is 200kHz), however the measured value shown in the LCD display was still unstable and thus unreliable to take the log. On the other hand with a discrete capacitor that was randomly selected, the Wayne Kerr 4300 indicated the expected capacitance value in the LCD display. Thus the measuring equipment itself was not faulty at all, but simply unsuitable for use with the fabricated buffer, and

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consequently it was necessary to come up with an alternative procedure for determining the input capacitance of the fabricated buffer.

After searching through literatures the author came across with the work proposed in [NAT90], so called the phase measurement approach, which claims that only standard laboratory equipment is required for measuring small capacitances. To describe the proposed work of [NAT90] in brief, the phase lag between the output and the input sinusoidal signals of an RC low-pass filter can be expressed by:

$$\phi = \tan^{-1}(2\pi fRC) \quad (6-3)$$

where  $\phi$  is the phase difference between the output and the input sinusoidal signals of the RC low-pass filter,  $f$  is the frequency of the applied input sinusoidal signal, and R and C are the resistance and the capacitance of the RC low-pass filter. If R and  $f$  are known and  $\phi$  can be measured, then C can be worked out. In the work of [NAT90], the authors propose to adjust R and  $f$  such that  $\phi$  near  $45^\circ$  is achieved for accurate measurement.

Using the concept described by the work in [NAT90], the fabricated buffer was set up as shown in Figure 6-11 and  $f$  is adjusted such that the phase shift between the output and the input of the sinusoidal signal  $\phi$  became near  $45^\circ$ . Figure 6-12 shows the obtained measurement result.

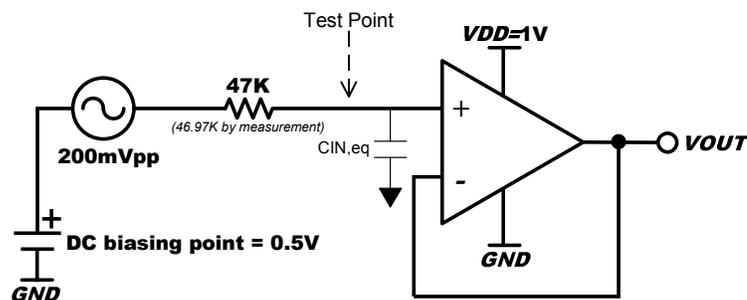


Figure 6-11 The Configured Setup for Determining the Input Capacitance of the Buffer

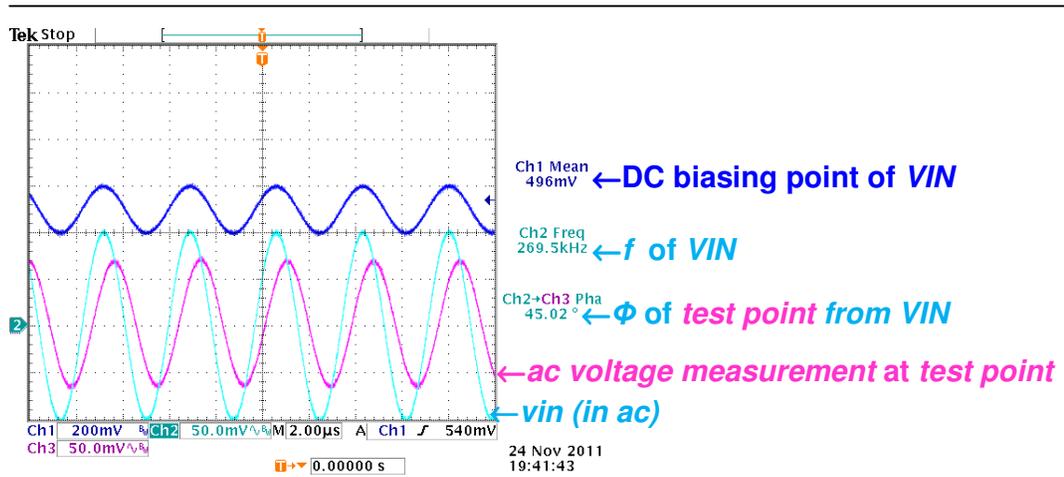


Figure 6-12 The Measurement Result of the Setup Shown in Figure 6-11

It is important to note, however, that the measurement result of Figure 6-12 also contains the parasitic elements (e.g. the parasitic of the used probe itself). To verify the overall parasitic element  $C_{\text{stray}}$ , the pin that is bond-wired to the PADONLY, as shown in Figure 6-12, has been probed and the same procedure has been taken for the measurement, so that in the end the capacitance of the interest, i.e. the input capacitance of the fabricated buffer  $C_{\text{IN,eq}}$ , can be extracted by calculation.

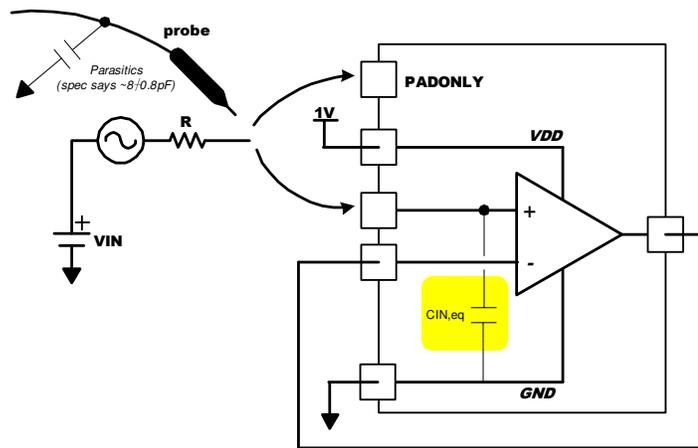


Figure 6-12 Measurement Procedure for Extracting  $C_{\text{IN,eq}}$

For the R selection in Figure 6-12, various resistance values has been tried out to observe the effect in the overall result. Also, the amplitude of the input sinusoidal signal has been tried with 100mVpp and 200mVpp to see if it can additionally affect the measurement result. Table 6-2 shows the summary of the measurement results.

**Table 6-2 Measurement Results of Figure 6-12 with Various Resistance Values and the Amplitudes of the Test Signal**

| <b>Tested condition</b>   | <b>Measurement Results</b>   | <b>Extracted <math>C_{IN,eq}</math><br/>(=<math>C_{total} - C_{stray}</math>)</b> |
|---|--|---|
| R=4k7 with<br>200mVpp   | $C_{total} = 11.71 \pm 0.15$ pF<br>$C_{stray} = 11.20 \pm 0.11$ pF | $C_{IN,eq} = 0.52 \pm 0.26$ pF  |
| R=4k7 with<br>100mVpp   | $C_{total} = 11.75 \pm 0.13$ pF<br>$C_{stray} = 11.17 \pm 0.13$ pF | $C_{IN,eq} = 0.58 \pm 0.26$ pF  |
| R=47k with<br>200mVpp   | $C_{total} = 12.53 \pm 0.23$ pF<br>$C_{stray} = 11.47 \pm 0.12$ pF | $C_{IN,eq} = 1.06 \pm 0.35$ pF  |
| R=470k with<br>200mVpp  | $C_{total} = 11.68 \pm 0.38$ pF<br>$C_{stray} = 11.16 \pm 0.24$ pF | $C_{IN,eq} = 0.52 \pm 0.62$ pF  |
| Other conditions:<br>1. The DC bias of the input voltage was set to 0.5V<br>2. The QFG block was unconnected in the buffer<br>3. The fabricated buffer has been measured for 20 times to compute the average and the standard deviation values. |  |   |

As can be seen from Table 6-2 the extracted result of  $C_{IN,eq}$  is dependent to the measurement condition, which the author initially could not understand the reason behind. However, by taking a closer look at the setup, as shown in Figure 6-13, few reasons can be explained.

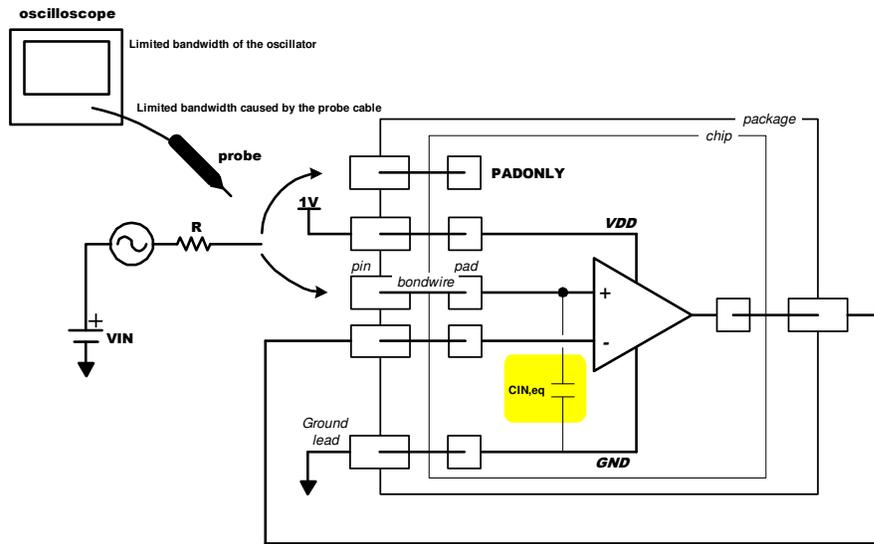


Figure 6-13 A Closer Look of the Set Up Shown in Figure 6-12

For  $R=4K7$   $f$  needed to be as fast as 3MHz in order to achieve  $\phi$  near  $45^\circ$ , but faster frequency introduces some side effects that may ruin the measurement results. One side effect is that the inductive elements within the measurement setup (e.g. the bond wires within the package and the ground lead) would appear in the measurement result as  $f$  increases. One other side effect that would appear with faster frequency of the input signal is due to the performance limit of the measuring equipment. For instance, as  $f$  increases the input impedance of the probe dominates the loading effect, and the bandwidth limit of the probe and the oscilloscope may cause inaccuracy in the amplitude measurement of the signals [TEK\_1], [TEK\_2], [TEK\_3]. Thus in order to reduce these possible side effects as minimal as possible, slower  $f$  (which consequently means the increased resistance of  $R$ ) needs to be applied for accurate measurement.

However in contradict to the observation mentioned above, when  $R=470K$  and the adjusted  $f$  that achieves  $\phi$  near  $45^\circ$  reduces to around 30kHz, the signal strength becomes weak and the noise disturbs the measurement. The results deviate more with

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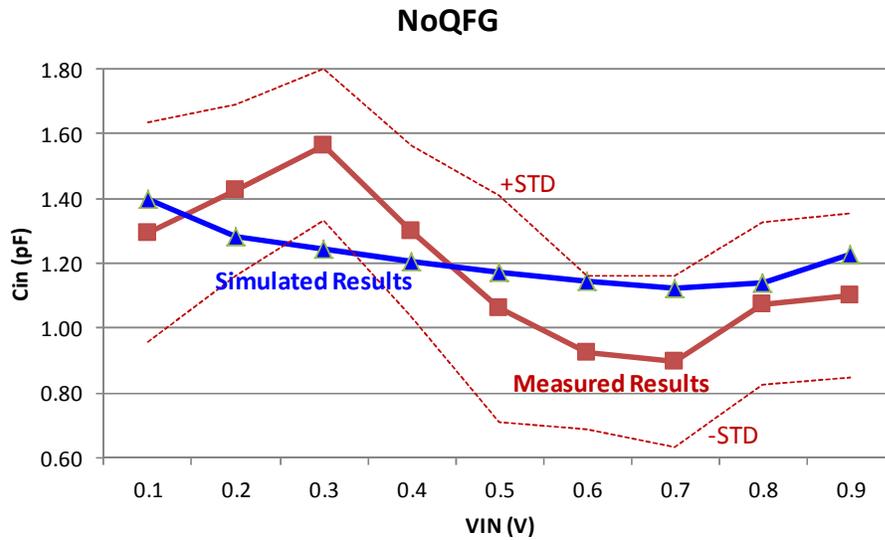
slower  $f$ . To obtain reliable measurement results,  $f$  needs to be faster than 30kHz to overcome the noise disturbance.

Concerning the amplitude of the input signal, 200mVpp was the maximum that can be set in this measurement as the objective was to measure the input capacitance of the fabricated buffer with the bias voltage of the input from 0.1V to 0.9V in a 100mV step. Under this measurement objective, a voltage amplitude of the input signal greater than 200mVpp would exceed the supply voltage rails of the buffer operating at 1V power supply. In order to justify that the amplitude of 200mVpp is large enough to extract  $C_{IN,eq}$ , another measurement has been carried out with the amplitude of 100mVpp to observe the effect. The result turned out the difference of only 0.06pF was obtained in the extracted  $C_{IN,eq}$ . Thus the amplitude of 200mVpp was judged as sufficiently large to carry on the experiment.

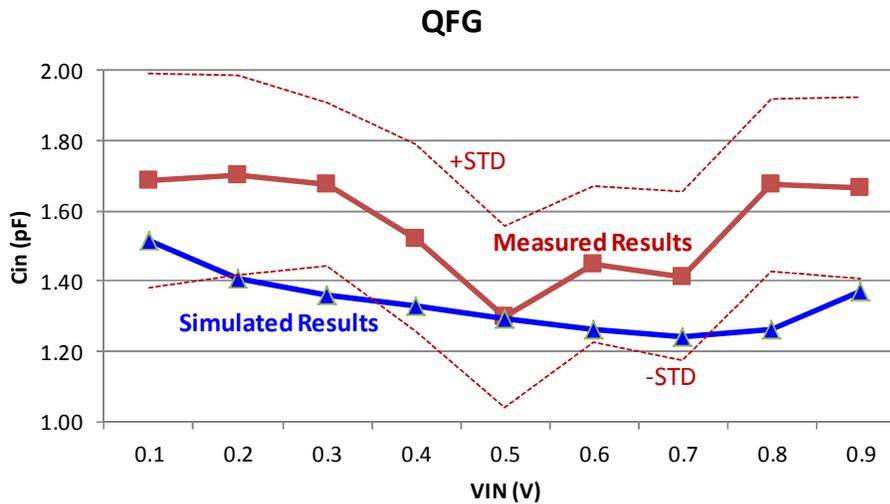
Considering all aspects mentioned above and carrying out further experiments with different setup of R, it appeared that R=47K with the amplitude of the input signal of 200mVpp gave a good compromise between the side effects of the fast signal input and the noise disturbance, and hence the author decided to continue the measurement under this setup.

### *Measurement Results and Observations*

Base on the decision made for the measurement procedure as described above, the experiment was carried out to determine  $C_{IN,eq}$  at different bias voltages  $V_{IN}$ . Figure 6-14 shows the measurement results of  $C_{IN,eq}$  with  $V_{IN}$  varying from 0.1V to 0.9V in a 100mV step, and the comparison to the simulation results.



(a) the buffer without the QFG block



(b) the buffer with the QFG block

**Figure 6-14** The Measurement Results of  $C_{IN,eq}$  (20 measurements were taken to compute the average and the standard deviation) with  $V_{IN}$  varying from 0.1V to 0.9V in a 100mV step and the Comparison to the Simulation Results

The measurement has been taken for 20 times per each  $V_{IN}$  biasing point. In comparison to the simulation results, in average the measured  $C_{IN,eq}$  differs by 16.9% (the maximum difference of 0.41pF at  $V_{IN} = 0.8V$ ) and 12.9% (the maximum difference of 0.32pF at  $V_{IN} = 0.3V$ ) for the buffer with and without the QFG block, respectively. The average deviation turned out to be 16.5 % (the maximum deviation

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of  $\pm 0.30\text{pF}$  at  $V_{IN} = 0.1\text{V}$ ) and 23.8% (the maximum deviation of  $\pm 0.35\text{pF}$  at  $V_{IN} = 0.5\text{V}$ ) for the buffer with and without the QFG block, respectively. Taking into account that the measurement of target is only in a few pico-Farad range, these deviation values are considerably small. The phase measurement approach proposed by [NAT90] works well in extracting  $C_{IN,eq}$  of the fabricated bulk-driven buffer.

In overall, when  $V_{IN}$  is varied the measured  $C_{IN,eq}$  changes more rapidly whereas the simulated  $C_{IN,eq}$  looks more flat. The measured and the simulated results may appear to be different to each other, however considering that the measurement imperfections are also introduced by the noise disturbances, it is hard to predict how accurately the BSIM3 model performs in the simulation. Instead what can be stated from this experiment is that the BSIM3 model in the postlayout simulation gives a reasonable prediction of the  $C_{IN,eq}$  of a bulk-driven buffer, within  $\pm 0.4\text{pF}$  of imprecision.

## ***6.4 Chapter Conclusion***

This chapter presented the study of the BSIM3 model used in the postlayout simulation of a bulk-driven buffer for determining  $C_{IN,eq}$ . For the verification the fabricated device was prepared and the phase measurement approach [NAT90] was investigated in details for extracting  $C_{IN,eq}$ . The obtained measurement and the simulation results of  $C_{IN,eq}$  are relatively matched over various  $V_{IN}$  operating point. The BSIM3 model used in the postlayout simulation is a useful verification technique in predicting  $C_{IN,eq}$  of a bulk-driven buffer.

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## Chapter 7      Conclusions

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This Chapter summarises the achievements of this research work and provides the author's recommendations for further work relating to the bulk-driven approach.

### *7.1 Summary*

The author's research objective as stated in Chapter 1 was to develop new circuit design techniques using the bulk-driven approach that can overcome many of the drawbacks which have been previously reported, and furthermore to invent new application areas of the bulk-driven approach where it can lead to performance enhancement in the field of CMOS analogue amplifier design. After reviewing the characteristics of a bulk-driven device in Chapter 2, where the key advantage is the depletion (JFET-like) characteristics whereas many of the associated drawbacks are related to small-signal behaviours and reliability, the following proposals have been made:

#### *BDDP*

In Chapter 3, two BDDP circuit blocks called the BDDRB and BDFVDP have been proposed. The BDDRB input stage uses the RBS to achieve constant small-signal behaviour hence to solve the non-linearity issue, and furthermore to diminish the latch-up issue by having the constant bias voltage. On the other hand, with the BDFVDP solves the issues of degraded input impedance characteristics and the latch-up by adding the reverse-bias connected diodes at the bulk-driven input. For both BDDRB and BDFVDP, the hardware implementation is simple.

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### *Bulk-Driven Source Follower*

Chapter 4 proposed the new application area of the bulk-driven approach, which is the design of source follower blocks. Like FVF and SSF, the proposed BDFVF and BDSSF blocks achieve low-power high-speed performances but with an additional feature such that the DC level shift can be eliminated and even programmable to the level that is less than the threshold voltage of a MOSFET. An application example of the level-shifted BDSSF in a simple current mirror was also given, which demonstrated the behaviour with the reduced voltage headroom consumption at the input device of the current mirror but without introducing an additional DC offset current.

### *Bulk-Driven Cascodes*

Chapter 5 proposed another new application area of the bulk-driven approach, which is seen at the cascode output stage of op-amps, for instance folded-cascode OTAs. For any op-amps having a cascode at the output stage to increase the output resistance, then forward-biasing the bulk of the cascode device can further enhance the output resistance and hence the open-loop gain, which helps to cover the disadvantage of low  $g_{mb}$  of the BDDP but without introducing an additional hardware in the core part of the op-amps. Based on utilising BDDP and forward-biased cascode devices, a design methodology of a fully differential rail-to-rail OTA that can be operated with a power supply voltage of 0.8-volt using a 0.35 $\mu\text{m}$  twin-well CMOS technology having a threshold voltage of 0.6-volt is demonstrated, and the verification results indicated that the open-loop gain of over 60dB is achieved.

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*Verification of the BSIM3 model for Determining the Input Capacitance of a Bulk-Driven Buffer*

Chapter 6 presented the study of the BSIM3 model used in the postlayout simulation of a bulk-driven buffer for determining the input capacitance. For the verification the phase measurement approach was applied for extracting the input capacitance of the fabricated buffer. The comparison between the measurement and the simulation results demonstrated that the BSIM3 model used in the postlayout simulation is a useful verification technique for predicting the input capacitance of a bulk-driven buffer.

In summary the bulk-driven approach may have an unfavourable impression due to too many associated problems, however the work reported in this thesis proves that that is false. Circuit design techniques like demonstrated in this thesis can overcome many of those drawbacks, and moreover new application areas can be identified and proposed by utilising the bulk-driven approach. The author's work has certainly made a progress in proving that this circuit design approach has a high potential in enhancing performances in the analogue amplifier design field, and it is encouraging to carry on the research to confront the difficulties of the low-voltage roadmap the ITRS is defining.

## ***7.2 Recommendations for Further Work***

After completing this work, the author would like to make the following recommendations:

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### *Other New Application Areas*

The author's work identified two new areas where the bulk-driven approach can be applied, in source followers and cascodes, however there have to be even more. In fact the author is currently aware of the following circuit blocks where the bulk-driven approach has been applied:

- Auxiliary amplifier for regulated cascode application [ZAB07], [MON09]
- Current conveyer [KHA06], [KHA11B]
- Mixer [HSI10], [SCH08], [VOR08]
- Phase Lock Loop [LUN09]
- Voltage Squarer [RAI10B]
- Variable Gain Amplifier [RAI10A]

Furthermore, the improved version of the bulk-driven current mirror, which was originally proposed in [BLA95], is recently proposed in [LAK11]. It is evident that the bulk-driven approach as a research topic is increasingly popular. The author recommends looking into other new application areas using the bulk-driven approach and/or developing the improved versions of the above circuit blocks.

### *Looking into other unsolved problems*

The author's work reported in this thesis leads to solving many of the associated drawbacks of the bulk-driven approach but few others still remain, in particular the low  $g_{mb}$  issue. The cascode approach presented in Chapter 5 enhances the output resistance and so does the open-loop gain of the OTA, however the low  $g_{mb}$  issue has not been addressed and hence the low-speed high-noise issues remain. From literature search, the research effort is seen by means of partial positive feedback technique. The work in [CAR05] is applying the partial positive feedback at the active load, whereas the work in [RAI10C] is applying the partial positive feedback

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at the input differential pair devices. The author fully agrees that the partial positive feedback technique is an excellent solution to avoid the speed reduction, but not the ultimate from the viewpoint that the issues of non-constant  $g_{mb}$  and the degraded input impedance characteristics remain unsolved. One last remark after completing this work and reviewing recent publications is that the author strongly believes the next research effort should be to develop a new circuit design technique that can combine the advantages of the gate and the bulk of a MOSFET.

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## Appendix A Published Works

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The author's publications listed below are provided in this appendix.

- [HAG05] Y. Haga, H. Zare-Hoseini, L. Berkovi, and I. Kale, "Design of a 0.8 Volt Fully Differential CMOS OTA Using the Bulk-Driven Technique", *IEEE Proc. International Symposium in Circuits and Systems*, 2005, pp. 220 – 223
- [HAG06] Y. Haga, R. C. S. Morling, and I. Kale, "A New Bulk-Driven Input Stage Design for sub 1-volt CMOS Op-Amps", *IEEE Proc. International Symposium in Circuits and Systems*, 2006, pp.1547 – 1550
- [HAG09A] Y. Haga and I. Kale, "Bulk-Driven Flipped Voltage Follower", *IEEE Proc. International Symposium in Circuits and Systems*, 2009, pp.2717 – 2720
- [HAG09B] Y. Haga and I. Kale, "CMOS Buffer Using Complementary Pair of Bulk-Driven Super Source Followers", *IEEE Electronic Letters*, Vol. 45, Issue 18, 2009, pp. 917 – 918
- [HAG09C] Y. Haga and I. Kale, "Class-AB Rail-to-Rail CMOS Buffer with Bulk-Driven Super Source Followers", *IEEE European Conference on Circuit Theory and Design*, 2009, pp. 695 – 698
- [HAG10] Y. Haga and I. Kale, "Bulk-Driven Flipped Differential Pair", *IEEE Proc. PhD Research in Microelectronics and Electronics*, 2010
- [HAG11] Y. Haga and I. Kale, "Bulk-Driven DC Level Shifter", *IEEE Proc. International Symposium in Circuits and Systems*, 2011, pp.2039-2042

# Design of a 0.8 Volt Fully Differential CMOS OTA Using the Bulk-Driven Technique

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**Abstract**— This paper explores and presents the possible approaches to the design of low-voltage Operational Transconductance Amplifier (OTA) using the bulk-driven technique. The design of a 0.8 volt fully differential folded-cascode OTA using a 0.35 $\mu\text{m}$  CMOS technology having a threshold voltage of 0.6 volt is presented. This OTA utilizes bulk-driven differential-pairs to achieve rail-to-rail input operation, and gate- and bulk-biased cascode transistors to increase the output resistance. A continuous-time Common-Mode FeedBack (CMFB) is used for this OTA, which implements the bulk-driven differential pairs to sense the common-mode voltage smaller than the transistor's threshold voltage, as well as bulk-driven current mirrors to reduce voltage headroom consumption. This OTA has been designed using Alcatel's 0.35 $\mu\text{m}$  twin-well CMOS technology, and the simulation results indicate an open-loop gain > 60dB, unity gain-bandwidth = 3.4MHz with a 5pF load, and an Input Common Mode Range (ICMR) of 0.8V.

## I. INTRODUCTION

The need of power supply voltage reduction in integrated circuits is driven by several factors: (1) the reduction in the minimum dimensions in CMOS technologies necessitating reduced power supply voltages, and (2) low supply voltages are in favor of reducing power consumption, weight and volume of the battery in portable electronics [1]. The main blocks of analog circuits such as the op-amps require a supply voltage of at least the sum of the magnitude of the nMOS and pMOS transistor's threshold voltages [3]. However, the threshold voltages do not decrease much below what is available today because of the digital logic [2], causing difficulty in designing analog circuits with low supply voltages on a standard CMOS technology. Consequently, novel circuit techniques are required to overcome this conflict.

The bulk-driven technique is a strong candidate for op-amp design under the constraints introduced by low-voltage operation. This paper firstly provides a brief review of the bulk-driven technique. It then follows by presenting a fully-differential Operational Transconductance Amplifier (OTA)

design which operates at 0.8 volt power supply using a 0.35 $\mu\text{m}$  CMOS technology where the threshold voltage of the MOS transistor is 0.6 volt.

## II. BRIEF REVIEW OF THE BULK-DRIVEN TECHNIQUE

When using a single MOS transistor as an amplifier, the input signal is usually fed into the gate (or sometimes the source) terminal and the bulk-terminal is tied to a fixed bias voltage (usually the supply-rail), as shown in Fig 1(a). In this configuration, named gate-driven MOS transistor throughout this paper, the gate-to-source voltage controls the drain current of the transistor. For a bulk-driven MOS transistor, on the other hand, its gate is tied to a fixed bias voltage (e.g. the supply-rail) and the input signal is fed into the bulk, as shown in Fig. 1(b). In this configuration, the threshold voltage of the transistor, which is a function of the bulk-to-source voltage, controls the drain current. The operational characteristics of the bulk-driven and gate-driven MOS transistors are illustrated in Fig. 2.

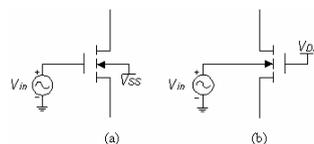


Figure 1. (a) Conventional gate-driven nMOS and (b) bulk-driven nMOS

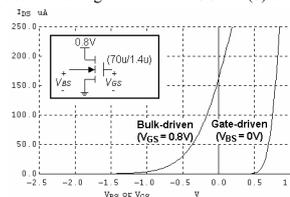


Figure 2. Simulating transconductance characteristics of gate-driven and bulk-driven nMOS transistors [3] using a 0.35 $\mu\text{m}$  CMOS Process

As shown in Fig. 2, to operate the gate-driven MOS transistor in the active region, the gate-to-source voltage

needs to be greater than the threshold voltage (which is approximately 0.6 volts in this case). On the other hand, the bulk-driven MOS transistor behaves in a similar fashion to a depletion MOS transistor or a Junction Field Effect Transistor (JFET). Therefore, with the zero-bias voltage at the input node, the transistor is still in the active region. This is the key characteristic of a bulk-driven MOS transistor we use in designing low-supply voltage op-amps and other analog circuits. The two fundamental advantages of using the bulk-driven devices are:

- Bulk-driven differential pairs in op-amps significantly improve the Input Common-Mode Range (ICMR) since a bulk-driven device allows an extension in its input range on the negative side, as illustrated in Fig. 2. With proper design of the bulk-driven differential pair, the devices can remain saturated over the entire rail-to-rail ICMR.
- Bulk-driven current mirrors, as shown in Fig. 3(a), can eliminate the large voltage drop across the input device. This is because the voltage drop across the input device  $V_{DS}$ , which is equal to the bulk-to-source voltage  $V_{BS}$ , does not need to be greater than the threshold voltage  $V_{T0}$  for proper operation. The cascode configuration, as shown in Fig. 3(b), can be used to improve current matching and increase the finite output impedance of the current mirror. In this configuration, the voltage drop across the input devices still remains below the threshold voltage.

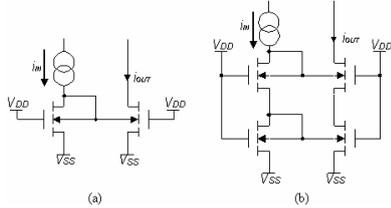


Figure 3. Bulk-driven current mirror (a) simple (b) cascode

However, there are several disadvantages of bulk-driven MOS transistors, which are all described in detail in [3]. The two fundamental ones are:

- As shown in Fig. 2, the transconductance of the bulk-driven MOS transistor  $g_{mb}$  is less than the transconductance of the conventional gate-driven MOS transistor  $g_m$ . ( $g_m$  and  $g_{mb}$  are the slopes of its drain current versus its input voltage at the bias point). Therefore utilizing a bulk-driven differential pair for op-amp design introduces a challenge in achieving high open-loop gain. Equation (1) is the level-1 model expression for  $g_{mb}/g_m$  ratio,  $\eta$ , which is typically 0.2 to 0.4, dependent on the Common-Mode Level (CML) of the input:

$$\eta = g_{mb}/g_m = (\gamma/2)(2|\Phi_F| - V_{BS})^{-0.5} \quad (1)$$

- The polarity of the bulk-driven MOS transistor is process related as wells are required to isolate the bulk-terminals. For a standard digital CMOS technology (i.e. n-well process), only pMOS can be bulk-driven. If both polarities need to be bulk-driven, then a twin-well technology is required.

### III. STATE-OF-THE-ART AND DESIGN OBJECTIVE

The op-amp design presented in [3] is a single-ended amplifier, which operates at 1-volt power supply using a standard digital CMOS technology with a threshold voltage of 0.8 volts. Their achieved open-loop gain is 48.8dB with a unity-gain bandwidth of 1.3MHz at 22pF load.

The op-amp design presented in [4] is a 0.8 volt fully differential OTA using a twin-well CMOS technology, and it utilizes a gain-boosting technique to increase the open-loop gain to 68dB with a unity-gain bandwidth of 93.3MHz with no load condition.

This paper reports on and demonstrates an alternative approach of increasing the open-loop gain of a fully differential folded-cascode OTA without the use of additional circuit or extra power consumption. In the next section, the design of 0.8 volt 60dB fully differential OTA is presented using a 0.35 $\mu$ m CMOS twin-well technology having a threshold voltage of 0.6 volts.

### IV. PROPOSED SCHEMATICS

#### A. OTA

A one stage folded-cascode OTA using bulk-driven differential pairs at the input stage, which is illustrated in Fig. 4, was chosen for the low power-supply voltage amplifier.

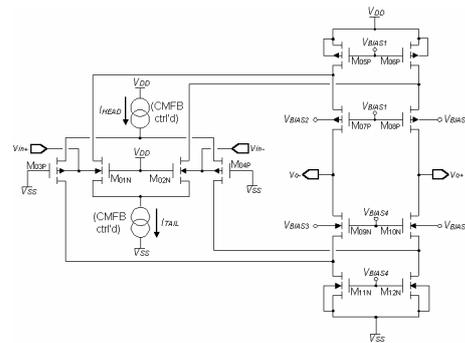


Figure 4. Proposed core OTA

- *Complementary Bulk-Driven Differential Pair*

As mentioned in section II, the depletion characteristics of an nMOS transistor allow the ICMR to extend below the negative power supply. The transconductance of an nMOS transistor, however, increases by increasing the ICMR [3].

This effect can be illustrated by simulating the transconductance of an nMOS transistor with the set-up shown in Fig. 5(a). The results of the simulation are shown in Fig. 6. The variance of the input transconductance causes the op-amp open-loop gain and also the phase margin to vary with ICMR. For a pMOS transistor with the setup illustrated in Fig. 5(b), the complementary characteristics can be observed as illustrated in Fig. 6.

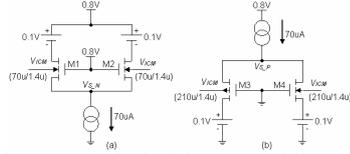


Figure 5. Set up for simulating (a)  $g_{mb1}$  and (b)  $g_{mb3}$

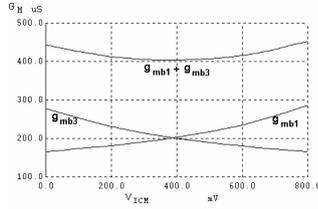


Figure 6. Simulation plots of  $g_{mb1}$  and  $g_{mb3}$

In order to reduce the variance of the input transconductance, complementary differential pairs can be utilized [5], as the results demonstrate in Fig. 6. The overall transconductance variation, which is the sum of the transconductance of the nMOS and pMOS transistors, is improved by approximately 50%. To achieve a transconductance with minimum variations, a proper W/L ratio for the nMOS and pMOS transistors should be carefully selected.

- *Cascode Devices*

As can be realized from (1), the transconductance of a bulk-driven differential pair is less than that of a gate-driven differential pair, causing a challenge in achieving high open-loop gain for the amplifier. One possible method to increase the open-loop gain is to increase the output resistance. The output resistance of the core OTA in Fig. 4 can be approximated to:

$$R_{out} \approx (g_{m7} + g_{mb7})r_{o7}(r_{o5} // r_{o1}) / ((g_{m9} + g_{mb9})r_{o9}(r_{o11} // r_{o3})) \quad (2)$$

From (1) it can be realized that  $g_{mb7}$  and  $g_{mb9}$  can be increased as the bulks are slightly forward-biased. Therefore if a twin-well process is available, the bulks of cascode transistors could be slightly forward-biased. As an numerical example, for the term  $(g_m + g_{mb})$ , which equals to  $(1 + \eta)g_m$ , the  $\eta$  can be increased by approximately 0.04 when  $V_{BS}$  of the nMOS and pMOS cascode transistors are

increased from -0.1V to 0.2V in a 0.35 $\mu$ m CMOS technology.

### B. Common-Mode Feedback

To stabilize the CML of the two outputs to be midway between the power-supply voltages the Common-Mode FeedBack (CMFB) is required. Fig. 7 illustrates typical circuit diagrams of continuous-time CMFB circuits [2], [7].

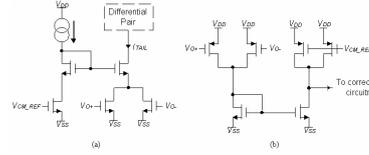


Figure 7. Typical CMFB circuit (a) current output and (b) voltage output

The problem of using the CMFB circuit shown in Fig. 7 in a low-supply-voltage environment is that the reference input  $V_{CM\_REF}$  and the output CML of the OTA have to be greater than the threshold voltage for the circuit to operate in the active region. To overcome this problem, bulk-driven devices can be utilized. The proposed CMFB circuit is illustrated in Fig.8.

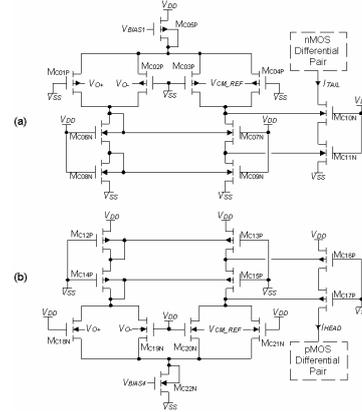


Figure 8. Proposed (a) nMOS driven CMFB and (b) pMOS driven CMFB

These proposed CMFB circuits are simply the same as Fig. 7(b) with the bulk-driven differential pairs and current mirrors included.  $M_{C05P}$  and  $M_{C22N}$  are added extra to improve the input range of operation, which is the output range of the core OTA. Simulation results of this proposal are shown in Fig. 9.

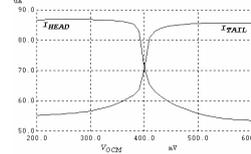


Figure 9. Verification of the proposed CMFB circuit

The simulation results shown in Fig. 9 imply that the bulk-driven technique can also be a strong candidate for low-voltage CMFB design.

### C. Supply-Independent Bias Circuit

The supply independent bias circuit presented in [6], as shown in Fig. 10(a), can be operated at a minimum supply voltage of  $V_{TO}+2V_{DSsat}$ . This is very suitable for low-voltage systems and therefore applied for generating  $V_{BIAS1}$  and  $V_{BIAS4}$ . For generating  $V_{BIAS2}$  and  $V_{BIAS3}$ , which have to be less than  $V_{TO}$ , bulk-driven devices can be utilized as shown in Fig. 10(b).

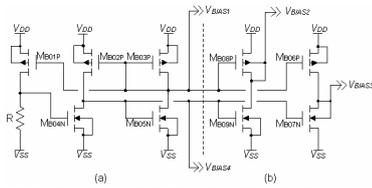


Figure 10. (a) Using the supply-independent bias circuit presented in [6] for generating  $V_{BIAS1}$  and  $V_{BIAS4}$  and (b) bias voltage generator for  $V_{BIAS2}$  and  $V_{BIAS3}$

Simulation results of Fig. 10 are illustrated in Fig. 11.

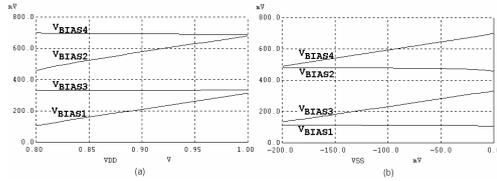


Figure 11. Effects of bias voltages with respect to (a) VDD and (b) VSS

As expected and seen in Fig.11,  $V_{BIAS1}$  and  $V_{BIAS2}$  are independent of  $V_{SS}$  and therefore suitable for biasing pMOS devices. Similarly,  $V_{BIAS3}$  and  $V_{BIAS4}$  are independent of  $V_{DD}$  and therefore suitable for biasing nMOS devices.

### D. Simulation Results

Alcatel's 0.35 $\mu$ m CMOS twin-well technology was used to verify the proposal. The open-loop gain and the phase margin of the OTA with a load capacitance of 5pF is depicted in Fig. 12. The overall OTA characteristic is shown in Table I.

### CONCLUSION

This paper explored the approach of low-voltage OTA design using the bulk-driven technique. The observed advantages are:

- As previously pointed out by [3], bulk-driven differential-pairs can provide rail-to-rail ICMR operation, and bulk-driven current mirrors can

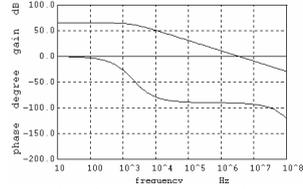


Figure 12. Plots of open-loop gain and phase margin

TABLE I. SUMMARY OF OTA PERFORMANCE

| Characteristics                   | Simulated Value                      |
|-----------------------------------|--------------------------------------|
| Open-loop DC gain                 | 66dB                                 |
| Unity gain-bandwidth              | 3.4MHz                               |
| Total current consumption         | 243 $\mu$ A                          |
| Phase margin                      | >80°                                 |
| Differential output voltage swing | 1V                                   |
| Slew rate                         | SR+=4.7V/ $\mu$ s, SR-=5.1V/ $\mu$ s |
| ICMR                              | 0.8V                                 |

$V_{DD} = 0.8V$ ,  $V_{SS} = 0V$ ,  $V_{ICM} = 0.4V$ ,  $C_L = 5pF$

be operated with less voltage headroom consumption.

- With the use of bulk- and gate-biased cascodes, the output resistance of a folded-cascode fully differential OTA can be increased with no additional circuit or extra power consumption.
- Bulk-driven CMFB can sense the input common-mode voltage smaller than the threshold voltage.

In summary, the bulk-driven technique has been shown to be a serious contender for low-supply voltage amplifier design.

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# A New Bulk-Driven Input Stage Design for Sub 1-Volt CMOS Op-Amps

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**Abstract**— This paper presents a new design approach for a rail-to-rail bulk-driven input stage using a standard single-well (n-well in this paper) CMOS technology. This input stage can provide nearly constant transconductance and constant slew rate over the entire input common-mode voltage, operating with a wide supply voltage ranging from sub 1-volt ( $V_{T0}+3V_{DSSM}$ ) to the maximum allowed for the CMOS process, as well as preventing latch-up.

## I. INTRODUCTION

Lowering of the supply voltage in portable electronics has always been a priority for many years, as it allows reduction in the number of battery cells rendering the products more compact and light, and leading to decreased power consumption of the digital circuits. However, in analog circuits, particularly op-amps in unity-gain configuration, lowering the supply voltage degrades the signal-to-noise ratio. As a consequence, those op-amps require rail-to-rail input and output stages.

For the input stage, it is essential that its effective transconductance ( $g_m$ ) is nearly constant over the rail-to-rail Input Common-Mode Range (ICMR), as the large variation introduces signal distortion and creates difficulty in the frequency compensation of the multi-stage op-amps [1], [7]. Traditionally, complementary differential pairs are used to achieve the rail-to-rail operation, and the tail current is controlled with current switches to keep the  $g_m$  constant [1]. However, the mobility ratio of the complementary pairs ( $\mu_n/\mu_p$ ) is process- and temperature-dependent, causing the  $g_m$  variation to deviate by approximately 12% [2]. This motivates designers to come up with new circuit topologies using only a single type of the differential pair. Currently three candidates have been proposed – level-shifting [2], floating-gate [3], and the bulk-driven [4] techniques.

At the present time, the bulk-driven technique is probably the least popular, since the transconductance of a bulk-driven MOSFET ( $g_{mbs}$ ) is dependent on the bulk-to-source voltage ( $V_{BS}$ ). The level-1 model of the  $g_{mbs}$  is given by:

$$g_{mbs} = \gamma (2\beta I_{DS})^{0.5} / 2 (2|\Phi_F| - V_{BS})^{0.5} \quad (1)$$

where  $\gamma$  is the bulk-threshold parameter,  $\beta$  is the small-signal transconductance parameter,  $I_{DS}$  is the drain current, and  $2|\Phi_F|$  is the surface potential. The  $g_{mbs}$  is typically only 20-40% of the gate-driven transconductance [4]. However, the beauty of a bulk-driven MOSFET is that it removes the threshold voltage constraint. This property makes the bulk-driven approach worthy of development to improve its performance.

So far three proposals are available for improving the  $g_m$  variation of the Bulk-Driven Differential Pair (BDDP) – the complementary BDDP [5], the Replica-Biased Scheme (RBS) [5], and the feedback techniques [6]. The complementary BDDP technique utilizes the complementary behavior of the pairs to reduce the  $g_m$  variation. However, a special CMOS technology (e.g. a twin-well process) is required for the implementation. The RBS, as illustrated in Fig. 1, biases the gates of the pair to keep  $V_{BS} = 0$  so that the  $g_{mbs}$  becomes constant. The problem is, however,  $V_{BS} = 0$  means  $V_B = V_S$ , and it is impossible for the source-coupled voltage to swing rail-to-rail. Thus the  $g_m$  is constant over only a portion of the rail-to-rail ICMR. The feedback technique senses the input common-mode voltage ( $V_{ICM}$ ) and adjusts the tail current to reduce the  $g_m$  variation; however, this causes the Slew Rate (SR) to become  $V_{ICM}$  dependent.

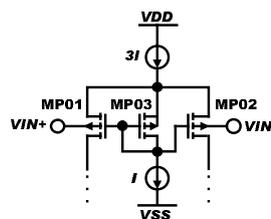


Figure 1. The bulk-driven RBS proposed in [5]

This paper presents a new bulk-driven rail-to-rail input stage using a standard single-well (n-well in this paper) CMOS process. This input stage achieves almost constant- $g_m$  and constant-SR, working with a wide supply voltage

ranging from sub 1-volt ( $V_{T0}+3V_{DSSat}$ ) to the maximum allowed by the CMOS process, and also diminishes the latch-up likelihood.

## II. THE NEW BULK-DRIVEN INPUT STAGE

### A. Topology

The idea of our bulk-driven input stage comes from utilizing two pairs of the RBS to cover all portions of the rail-to-rail ICMR. Fig. 2 illustrates the topology of our approach, which we call the Bulk-Driven Double Replica-Biased (BDDRB) input stage.

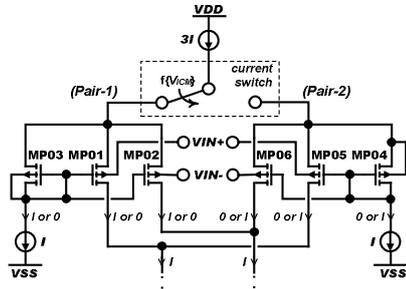


Figure 2. Topology of the BDDRB input stage

The BDDRB input stage consists of pair-1 (MP01~MP03) and pair-2 (MP04~MP06), which are assigned for the low and high portions of the ICMR, respectively, and a current switch.

The device sizes of pair-1 are all the same, and the same dc current runs through each device when the pair is selected. This leads MP03 to be the replica of the input pair, and  $V_{BS1,2}$  to be equal to  $V_{GS3}$  (= constant). The same argument goes to pair-2 except that  $V_{BS5,6}$  would be zero instead. The pair-1 would be operational for the ICMR between  $VDD-V_{SDsat}-V_{SG3}$  and  $VSS+V_{DSSat}$ , and for pair-2 the operational range would be between  $VDD-V_{SDsat}$  and  $VSS+V_{DSSat}+V_{SG4}$ . To maximize the ICMR a current switch is implemented so that the effective ICMR would be between  $VDD-V_{SDsat}$  and  $VSS+V_{DSSat}$ .

### B. Principle of Operation

Fig. 4(a) illustrates how the BDDRB input stage can be realized as a transistor circuit. Again, MP01~MP03 (pair-1) and MP04~MP06 (pair-2) are the replica-biased input pairs for the low and high portions of the ICMR, respectively. MP09~MN12 form a current switch and work as a function of  $V_{ICM}$ . This input stage is configured such that it normally operates with pair-1. When  $V_{ICM}$  becomes high and causes  $V_{SG9}$  to be greater than the threshold voltage ( $|V_{T0}|$ ), the switch deactivates pair-1 and activates pair-2 instead. Conversely, when  $V_{ICM}$  becomes low and causes  $V_{SG9} < |V_{T0}|$ , pair-1 turn on and pair-2 turns off. The bias-voltage,  $V_{SWTCH}$ , controls the crossover voltage between the two points.

To verify the operation of the BDDRB input stage, it was necessary to implement it in an op-amp. For this we chose a folded-cascode two-stage op-amp, as illustrated in Fig. 4(b), to present as an application example.

## III. SIMULATION RESULTS

Using the BSIM3 MOSFET models of a 0.18 $\mu$ m CMOS process, we simulated the op-amp of Fig. 4 with a supply voltage of 0.8-volt and a load resistance and capacitance of 1M $\Omega$  and 5pF, respectively. Table I shows the summary of the simulation results.

TABLE I. SIMULATION RESULTS OF THE OVERALL PERFORMANCE OF THE OP-AMPS IN FIGURE. 4

| Characteristics   | Simulated Results   |
|---|---|
| Open-loop DC gain   | 60dB  |
| Unity-gain frequency  | 0.6MHz  |
| Phase margin  | 58°   |
| ICMR  | 0.6V  |
| Total current consumption   | 61~74 $\mu$ A ( $V_{ICM}$ dependent)  |
| SR  | SR+ = 1.0V/ $\mu$ s, SR- = -0.5V/ $\mu$ s   |
| Output voltage swing  | 0.6V  |
| Common-mode rejection ratio   | 63dB (when $V_{ICM} = 0.5(VDD+VSS)$ )   |
| Power Supply Rejection Ratio (PSRR)   | PSRR+ = 58dB, PSRR- = 79dB  |
| Input referred noise voltage  | 146~169nV/ $\sqrt$ Hz (white noise only, $V_{ICM}$ dependent)                                 |
| Total harmonic distortion, $A_{VCL}=+1V/V$  | 0.014% (-77.1dB) for 0.6Vp-p, 1kHz sine wave<br>0.093% (-60.6dB) for 0.6Vp-p, 10kHz sine wave |
| Measurement condition: $VDD = 0.8V$ , $VSS = 0V$ , $C_L = 5pF$ , $R_L = 1M\Omega$ |   |

The simulation confirmed the rail-to-rail ICMR operation ( $VDD-V_{SDsat14}$  to  $VSS+V_{DSSat07}$  precisely). Fig.3 and Fig. 5 show the simulation results of the open-loop gain frequency response and the effective tail current of the op-amp in Fig. 4, which indicate that both characteristics are nearly  $V_{ICM}$  independent. Fig. 6 gives the simulation results of the effective transconductance [ $g_m(\text{eff})$ ] of the op-amp versus  $V_{ICM}$ .

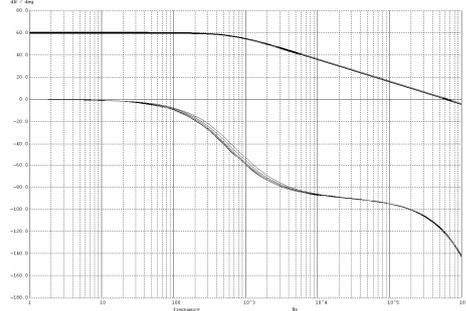


Figure 3. Simulated frequency response of the op-amps for  $V_{ICM}$  varying from 0.1 to 0.7V with a 0.1V step

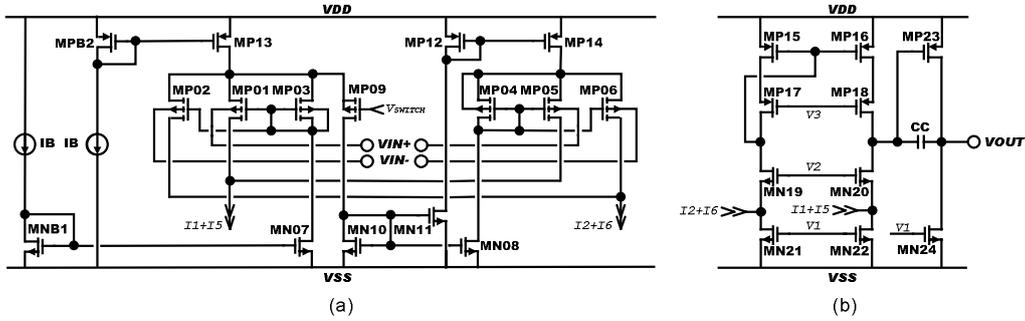


Figure 4. An application example of the BDDRB input stage in a folded-cascode two-stage op-amps (a) the BDDRB input stage, and (b) a folded-cascode two-stage op-amps

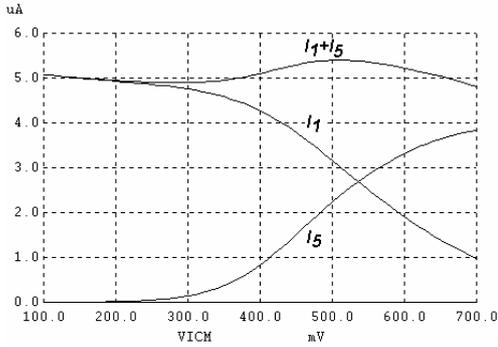


Figure 5. Simulated tail current vs  $V_{ICM}$

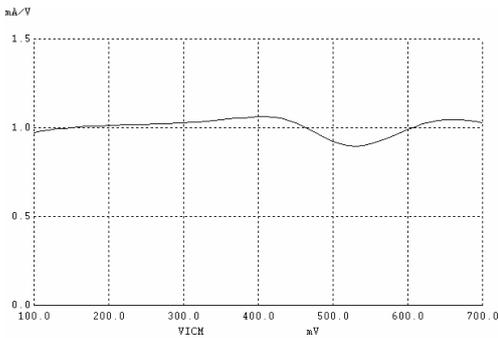


Figure 6. Simulated  $g_m(\text{eff})$  vs  $V_{ICM}$

Fig. 6 indicates that the  $g_m$  variation is approximately 10% over the rail-to-rail ICMR operation. This variation peaks at the transition point between the two pairs, i.e. when the pairs are partially on and off. It is worth noting that the source-to-bulk voltage of the input pairs ( $V_{SB1}$  and  $V_{SB5}$ )

change at the transition stage, which should also have created a major impact in the  $g_m$  variation according to (1). Fig. 7 shows the simulation results of  $V_{SB1}$  and  $V_{SB5}$  versus  $V_{ICM}$ .

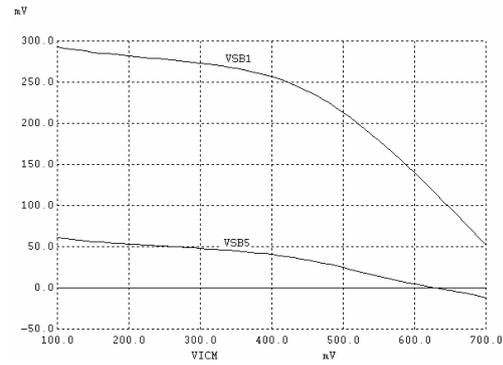


Figure 7. Simulated  $V_{SB1}$  and  $V_{SB5}$  vs  $V_{ICM}$

#### IV. ADVANTAGES AND DISADVANTAGES

An important practical advantage of the BDDRP input stage is that it requires no special CMOS process. Other advantages are  $g_m(\text{eff})$  and SR of the op-amp remain relatively constant with respect to  $V_{ICM}$ , and the circuit prevent latch-up. Conventional BDDP techniques require very low supply voltages, otherwise the rail-to-rail ICMR operation would cause the bulk terminals to be strongly forward-biased. With the BDDRB input stage, the bulk-to-source voltages remain as the same condition as the replica device regardless of the supply voltage condition. For confirmation, we simulated the circuit of Fig. 4 with a 3-volt power supply and observed that the rail-to-rail ICMR operations did not result in any significant input current or substantial forward-biased pn junctions.

However, in comparison to previously mentioned bulk-driven techniques, our proposal increases input referred

noise. Previously mentioned bulk-driven techniques utilize the depletion-mode characteristics of a MOSFET so that the input pair can be always on for rail-to-rail. In contrast, our input stage has two pairs connected in parallel, and except in the transition stage one of the pair is off. The off-pair contributes additional thermal noise, as it is inversely proportional to  $g_{mbs}$  [11].

Another drawback to previously mentioned bulk-driven techniques is the increase in input capacitance, since two input pairs are utilized in our proposal. The input capacitance of a bulk-driven MOSFET consists of  $C_{bsub}$  and  $C_{bs}$ , where  $C_{bsub}$  is the well-to-substrate capacitance and  $C_{bs}$  is the bulk-to-source capacitance.  $C_{bsub}$  depends on layout design, and a detail description is given in [4].  $C_{bs}$ , on the other hand, can be controlled by circuit designers to some extent as it is directly related to its source-to-bulk voltage. Reducing the forward-bias of the bulk-terminal results in decreased  $C_{bs}$  as well as increased input resistance. With the BDDRB input stage, this can be easily achieved by decreasing the source-to-bulk voltage of the replica device ( $V_{SB3}$  of Fig 4(a), which is equivalent to  $V_{SG3}$ ). Fig. 8 illustrates the simulation results of the input impedance measurements for the op-amp shown in Fig. 4.

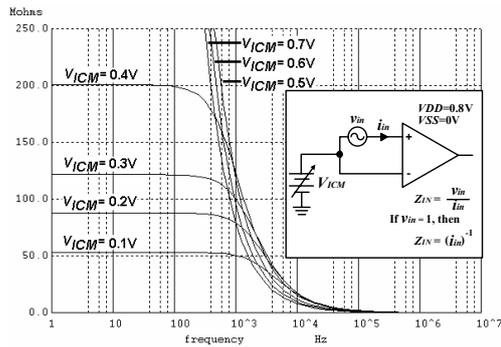


Figure 8. Simulation results of the circuit-level input impedance characteristic

## V. CONCLUSION

A new approach for the bulk-driven input stage called BDDRB to achieve rail-to-rail ICMR operation has been

presented. This approach leads the operational supply voltage to be from under 1-volt to the maximum allowed by the CMOS process used, as well as diminishing the latch-up problem. SPICE simulations indicate that the  $g_m$  is nearly constant (within 10%) over the entire ICMR whilst the effective tail current remains almost unchanged. The additional hardware implemented to achieve this performance is only a replica circuit for each pairs and a current switch.

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# Bulk-Driven Flipped Voltage Follower

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**Abstract**— A voltage buffer so-called the bulk-driven flipped voltage follower is presented. This proposal is based on the Flipped Voltage Follower (FVF) technique, but a bulk-driven MOSFET with the replica-biased scheme is utilized for the input device to eliminate the DC level shift. The proposed buffer has been designed and simulated with a  $0.35\mu\text{m}$  CMOS technology. The input current and capacitance of our proposal are  $1.5\text{pA}$  and  $9.3\text{fF}$  respectively, and with  $0.8\text{V}$  peak-to-peak  $500\text{kHz}$  input, the total harmonic distortion is  $0.5\%$  for a  $10\text{pF}$  load. This circuit can operate from a single  $1.2\text{V}$  power supply and consumes only  $2.5\mu\text{A}$ .

## I. INTRODUCTION

Voltage buffers play an essential role in analog and mixed-signal circuits and processing systems, where they are widely used for driving large capacitive loads at high speeds. The ideal performance of a voltage buffer is not only to drive the large load as fast as possible but also with minimal power consumption, which means that the buffer needs to have high slew rate and low static power consumption. Today, it is evident that the Flipped Voltage Follower (FVF) proposed by R. G. Carvajal *et al* in [1] is one of the closest to the ideal voltage buffer, as many recent proposals are utilizations and/or modifications of the FVF [2]-[5].

Recently, the new version of the class-AB FVF that is free from the DC level-shift has been proposed by Ramirez-Angulo *et al* [5]. In this paper, we present a much simpler technique which can eliminate the DC level shift and convert into class AB operation, whilst preserving the advantages of the FVF approach— low-power consumption with high-power drive.

## II. PREVIOUS ESSENTIAL WORKS

This section covers a brief review of voltage followers and the bulk-driven MOSFETs used in a differential pair, which we have utilized and forms the essential part of our proposal.

### A. Voltage followers

Figure 1 illustrates two types of voltage followers. Figure 1(a) is the conventional type of a voltage follower, which is also known as a source follower [6]-[7]. The input device MP01 is biased with the drain current of  $I_{REF}$ , therefore the gate-to-source voltage  $V_{GS,MP01}$  becomes constant if the body-

effect is neglected, and therefore the output voltage  $V_{OUT}$  is equal to  $V_{IN} + V_{GS,MP01}$ . Figure 1(b) illustrates the FVF, in which  $V_{OUT}$  is also shifted up by  $V_{GS,MP01}$  from  $V_{IN}$ , however, in contrast to Figure 1(a), the beauty of the FVF is that it has current sourcing and sinking capabilities at the output, which can lead to delivering both high-power driving as well as low-power consumption simultaneously.

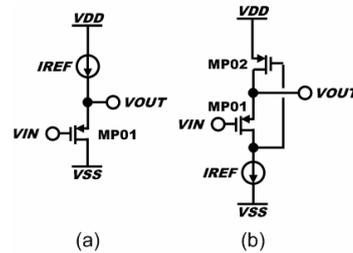


Figure 1. Voltage followers (a) common-drain amplifier (voltage follower) and (b) FVF proposed in [1]

### B. Bulk-driven MOSFETs used in differential pairs

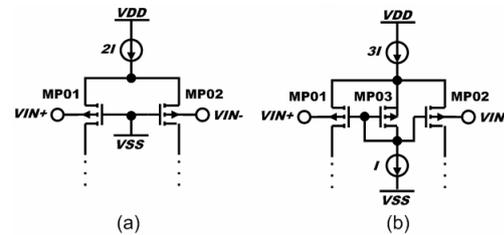


Figure 2. Bulk-driven differential pair (a) pMOS input pair and (b) the replica-biased scheme proposed in [10]

In low-voltage rail-to-rail operational amplifier designs, there exists a design technique called the bulk-driven approach. The traditional design technique for rail-to-rail operational amplifiers is the deployment of complementary differential pairs with the tail current being controlled with current switches to keep the  $g_m$  constant [8]. However, due to the fact that the mobility ratio of the complementary pairs ( $\mu_n/\mu_p$ ) is process- and temperature dependent, causing the  $g_m$

variation to deviate by approximately 12% [9], there exist circuit topologies which use only a single type of the differential pair, where one of them is the bulk-driven one. Figure 2(a) illustrates a bulk-driven differential pair that uses p-type devices only.

The primary problem of Figure 2(a), however, is that the transconductance of a bulk-driven MOSFET ( $g_{mbs}$ ) is dependent on the bulk-to-source voltage ( $V_{BS}$ ). The level-1 model of the  $g_{mbs}$  is given by:

$$g_{mbs} = \gamma (2\beta I_{DS})^{0.5} / 2 (2|\Phi_F| - V_{BS})^{0.5} \quad (1)$$

where  $\gamma$  is the bulk-threshold parameter,  $\beta$  is the small-signal transconductance parameter,  $I_{DS}$  is the drain current, and  $2|\Phi_F|$  is the surface potential.

To overcome the concern of  $g_{mbs}$  dependency over the  $V_{BS}$ , Blalock *et al* [10] proposed the Replica-Biased Scheme (RBS) as illustrated in Figure 2(b). The pMOS identified as MP03 is the replica device biasing the gates of the pair. Since the bulk of MP03 is shorted with its source, the  $V_{BS}$  of the pair is kept at zero.

We have noted the advantage from Blalock's approach namely that the condition of  $V_{BS} = 0$  is kept constant, meaning  $V_B = V_S$ , and we chose to apply this to the FVF illustrated in Figure 1(b) to remove the DC level shift.

### III. PROPOSED BULK-DRIVEN FLIPPED VOLTAGE FOLLOWER

Figure 3 illustrates our proposal of the modified FVF, which we have named as "Bulk-Driven Flipped Voltage Follower (BDFVF)". As mentioned in the previous section, this is the FVF for which the input device has been modified to a bulk-driven MOSFET biased by the replica circuit to eliminate DC level shift.

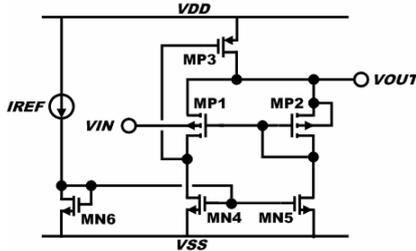


Figure 3. Bulk-driven flipped voltage follower (class-A)

The operation principle of the BDFVF of Figure 3 is very simple to follow. MP1, MP3, and MN4 form the FVF. MP1 is the input device, which its bulk is utilized to feed the input. MP2 and MN5 are the replica devices for MP1 and MN4 respectively. Note that the bulk of MP2 is physically shorted to its source, which is the output node. Since the gate of MP1 is biased with the diode-connected MP2, as well as the drain current of MP1 and MP2 are equally set to  $I_{REF}$ ,  $V_B$  and  $V_S$  of MP1 becomes virtually shorted (i.e.  $V_{BSMP1} = 0$ ), and in effect the output voltage  $V_{OUT}$  becomes equal to  $V_{IN}$ .

Our proposal of Figure 3 works well, however since it is class-A type there is a limitation in its sink capability to  $2I_{REF}$ , which leads to poor pull capability in driving large loads at high speed. To overcome this problem, we have modified the circuit of Figure 3 to class-AB type as shown in Figure 4.

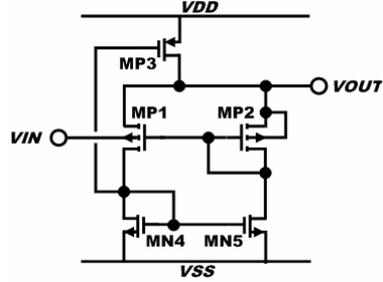


Figure 4. Proposed class-AB bulk-driven flipped voltage follower

The difference of Figure 4 from Figure 3 is that only MN4 has been modified to diode-connected instead of the constant bias to  $I_{REF}$ . In this way, MP1 and MP2 can also have the same drain current and hence the replica-biased scheme remains valid. This simple change has led to significant improvement in the sink capability of the output without the need of widening MN4 or MN5 or increasing  $I_{REF}$ . In the next section, simulation results are provided.

### IV. SIMULATED RESULTS

#### A. Overall Performance

Using the BSIM3 MOSFET models of a 0.35 $\mu$ m CMOS process, we designed and simulated the BDFVF of Figure 4. Table I shows the simulation results summarizing the overall performance.

TABLE I. SIMULATION RESULTS OF THE OVERALL PERFORMANCE OF THE CLASS AB BDFVF CIRCUIT OF FIGURE. 4

| Parameter  | Simulated results  |
|--|--|
| 3dB frequency  | 2.8MHz   |
| Total current consumption (when IL=0)  | 2.5 $\mu$ A  |
| Slew rate (VDD=2V, VSS=0V, CL=10pF, VIN=1V $\leftrightarrow$ 2V)                           | 1.9V/ $\mu$ s  |
| PSRR+ / PSRR-  | 41.7dB / 42.0dB (dc to 100kHz)                                       |
| 1/f noise at 1kHz  | 880nV/ $\sqrt$ Hz  |
| THD (Vpp=0.8V VDD=1.5V, VSS=0V, CL=10pF)   | 0.0747% when f=1kHz<br>0.0794% when f=100kHz<br>0.501% when f=500kHz |
| Input voltage range (VDD=2V, VSS=0V)   | 1V to 2V<br>For offset $\leq$ 10mV                                   |
| Load regulation  | $\pm$ 15 $\mu$ A for offset $\leq$ 10mV                              |
| Input current  | 1.5pA  |
| Input capacitance  | 9.3fF  |
| Unless stated, the set up condition is:<br>VDD=1.2V, VSS=0V, VIN=1V, CL=10pF, IL=0 $\mu$ A |  |

Figure 5 illustrates the simulated plot of  $V_{OUT}$  versus  $V_{IN}$  with the setup of  $VDD = 2V$  and  $VSS = 0V$ . The simulation

results indicate that the offset between  $V_{OUT}$  and  $V_{IN}$  was 10mV for the input range from 1V to 2V.

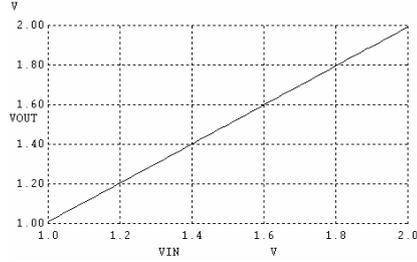


Figure 5.  $V_{OUT}$  vs  $V_{IN}$  ( $V_{DD}=2V$ ,  $V_{SS}=0V$ )

Figure 6 illustrates the simulated plot of  $V_{OUT}$  with a sinusoidal  $V_{IN}$  input with 0.8V peak-to-peak magnitude and 500kHz frequency, and with the set up of  $V_{DD} = 2V$ ,  $V_{SS} = 0V$ , and  $CL = 10pF$ . The simulation results indicate that the Total Harmonic Distortion (THD) was 0.5%.

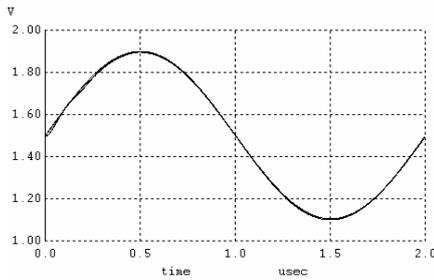


Figure 6.  $V_{OUT}$  and  $V_{IN}$  with 0.8Vpp 500kHz sinusoidal input ( $V_{DD}=2V$ ,  $V_{SS}=0V$ ,  $CL=10pF$ )

Figure 7 illustrates the simulated plot of  $V_{OUT}$  regulation capability against the load current  $I_L$ . With the setup of  $V_{DD} = 1.5V$ ,  $V_{SS} = 0V$ , and  $V_{IN} = 1V$ , the simulation results indicate that  $V_{OUT}$  kept on regulated within 10mV until the load current reaches to  $\pm 15\mu A$ .

### B. Input impedance

Using bulk-driven MOSFETs in a differential pair of the operational amplifier is known to be a disadvantage in input current and capacitance [11]. In this sub-section, we present the theoretical overview as well as the simulated results to state that this disadvantage is not the case with the BDFVF.

#### 1) Input current

With a bulk-driven MOSFET as an input device, the input signal is fed into the pn-junction of the MOSFET. The current through the pn-junction  $I_{Dpn}$  is modeled by Equation 2 [12]-[13]:

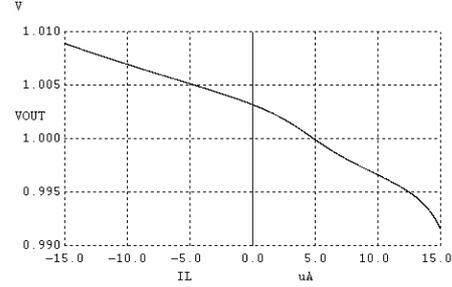


Figure 7. Load regulation ( $V_{DD}=2V$ ,  $V_{SS}=0V$ ,  $V_{IN}=1V$ )

$$I_{Dpn} = I_s \exp(V_D/V_T) \quad (2)$$

where  $I_s$  is the pn-junction current, which is also known as the scale current, when the voltage across the pn-junction  $V_D$  is zero.  $V_T$  is the thermal voltage, which is modeled as

$$V_T = kT/q \quad (3)$$

where  $k$  is the Boltzmann constant ( $=1.38 \times 10^{-23} \text{JK}^{-1}$ ),  $T$  is the temperature in Kelvin, and  $q$  is the charge of an electron ( $=1.602 \times 10^{-19} \text{C}$ ). At room temperature,  $V_T$  is approximately 26mV.

$I_s$  can be described as in Equation 4:

$$I_s \propto A_D [(1/N_A) + (1/N_D)] \quad (4)$$

where  $A_D$  is the area of the diode junction, and  $N_A$  and  $N_D$  are the doping concentrations of the acceptors and donors respectively.

In the case of a bulk-driven differential pair, the input current is expected to be large because of the bulk being forward-biased. On the other hand for BDFVF, a large input current is not expected since the aim is to achieve a virtual short between the input and output. To affirm this theoretical consideration further, we have simulated deploying the setup used for arriving at Figure 5 to observe the offset behavior and the input current, as shown in Figure 8 and 9 respectively.

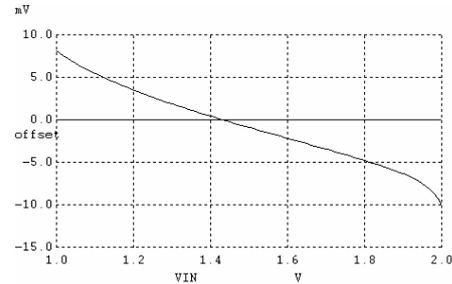


Figure 8. Offset voltage of Figure 5

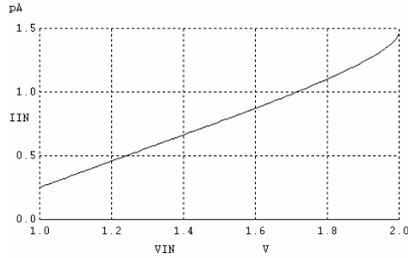


Figure 9. Input current ( $V_{DD}=2V$ ,  $V_{SS}=0V$ )

The simulated result of Figure 9 shows that the input current remains at less than 1.5pA.

## 2) Input capacitance

The capacitance of the pn-junction  $C_j$  can be modeled by Equation 5 [11]-[13]:

$$C_j = C_{j0} / (1 + (V_{SB}/\phi_0))^{0.5} \quad (5)$$

In the case of a bulk-driven differential pair, the input capacitance is expected to be large because of the bulk being forward-biased. On the other side for BDFVF, a large input capacitance is not expected since the aim is to achieve a virtual short between the input and output. To affirm this theoretical consideration further, we have set up the simulation condition as shown in Figure 10.

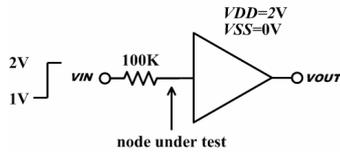


Figure 10. Simulation setup for the input capacitance

The simulated plot of the setup in Figure 10 is given in Figure 11.

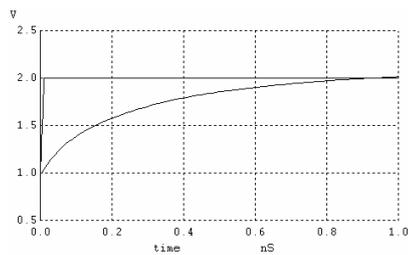


Figure 11. Simulation results for the Figure 10 setup

From Figure 11, the time constant  $\tau$  was found to be 0.93ns. Hence, the input capacitance was determined as 9.3fF ( $\tau=RC$ ).

## V. CONCLUSION

A new type of FVF called BDFVF has been presented. This proposal utilizes a bulk-driven MOSFET with the replica-biased scheme as the input device to eliminate the DC level shift. The theoretical overview of the input current and capacitance has been provided, and the simulation results showed that the input current and capacitance are in the pico-amp and femto-Farad ranges. The attractive and advantageous performances of the FVF, such as high-power driving and low-power consumption were retained. The BDFVF is a powerful block of the FVF family which is free of level shift.

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## CMOS buffer using complementary pair of bulk-driven super source followers

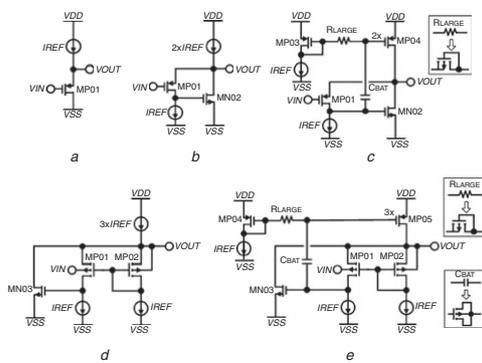
Y. Haga and I. Kale

A power-efficient rail-to-rail CMOS analogue voltage buffer is presented. It consists of a complementary pair of super source followers, but a bulk-driven input device with the replica-biased scheme is utilised to eliminate the DC level shift, quasi-floating gate transistors to achieve class-AB performance, and a current switch which shifts between the complementary pair to allow rail-to-rail operation. The proposed buffer has been designed for a 0.35  $\mu\text{m}$  CMOS technology to operate at a 1.8 V supply voltage. Simulated results are provided to demonstrate the total harmonic distortion for a 1.6 V<sub>pp</sub> 100 kHz sine wave with a 68 pF load is as low as  $-46$  dB, while the static current consumption remains under 8  $\mu\text{A}$ .

**Introduction:** Voltage buffers play a fundamental role in analogue and mixed-signal circuits and processing systems, especially for applications where the weak signal needs to be delivered to a large capacitive load without being distorted [1, 2]. To accomplish this demand, the input capacitance of the buffer needs to be as small as possible so that the weak signal is not affected under any circumstances, and the output stage needs to have a high slew-rate performance so that the signal can remain driven with large capacitive loads. Furthermore, for applications in portable electronics, where the battery lifetime needs to be extended to the maximum possible, the static power consumption of the buffer must be small while the slew-rate remains high. This suggests the use of a class-AB output stage in the buffer.

We recently proposed a CMOS buffer using a new circuit-design technique, the so-called ‘bulk-driven flipped voltage follower’ [3], and we demonstrated that this proposed buffer meets most of the needs mentioned above. In this Letter, we present a novel CMOS buffer based on our previous work reported in [3] which implements additional features of rail-to-rail power-efficient operation.

**Class-AB bulk-driven super source follower:** This Section briefly describes the previous works [1–4] using Fig. 1, which we have utilised to form the core part of our proposed CMOS buffer – a class-AB bulk-driven super source follower.



**Fig. 1** Class-A source follower (Fig. 1a), class-A super source follower (Fig. 1b), class-AB super source follower proposed by Lopez-Martin *et al.* [2] (Fig. 1c), class-A bulk-driven super source follower (Fig. 1d), class-AB bulk-driven super source follower using proposed QFG technique [4] (Fig. 1e)

Fig. 1a illustrates a conventional pMOS source follower, widely used as a level-shifted voltage buffer [1, 2]. If the body-effect is neglected, then the output voltage  $V_{OUT}$  follows the input voltage  $V_{IN}$  with an upward DC shift, i.e.  $V_{OUT} = V_{IN} + V_{SG_{MP01}}$ , where  $V_{SG_{MP01}}$  is the source-to-gate voltage of the transistor MP01. In the case of an nMOS source follower,  $V_{OUT}$  is instead shifted down from  $V_{IN}$ . This conventional source follower is widely used, however the drawback is that it is sensitive to resistive loads. Since the drain current of MP01 is affected by the output current, the DC-level  $V_{SG_{MP01}}$  cannot be kept constant. To overcome this concern, there exists a buffer which is

often referred to as a super source follower [1], as shown in Fig. 1b. The topology of Fig. 1b is the same as Fig. 1a, but since the drain current through MP01 is biased with a constant current  $I_{REF}$  and is independent of the output current,  $V_{SG_{MP01}}$  is also held constant against the output current. Today, we can observe many published proposals using this super source follower.

Recently, López-Martín *et al.* emphasised in [2] that despite the output becoming much more insensitive to resistive loads with the super source follower, the slew-rate (SR) remains in class-A operation. In the case of a pMOS super source follower as shown in Fig. 1b, the positive SR is limited to  $I_{REF}/C_L$ , where  $C_L$  is the load capacitance. Hence increasing  $I_{REF}$  leads to one possible approach for SR improvement, but at a cost of greater static power consumption. To avoid this trade-off, López-Martín *et al.* proposed a class-AB super source follower [2] by using a quasi-floating gate (QFG) technique presented in [4]. Their proposed circuit diagram is depicted in Fig. 1c.

In Fig. 1c, the gate of MP04 is weakly connected to the gate of MP03 with a large resistor  $R_{LARGE}$ , and also to the gate of MN02 with a capacitor  $C_{BAT}$ . In terms of DC characteristics, there exists no current flow across  $R_{LARGE}$  and therefore the gate voltage of MP03 and MP04 are the same. Thus the static power dissipation between Figs. 1b and c remains the same. In terms of AC characteristics, a high-pass filter is formed with a cutoff frequency of  $1/(2\pi R_{LARGE} C_{BAT})$ , when observed from the gate of MN02 to the gate of MP04. Thus the AC element of the signal at the gate of MN02 can propagate to the gate of MP04, which in turn achieves class-AB operation without introducing any extra static current consumption. Furthermore, it is remarkable to realise in [2, 4] that a unity-size diode-connected MOSFET but in the cutoff region can form a substantially large resistance of  $R_{LARGE}$ , which leads to achieving a low cutoff frequency  $1/(2\pi R_{LARGE} C_{BAT})$  with a moderately small capacitance of  $C_{BAT}$ . In [2], López-Martín *et al.* discuss the  $C_{BAT}$  value in terms of attenuation factor  $\alpha (\approx 1/(1 + CGS4/C_{BAT}))$ . A  $C_{BAT}$  greater than five times  $CGS4$  leads to  $\alpha > 0.83$ , which is enough to propagate almost all frequencies except the DC component of the signal.

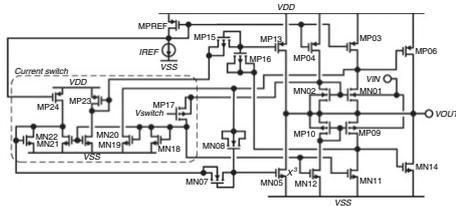
Fig. 1d illustrates the bulk-driven version of the super source follower, which is the same type of circuit-design technique we previously presented in [3]. As can be observed, the input is connected to the bulk terminal of MP01 instead of its gate. MP02 is the replica of the input device MP01, i.e. MP02 and MP01 have equal transistor sizing and are biased with the identical drain current and the gate voltage. Since the bulk-terminal of MP02 is directly shorted to its source-terminal, MP01 tends to replicate the conditions of MP02 and hence the source-terminal follows the input voltage with no DC voltage in between, thus  $V_{OUT} = V_{IN}$ . Remarkably, the input capacitance  $C_{IN}$  of this type of buffer can be small because of the small junction capacitance of MP01. The junction capacitance of a MOSFET  $C_j$  is given by:

$$C_j = C_{j0}/(1 + (V_{SB}/\Phi_0)^{0.5})$$

where  $C_{j0}$  is the zero-bias ( $V_{SB} = 0$ ) junction capacitance,  $V_{SB}$  is the bulk-to-source voltage, and  $\Phi_0$  is the bulk junction potential. Since  $V_{SB}$  of MP01 in Fig. 1d is designed to be zero, the junction capacitance of MP01 is constant at  $C_{j0}$ . We discuss the simulated value of  $C_{IN}$  later on in this Letter.

Fig. 1e shows a class-AB bulk-driven super source follower, where the class-AB operation has been implemented to Fig. 1d with the same technique proposed by Lopez-Martín *et al.* in [2]. However, we have chosen a modified approach for implementing the  $C_{BAT}$ . Ramírez-Angulo *et al.* [4] stated that, regarding the significance of the QFG technique, the actual value of  $C_{BAT}$  does not need to be highly accurate, as long as even a low frequency signal can be coupled. Owing to and appreciating this fact, we attempted to eliminate the need for a poly-poly capacitor, and chose to form the  $C_{BAT}$  with a MOSFET as shown in Fig. 1e. We observe that the size of the MOSFET five times larger than MP05 is more than enough to achieve good attenuation.

**Proposed rail-to-rail class-AB CMOS buffer:** We applied the bulk-driven super source follower as shown in Fig. 1e in our design to propose a rail-to-rail power-efficient CMOS voltage buffer. Fig. 2 illustrates the circuit diagram of our proposal.



**Fig. 2** Proposed class-AB rail-to-rail CMOS analogue buffer using complementary pair of bulk-driven super source followers

The operation principle of Fig. 2 is very simple to follow. From MN01 to MN08 and from MP09 to MP16 form an nMOS-type and pMOS-type of the bulk-driven super source follower, respectively, and from MP17 to MP24 forms a current switch. The  $V_{switch}$  at the gate of MP17 determines the switching point between the two types of follower. When  $V_{IN}$  (and thus  $V_{OUT}$ ) is close to  $V_{SS}$  the pMOS follower is active while the nMOS follower is off, and when  $V_{IN}$  moves towards  $V_{DD}$ ,  $V_{OUT}$  and the drain voltage of MN02 also increase and eventually MP17 turns on to reduce the drain current of MN01, MN02 and MN05 (i.e. to shut off the nMOS follower) and instead to increase the drain current of MP09, MP10 and MP13 (i.e. to activate the pMOS follower) to continue the buffer operation.

**Simulated results:** Using a 0.35  $\mu\text{m}$  CMOS process, we chose to operate the circuit of Fig. 2 at 1.8 V supply voltage and simulated with the BSIM3 MOSFET models. Table 1 shows the simulation results summarising the overall performance. From Table 1 we emphasise that the proposed buffer of Fig. 2 meets the demands we discussed in the Introduction. The input capacitance is as small as 17 fF, the SR is very high such that the buffer can deliver a 1.6 Vpp 100 kHz signal with a total harmonic distortion as low as -46 dB when the capacitive load is as large as 68 pF, while the static current consumption remains under 8  $\mu\text{A}$ . Also the offset voltage remains as small as 10 mV throughout the rail-to-rail operation.

**Table 1:** Simulated results of overall performance of Fig. 2

| Parameter   | Simulated results  |
|---|--|
| -3 dB frequency   | 6 MHz  |
| Static current dissipation  | 5 $\mu\text{A}$ to 8 $\mu\text{A}$ for $V_{IN}$ sweeping between $V_{DD}$ and $V_{SS}$   |
| Slew-rate   | SR + = 9.3 V/ $\mu\text{s}$ , SR - = 13.7 V/ $\mu\text{s}$   |
| Input capacitance   | 17 fF  |
| Offset voltage  | < 10 mV for $V_{IN}$ sweeping between ( $V_{DD} - 50$ mV) and ( $V_{SS} + 50$ mV)  |
| THD   | -52 dB (1.6 Vpp at 100 kHz, CL = 10 pF)<br>-50 dB (1.6 Vpp at 100 kHz, CL = 22 pF)<br>-47 dB (1.6 Vpp at 100 kHz, CL = 47 pF)<br>-46 dB (1.6 Vpp at 100 kHz, CL = 68 pF) |
| Simulated condition: $V_{DD} = 1.8$ V, $V_{SS} = 0$ V, $V_{SW} = 0.9$ V, CL = 10 pF |  |

**Conclusion:** A new type of CMOS buffer using the complementary pair of bulk-driven super followers is presented. Utilising the bulk-driven MOSFETs with the replica-biased scheme and the QFG techniques into the buffer enabled us to have a few femto-Farad range of the input capacitance so that the weak input signals are minimally affected, while delivering the signal without much distortion even if the capacitive load is very large. The static current consumption can remain small too. Our proposed buffer can become a serious contender for portable electronics needing to deliver weak analogue signals into large capacitive loads with as little distortion as possible.

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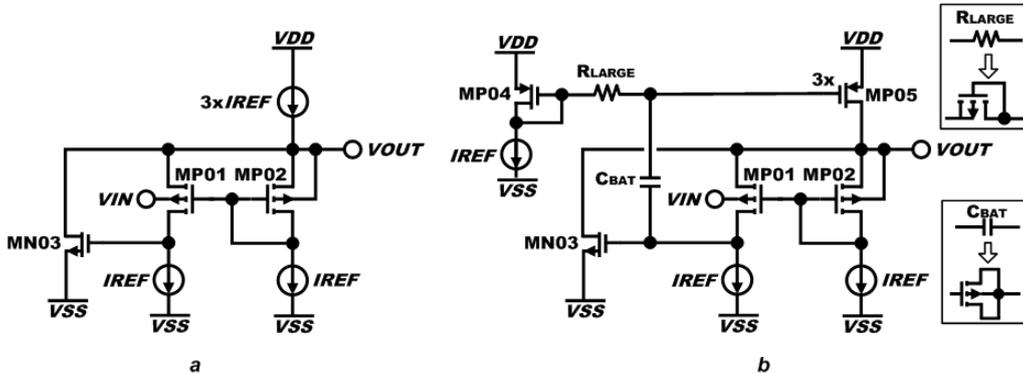


Figure 2. Bulk-driven super source followers (a) class-A operation, and (b) converting into class-AB operation using the QFG technique proposed by Ramirez-Angulo *et al* [2-3]

Recently, A.J. Lopez-Martin *et al* emphasized in their work in [2] that despite the output becoming much insensitive to resistive loads with the super source follower, the Slew-Rate (SR) remains in class-A operation. In the case of a pMOS super source follower as shown in Figure 1b, the positive SR is limited to  $I_{REF}/C_L$ , where  $C_L$  is the load capacitance. Hence increasing  $I_{REF}$  leads to one possible approach for the SR improvement, but at a cost of larger static power consumption. To avoid this trade-off, A.J. Lopez-Martin *et al* proposed a class-AB super source follower in [2] by using a quasi-floating gate (QFG) technique presented in [3]. Their proposed circuit diagram is depicted in Figure 1c.

In Figure 1c, the gate of MP04 is weakly connected to the gate of MP03 with a large resistor  $R_{LARGE}$ , and also to the gate of MN02 with a capacitor  $C_{BAT}$ . In terms of DC characteristics, there exists no current flow across  $R_{LARGE}$  and therefore the gate voltage of MP03 and MP04 are the same. Thus the static power dissipation between Figure 1b and Figure 1c remains the same. In terms of AC characteristics, a high pass filter is formed with a cutoff frequency of  $1/(2\pi R_{LARGE} C_{BAT})$ , when observed from the gate of MN02 to the gate of MP04. Thus the ac element of the signal at the gate of MN02 can propagate to the gate of MP04, which in turn achieves class-AB operation without introducing any extra static current consumption. Furthermore, it is remarkable to realize in [2-3] that a unity-size diode-connected MOSFET but in the cutoff region can form a substantially large resistance of  $R_{LARGE}$ , which leads to achieving a low cutoff frequency  $1/(2\pi R_{LARGE} C_{BAT})$  with a moderately small capacitance of  $C_{BAT}$ . In [2], A.J. Lopez-Martin *et al* discuss the  $C_{BAT}$  value in terms of attenuation factor  $\alpha (\approx 1/(1+C_{GS4}/C_{BAT}))$ . A  $C_{BAT}$  greater than 5 times  $C_{GS4}$  leads  $\alpha > 0.83$ , which is enough to propagate almost all frequencies except the DC component of the signal.

Figure 2a illustrates the bulk-driven version of the super source follower, which is the same type of circuit-design technique the authors previously presented in [4]. As can be observed, the input is connected to the bulk terminal of MP01 instead of its gate. MP02 is the replica of the input device

MP01, i.e. MP02 and MP01 having equal transistor sizing and are biased with the identical drain current and the gate voltage. Since the bulk-terminal of MP02 is directly shorted to its source-terminal, MP01 tends to replicate the conditions of MP02 and hence the source-terminal follows the input voltage with no DC voltage in between, thus  $V_{OUT} = V_{IN}$ . Remarkably, the input capacitance  $C_{IN}$  of this type of buffer can be small because of the small junction capacitance of MP01. The junction capacitance of a MOSFET  $C_j$  is given by:

$$C_j = C_{j0} / (1 + (V_{SB} / \Phi_0))^{0.5} \quad (1)$$

where  $C_{j0}$  is the zero-bias ( $V_{SB}=0$ ) junction capacitance,  $V_{SB}$  is the bulk-to-source voltage, and  $\Phi_0$  is the bulk junction potential. Since  $V_{SB}$  of MP01 in Figure 1d is designed to be zero, the junction capacitance of MP01 is constant at  $C_{j0}$ . We will discuss the simulated value of  $C_{IN}$  later on in this paper.

Figure 2b shows a class-AB bulk-driven super source follower, where the class-AB operation has been implemented to Figure 1d with the same technique proposed by A.J. Lopez-Martin *et al* in [2]. However, we have chosen a modified approach for implementing the  $C_{BAT}$ . Ramirez-Angulo *et al* stated the significance of the QFG technique in [3] that the actual value of  $C_{BAT}$  does not need to be highly accurate, as long as even a low frequency signal can be coupled. Owing to and appreciating this fact, we attempted to eliminate the need for a poly-poly capacitor, and chose to form the  $C_{BAT}$  with a MOSFET as shown in Figure 1e. The authors observe that the size of the MOSFET five times larger than MP05 is more than enough to achieve good attenuation.

### III. PROPOSED RAIL-TO-RAIL CLASS-AB CMOS BUFFER

We applied the bulk-driven super source follower as shown in Figure 2b in our design to propose a rail-to-rail power-efficient CMOS voltage buffer. Figure 3 illustrates the circuit diagram of our proposal.

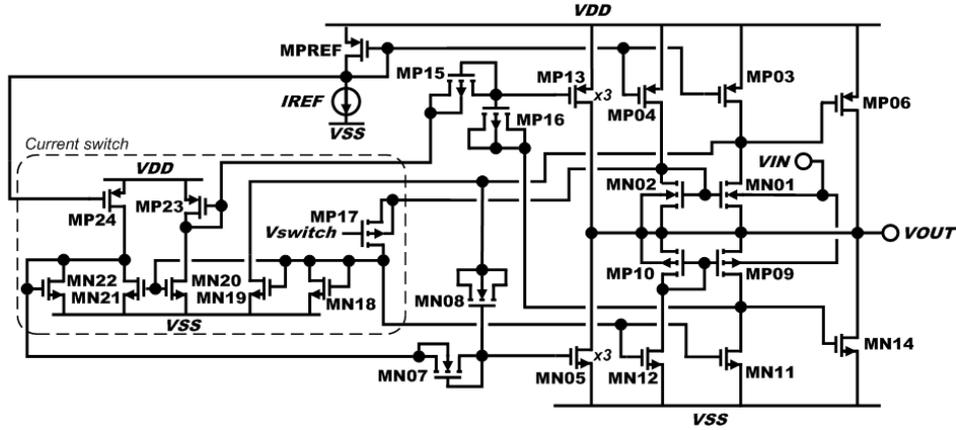


Figure 3. Proposed class-AB rail-to-rail CMOS analog buffer using a complementary pair of bulk-driven super source followers

The operation principle of Figure 3 is very simple to follow. From MN01 to MN08 and from MP09 to MP16 form a nMOS-type and pMOS-type of the bulk-driven super source follower, respectively, and from MP17 to MP24 forms a current switch. The  $V_{switch}$  at the gate of MP17 determines the switching point between the two types of follower. When  $V_{IN}$  (and thus  $V_{OUT}$ ) is close to  $V_{SS}$  the pMOS follower is active while the nMOS follower is off, and when  $V_{IN}$  moves towards  $V_{DD}$ ,  $V_{OUT}$  and the drain voltage of MN02 also increase and eventually MP17 turns on to reduce the drain current of MN01, MN02 and MN05 (i.e. to shut off the nMOS follower) and instead to increase the drain current of MP09, MP10 and MP13 (i.e. to activate the pMOS follower) to continue the buffer operation.

#### IV. SIMULATED RESULTS

Using a  $0.35\mu\text{m}$  CMOS process, we designed to operate the circuit of Figure 3 at 1.8V supply voltage and simulated with the BSIM3 MOSFET models. Table 1 shows the simulation results summarizing the overall performance.

TABLE I. SIMULATED RESULTS OF THE OVERALL PERFORMANCE OF FIGURE 3

| Parameter                  | Simulated Results  |
|----------------------------|--|
| -3dB frequency             | 6MHz   |
| Static current dissipation | $5\mu\text{A}$ to $8\mu\text{A}$ for $V_{IN}$ sweeping between $V_{DD}$ and $V_{SS}$   |
| Slew rate                  | $\text{SR}^+ = 9.3\text{V}/\mu\text{s}$ , $\text{SR}^- = 13.7\text{V}/\mu\text{s}$   |
| Input capacitance          | 17fF   |
| THD                        | -52dB (1.6Vpp@100kHz, $\text{CL} = 10\text{pF}$ )<br>-50dB (1.6Vpp@100kHz, $\text{CL} = 22\text{pF}$ )<br>-47dB (1.6Vpp@100kHz, $\text{CL} = 47\text{pF}$ )<br>-46dB (1.6Vpp@100kHz, $\text{CL} = 68\text{pF}$ ) |
| Simulated condition:       | $V_{DD} = 1.8\text{V}$ , $V_{SS} = 0\text{V}$ , $V_{SW} = 0.9\text{V}$ , $\text{CL} = 10\text{pF}$   |

From Table 1 we emphasize that the proposed buffer of Figure 2 meets the demands we discussed in the Introduction. The input capacitance is as small as 17fF, the SR is very high such that the buffer can deliver a 1.6Vpp 100kHz signal with a

total harmonic distortion as low as -46dB when the capacitive load is as large as 68pF, whilst the static current consumption remains under  $8\mu\text{A}$ . Figure 4 is the simulated results of DC-sweeping the  $V_{IN}$ , which indicates that the offset remains small throughout the rail-to-rail operation.

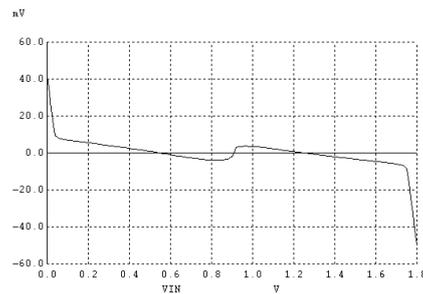


Figure 4. Simulated results of the DC offset voltage versus  $V_{IN}$  ( $V_{DD} = 1.8\text{V}$ ,  $V_{SS} = 0\text{V}$ ,  $V_{switch} = 0.9\text{V}$ )

Fig 5 indicates the simulated results of the static current dissipation with DC sweeping the  $V_{IN}$  between  $V_{DD}$  and  $V_{SS}$ .

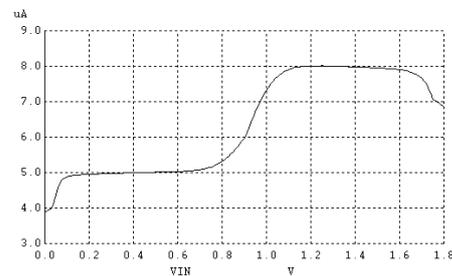


Figure 5. Simulated results of the static current dissipation ( $V_{DD} = 1.8\text{V}$ ,  $V_{SS} = 0\text{V}$ ,  $V_{switch} = 0.9\text{V}$ )

Figure 6 illustrates the simulated results of the  $V_{OUT}$  and the  $I_{OUT}$  with  $V_{IN}$  having 1.6V peak-to-peak 100kHz sine wave signal and a capacitive load CL of 68pF.

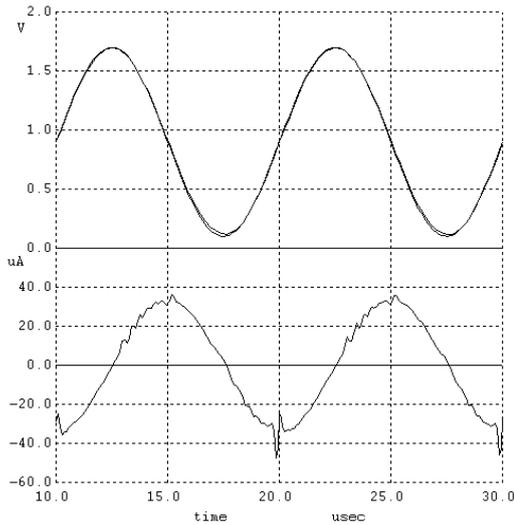


Figure 6.  $V_{OUT}$  vs  $V_{IN}$  and  $I_{OUT}$  with  $V_{IN} = 1.6\text{Vpp}$  100kHz sine wave and  $CL = 68\text{pF}$  ( $V_{DD} = 1.8\text{V}$ ,  $V_{SS} = 0\text{V}$ ,  $V_{switch} = 0.9\text{V}$ )

Figure 5 and Figure 6 show clearly that the goal of excellent power efficiency is achieved – during the static mode the current dissipation of the proposed buffer remains under  $8\mu\text{A}$ , whereas  $I_{OUT}$  can be pushed and pulled to approximately  $\pm 40\mu\text{A}$  during the dynamic  $V_{IN}$  so that the Total Harmonic Distortion (THD) of  $V_{OUT}$  can be as small as  $-46\text{dB}$  even the CL is as large as  $68\text{pF}$ .

To verify the input capacitance of the proposed buffer shown in Figure 3, we have set up the simulation condition as shown in Figure 7.

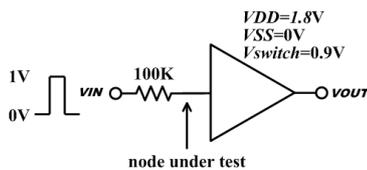


Figure 7. Simulation setup for the input capacitance

The simulated plot of the setup in Figure 7 is given in Figure 8.

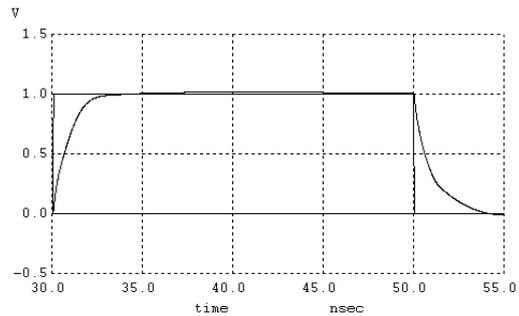


Figure 8. Simulation results for the Figure 7 setup

From Figure 8, the time constant  $\tau$  was found to be  $1.7\text{ns}$ . Hence, the input capacitance was determined as  $17\text{fF}$  ( $\tau = RC$ ).

## V. CONCLUSION

A new design technique for a CMOS buffer using the complementary pair of bulk-driven super followers has been presented. Applying the bulk-driven MOSFETs with the replica-biased scheme and the QFG techniques into the buffer enabled us to have a few femto-Farad range of the input capacitance so that the weak input signals are minimally affected, whilst delivering the signal without much distortion even if the capacitive load is very large. The static current consumption can remain small too. Our proposed buffer can become a serious contender for portable electronics needing to deliver weak analogue signals into large capacitive loads with as little distortion as possible.

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# Bulk-Driven Flipped Voltage Differential Pair

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**Abstract**— This paper explores a new design approach of a low-power high slew rate CMOS voltage buffer. The buffer is based on the Flipped Voltage Follower Pseudo Differential Pair, but the bulk-driven technique is utilized at the input stage to achieve rail-to-rail operation. This buffer has been designed for a 0.35 $\mu\text{m}$  CMOS technology to operate at a 1.8V supply voltage. The BSIM3 simulated results are provided which demonstrate the open-loop gain of 50dB, gain bandwidth of 3MHz with a 5pF load, whereas the total static current consumption remains below 9 $\mu\text{A}$ . This paper also addresses the issue of latch-up problem that occurs with a large step input.

## I. INTRODUCTION

Lowering of the supply voltage and the current consumption in portable electronics has been a top priority for many years, as it helps reducing the number of battery cells so that the product can be produced more compact and light. In digital circuits, lower supply voltage also leads to reduction of dynamic power consumption.

In analog circuits, particularly voltage buffers which play an essential role in analog and mixed-signal circuits, lowering the supply voltage brings a challenge in achieving acceptable dynamic range. To overcome this issue, rail-to-rail input stage would have to be adopted in the voltage buffer designs. Furthermore, lowering the static current consumption of voltage buffers causes less capability in driving large capacitive load at high speed.

There is a published proposal of a differential pair so-called Flipped Voltage Follower Pseudo Differential Pair (FVFDP) [1], which achieves high drive capability low static current consumption. Figure 1(a) and 1(b) illustrates the transistor realization of the FVFDP, and the simulated plot with  $I_B$  set to 1 $\mu\text{A}$  using a 0.35 $\mu\text{m}$  CMOS process.

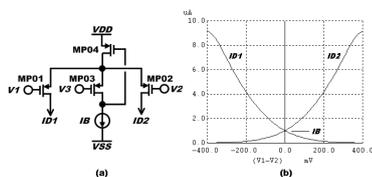


Figure 1. (a) pMOS FVFDP [1] and (b) simulating the DC transfer characteristics using a 0.35 $\mu\text{m}$  CMOS process

In Figure 1(a),  $V_1$  and  $V_2$  are the differential input, and  $V_3$  is the common-mode voltage of  $V_1$  and  $V_2$ , i.e.  $(V_1+V_2)/2$ . As can be observed from Figure 1(b), when no differential signal is applied (i.e.  $V_1=V_2=V_3$ , steady condition) the drain current of MP01 and MP02 ( $I_{D1}$  and  $I_{D2}$ ) become equal to  $I_B$ , and when the differential signals are applied then  $I_{D1}$  and  $I_{D2}$  can become much larger than the twice of  $I_B$ . This low-static high-dynamic performance is not possible to achieve with the conventional differential pair.

In this paper, we present a design of a CMOS voltage buffer using the FVFDP but with the bulk-driven technique [2] applied at the input stage, so that rail-to-rail low-power high-driving performances can be all achieved.

## II. BULK-DRIVEN MOSFET WITH DIODE

This section discusses utilization of a reverse-biased diode with the bulk-driven MOSFET, as the CMOS voltage buffer proposed in this paper is based on this technique. Figure 2(a) and 2(b) illustrate the circuit diagram of a bulk-driven pMOS connected with the reverse-biased diode, and a sketch of a diode realized in CMOS technology.

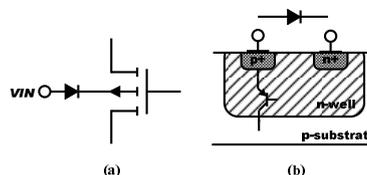


Figure 2. (a) bulk-driven pMOS with reversed-biased diode, and (b) diode in CMOS technology

Figure 4 shows the simulated plot of the DC sweep analysis of Figure 2(a) using a 0.35  $\mu\text{m}$  CMOS process, where the transistor width and length are 2 $\mu\text{m}$  and 1.4 $\mu\text{m}$ , and source, drain, and gate voltages of the pMOS are fixed at 0V, -0.2V, and -0.8V respectively. For the diode the minimum size is used. As can be observed from the plot, only a few pico-ampere of the DC input current  $I_{IN}$  flows at any operation point of the input voltage  $V_{IN}$ , since the body-diode of the pMOS and the added diode are in reverse connected to each other and thus only the leakage current passes through. Consequently, the source-to-bulk voltage

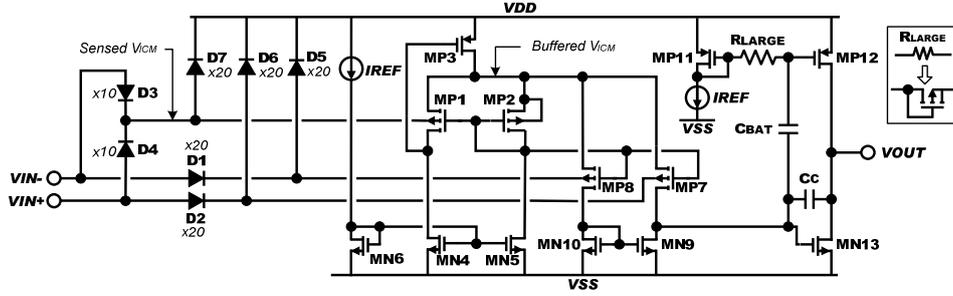


Figure 3. Proposed CMOS buffer using Bulk-Driven Flipped Voltage Differential Pair

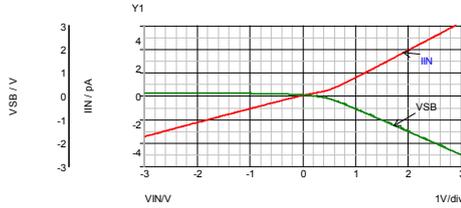


Figure 4. Simulated  $I_{IN}$  and  $V_{SB}$  of Figure 2(a)

$V_{SB}$  of the PMOS does not become strongly forward-biased since the forward current of the diode is extremely small. It is worth noting that the added diode does not become strongly forward-biased either, so that the parasitic vertical bipolar illustrated in Figure 2(b) remains off.

Interestingly, with Figure 2(a) the input is fed into p+ implant, whereas it would have been n+ implant for a conventional bulk-driven MOSFET. This means that the input indirectly sees the pn-junction (from n-well to p-substrate), and thus the effective input capacitance can be significantly reduced.

### III. OPERATION PRINCIPLE OF THE PROPOSED BUFFER

Based on the analysis shown in the previous section, we propose a CMOS voltage buffer using a new design technique which we named as Bulk-Driven Flipped Voltage Differential Pair (BDFVDP). Figure 3 illustrates the circuit diagram of the proposal.

The operation principle of the circuit in Figure 3 is simple to follow. From MP1 to MN5 form a circuit block called Bulk-Driven Flipped Voltage Follower (BDFVF) [3]. MP1 and MP2 are equally sized and biased with identical drain current with MN4 and MN5. Since the bulk-terminal of MP2 is physically shorted to the coupled source node (i.e.  $V_{SB2}=0$ ), MP1 becomes the replica of MP2, and hence the source-to-bulk voltage of MP1 becomes virtually shorted (i.e.  $V_{SB1}\approx 0$ ). In another words, the coupled source voltage follows the bulk input voltage of MP1. If MP3 is sized wide

enough such that it is in linear region, then the coupled source node becomes low impedance and hence it becomes the buffered signal of the bulk input of MP1. In the design of the proposed buffer, BDFVF is utilized to buffer the common-mode signal of the differential input  $V_{ICM}$ .

From MP7 to MN10 forms the first stage of the operational amplifier. The input devices of this stage are bulk-driven, and when the differential signals  $V_{IN+}$  and  $V_{IN-}$  are in identical then the drain current of the input devices,  $I_{D7}$  and  $I_{D8}$ , settle to the bias current  $I_{REF}$ . When large differential signals are applied, then  $i_{D7}$  and  $i_{D8}$  can become much greater than twice the current of  $I_{REF}$ , since the coupled source node has very low impedance and MP3 can supply a source current that is bigger than  $2 \times I_{REF}$ .

From MP11 to MN13 forms the second stage of the operational amplifier, which has been converted to class-AB operation using the Quasi-Floating Gate (QFG) technique [4]. As can be observed, the gate of MP12 is connected to the gate of MP11 with a large resistor  $R_{LARGE}$ , and also to the gate of MN9 with a capacitor  $C_{BAT}$ . In terms of DC characteristics, there exists no current flow across  $R_{LARGE}$  and therefore the gate voltage of MP12 and MP11 are the same, and thus the static drain current  $I_{D12}$  is  $I_{REF}$ . In terms of AC characteristics, a high pass filter is formed at the gate of MP12 with a cutoff frequency of  $1/(2\pi R_{LARGE} C_{BAT})$ , and therefore MP12 achieves not only static but also dynamic operation, which in turn leads to class-AB operation. It is remarkable to realize that a unity-size diode-connected MOSFET but in the cutoff region can form a substantially large resistance of  $R_{LARGE}$ , thus a low cutoff frequency can be achieved with a moderately small capacitance of  $C_{BAT}$ .

From D1 to D4 are the reverse-biased diodes to the bulk-driven devices. D3 and D4 are used to detect for  $V_{ICM}$ . In Figure 3, those diodes have been sized to 20 times of the minimum size of the diode for D1 and D2, and 10 times for D3 and D4, to prevent from further reduction of the transconductance as possible. The transconductance of a bulk-driven MOSFET with the reverse-biased diode  $g_{mb,VR}$  can be expressed as:

$$g_{mb\_VR} = \alpha g_{mb} \quad (1)$$

where  $\alpha$  is the attenuation factor of the signal and  $g_{mb}$  is the transconductance of the bulk-driven MOSFET.  $\alpha$  can be expressed as:

$$\alpha = C_{DIODE} / (C_{DIODE} + C_{SB}) \quad (2)$$

where  $C_{DIODE}$  is the junction capacitance of the reverse-biased diode, and  $C_{SB}$  is the source-to-bulk capacitance of the MOSFET.  $C_{DIODE}$  given by

$$C_{DIODE} = C_{J0\_DIODE} / (1 + V_R / \phi_0)^{0.5} \quad (3)$$

where  $C_{J0\_DIODE}$  is the zero-biased junction capacitance of the reverse-biased diode,  $V_R$  is the reversed-biased DC voltage, and  $\phi_0$  is the built-in bulk junction potential. Similarly,

$$C_{SB} = C_{J0\_MOSFET} / (1 + V_{SB} / \phi_0)^{0.5} \quad (4)$$

where  $C_{J0\_MOSFET}$  is the zero-biased junction capacitance of the MOSFET, and  $V_{SB}$  is the source-to-bulk DC voltage.

From D5 to D7 are the protection diodes to prevent latch up when a large step input is applied. The effectiveness of these diodes will be described in the next section.

#### IV. SIMULATED RESULTS

To verify the proposed solution of Figure 3, we designed it using a 0.35 $\mu$ m CMOS process to operate with a 1.8V supply voltage. This section provides simulated results using the BSIM3 MOSFET models.

##### A. DC-Sweep Analysis

This subsection provides the simulation results of the DC-sweep analysis. Figure 3 has been setup in a unity-gain configuration with a 1.8V supply voltage, and the input voltage  $V_{IN}$  is swept from rail to rail. Figure 5 shows the simulated behavior of the source-to-bulk voltage of the bulk-driven device MP7  $V_{SB7}$  and the potential difference between the output  $V_{OUT}$  and  $V_{IN}$ .

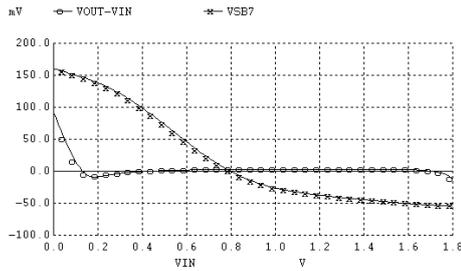


Figure 5. Simulated  $V_{OUT} - V_{IN}$  and  $V_{SB7}$  of Figure 3 in unity-gain configuration

As can be noticed from Figure 5,  $V_{SB7}$  does not become strongly forward biased which indicates that latch up does

not occur, and  $V_{OUT} - V_{IN}$  remains small which confirms that the proposed buffer is operational in rail-to-rail.

Figure 6 is the simulated plot of the input DC current  $I_{IN}$  of the same setup. It indicates that only  $\pm 30$  pA of DC current flows from rail to rail, suggesting that the input resistance would be as large as 30G $\Omega$ . This superior result is expected since the diodes are connected in reverse-bias to the body-diode of the MOSFET.

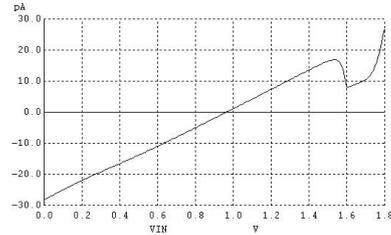


Figure 6. Simulated  $I_{IN}$  of Figure 3 in unity-gain configuration

##### B. Transient Analysis

This subsection provides the simulation results of the DC-sweep analysis. Figure 3 has been setup in a unity-gain configuration with a 1.8V supply voltage and a capacitive load of 5pF, and a step input from 0.2V to 1.6V and vice versa is applied. Figure 7 is the simulated plot of the input voltage  $v_{IN}$ , the output slew rate  $v_{OUT}$ , and the transient behavior of the source-to-bulk voltage of the bulk-driven device MP7,  $v_{SB7}$ . The key observation of Figure 7 is the  $v_{SB7}$  behavior when a large step-down input is applied. Appreciating to the protection capability of the diodes from D5 to D7,  $v_{SB7}$  does not even instantaneously become forward biased by more than 0.3V and therefore the latch up problem has been prevented.



Figure 7. Simulated  $v_{SB7}$  and slew rate of  $v_{OUT}$  of Figure 3 in unity-gain configuration with  $CL=5$ pF ( $v_{IN}$  stepping between 0.2V and 1.6V)

Figure 8 is the simulated transient analysis plot of the input and output instantaneous current,  $i_{IN}$  and  $i_{OUT}$ , indicating that  $i_{IN}$  never achieves more than 1 $\mu$ A and  $i_{OUT}$  current reaches over 20 $\mu$ A. This suggests that the  $i_{IN}$  would always be in the nano-ampere range for an AC input slower than the Gain-Bandwidth (GBW), which proves the effectiveness of the proposed buffer. This low  $i_{IN}$  has been

achieved because the well-to-substrate capacitance is indirectly seen by the input and also the effective input capacitance has been lowered by the attenuation factor  $\alpha$ .

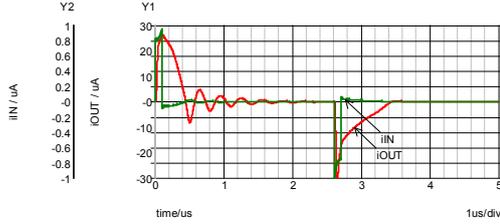


Figure 8. Simulated  $i_{IN}$  and  $i_{OUT}$  of Figure 4 in unity-gain configuration with  $CL=5pF$  ( $V_{IN}$  stepping between 0.2V and 1.6V)

### C. Observation

To further observe our proposal of Figure 3, we designed another CMOS buffer as shown in Figure 9 for comparison purposes. This circuit block is the gate-driven type of Figure 4, and all transistors are sized identical to Figure 3. Table I shows the summary of the overall performance of the two circuit blocks.

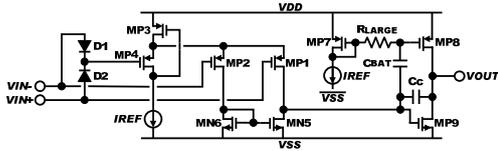


Figure 9. Gate-driven Flipped Voltage Differential Pair

As expected, the open-loop gain  $A_{OL}$  and the GBW of the bulk-driven one is smaller and slower in comparison to the gate-driven one due to reduced transconductance of the input device, however  $A_{OL}=50dB$  GBW (at  $CL=5pF$ ) = 3MHz is relatively efficient for the total static current consumption of only  $9\mu A$ . It is important to realize that the input referred noise of Figure 4 is moderately independent to the input condition since no transistors change the operation region. This property suggests that the single-pair approach is worthy of further improving than the double-pair approach which changes the operation region.

On the other hand, there are two significant drawbacks with our proposal. One is that the  $A_{OL}$  is not constant to  $V_{ICM}$ , where the dominant root cause is that  $\alpha$  in Equation (1) varies significantly with the reverse voltage of the diode. The other drawback is that the Power Supply Rejection Ratio (PSRR) is substantially deteriorated, possibly due to the fact that the protection diodes D5 – D7 are directly propagating the supply noise towards the differential signal. Currently we are investigating these drawbacks to improve performances.

TABLE I. SIMULATED RESULTS OF THE OVERALL PERFORMANCE

| Parameter  | Simulated results  |   |
|--|--|---|
|  | Figure 9   | Figure 4  |
| Open-loop gain $A_{OL}$  | 60dB   | 50dB  |
| Gain bandwidth (GBW) at $CL=5pF$   | 9MHz   | 3MHz  |
| Total static current consumption $I_{CC}$  | $7\mu A$   | $9\mu A$  |
| Power Supply Rejection Ratio (PSRR)  | PSRR+=75dB<br>PSRR-=56dB   | PSRR+=26dB<br>PSRR-=37dB  |
| Slew Rate (SR) at $CL=5pF$   | SR+=5.2V/ $\mu s$<br>SR-=7V/ $\mu s$                             | SR+=5.2V/ $\mu s$<br>SR-=2.3V/ $\mu s$                          |
| Input referred noise   |  |   |
| $V_{IN}=VDD$   | 1/f @1kHz: 230mV/ $\sqrt{Hz}$<br>Wideband: 70 $\mu V/\sqrt{Hz}$  | 1/f @1kHz: 11 $\mu V/\sqrt{Hz}$<br>Wideband: 600nV/ $\sqrt{Hz}$ |
| $V_{IN}=0.9V$  | 1/f @1kHz: 9 $\mu V/\sqrt{Hz}$<br>Wideband: 600nV/ $\sqrt{Hz}$   | 1/f @1kHz: 15 $\mu V/\sqrt{Hz}$<br>Wideband: 600nV/ $\sqrt{Hz}$ |
| $V_{IN}=VSS$   | 1/f @1kHz: 1.5 $\mu V/\sqrt{Hz}$<br>Wideband: 100nV/ $\sqrt{Hz}$ | 1/f @1kHz: 22 $\mu V/\sqrt{Hz}$<br>Wideband: 600nV/ $\sqrt{Hz}$ |
| Total Harmonic Distortion ( $A_{CL}=1$ , 1.4Vpp sinewave)                                    |  |   |
| CL=5pF @100kHz   | Not possible   | -40dB   |
| CL=10pF @100kHz  |  | -33dB   |
| CL=5pF @200kHz   |  | -33dB   |
| CL=5pF @300kHz   |  | -27dB   |
| Unless stated, the set up condition is:<br>$VDD=1.8V$ , $VSS=0V$ , $V_{IN}=0.9V$ , $C_L=5pF$ |  |   |

### V. CONCLUSION

A new low power consumption high-speed CMOS buffer has been proposed. The new circuit block consists of a FVFDP and a QFG type of class-AB second stage, which delivers high-speed at 3MHz GBW operation for a 5pF load whilst maintaining the static current consumption as small as  $9\mu A$ . This paper also addresses the latch up problem by having reverse-bias connected diodes to the body diode of the bulk-driven MOSFET, so that only the diode's leakage current flows and forward biasing of the diodes can be prevented. Our proposed buffer has proven to be very power-efficient, and is motivating to work on for further improvement.

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# Bulk-Driven DC Level Shifter

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**Abstract**—A new CMOS DC level shifter that can be programmed at a level less than the threshold voltage of a MOSFET is proposed. This design technique utilizes a bulk-driven MOSFET, which is biased with a constant reverse voltage, to shift the input. Furthermore since the proposed block is in a class-AB super source follower form, it is power-efficient. This paper presents the design and the simulation of the proposed block and also its application in a simple current mirror using a 0.35 $\mu\text{m}$  CMOS process, which indicates leading to the reduction of the voltage headroom consumption of the input device but without introducing DC offset current, while the additional distortion remain negligible until 1MHz operation. The additional static current consumption is as small as 5 $\mu\text{A}$ .

## I. INTRODUCTION

Designing analog circuits that can operate from a low battery voltage is a challenge especially when one tries to avoid introducing performance drawbacks. Common building blocks such as current mirrors, which are widely used for biasing and as active loads in amplifiers, are no exception. To utilize current mirrors under the limited supply voltage available, designers must firstly confront the large voltage headroom consumed at the input device. One popular approach that can overcome this problem is by utilizing a DC level shifter in-between the drain and the gate of the input device [1-3]. Fig. 1 shows a couple of examples of CMOS circuit diagrams to describe this approach.

Fig. 1(a) and (b) depict a simple nMOS current mirror and utilization of a DC level shifter, respectively, and Fig. 1(c) shows the simulated results of the two blocks using the BSIM3 MOSFET models of a 0.35 $\mu\text{m}$  CMOS process. From Fig. 1(c), it is clear that a significant offset in the DC current is observed for Fig. 1(b). This is because the circuit block formed by MP3 and  $I_B$  generates a DC level shift upward by more than the threshold voltage of MP3 and causes MN1 to leave the saturated region and enter into the linear region. To avoid this undesirable side effect, a DC level shifter that can be programmed to operate at a level less than the threshold voltage of a MOSFET is rather in favor of the novel technique, which to the best knowledge of the authors has not been reported in any open literature of today's circuit design techniques.

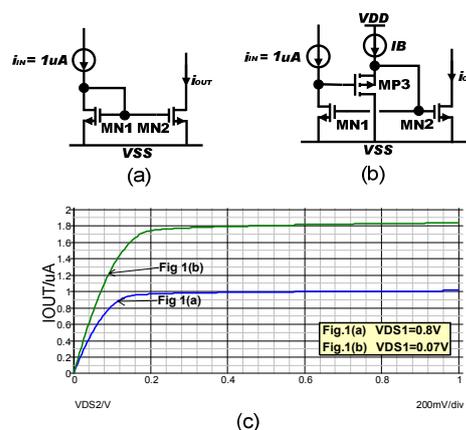


Figure 1. (a) Simple current mirror with  $I_{in} = 1\mu\text{A}$ , (b) with a DC level shifter, and (c) the  $V_{DS2}$  DC-sweep simulated results

In this paper we present a novel CMOS DC level shifter for which the constant DC voltage can be easily programmed to a level less than the threshold voltage of a MOSFET.

## II. PREVIOUS ESSENTIAL WORKS

This section covers a brief review of the two essential design techniques, known as the Bulk-Driven Super Source Follower (BDSSF) [4] and the Quasi Floating Gate (QFG) technique [5-6], which we have utilized to come up with our novel proposal.

### A. Bulk-Driven Super Source Follower (BDSSF)

Fig. 2(a) illustrates the circuit diagram of the BDSSF, which we have proposed this circuit design technique in [4] that can eliminate the DC level shift of a super source follower lectured in the literature of [7].

The operation principle of the BDSSF of Fig. 2(a) is simple to follow. MP01 is the input device, which its bulk is utilized to feed the input. MP02 and MN05 are the replica devices for MP01 and MN04 respectively. Note that the bulk

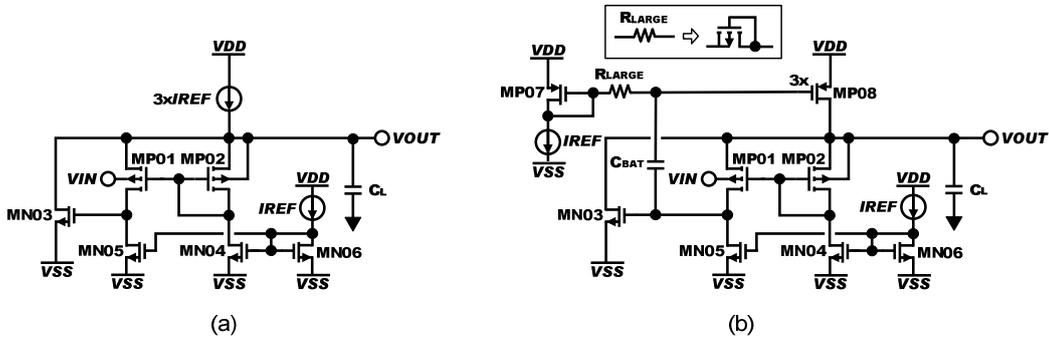


Figure 2. (a) class-A and (b) class-AB of BDSSF

of MP02 is physically shorted to its source, which is the output node. Since the gate of MP01 is biased with the diode-connected MP02, as well as the drain current of MP01 and MP02 are equally set to  $I_{REF}$ ,  $V_B$  and  $V_S$  of MP01 becomes virtually shorted (i.e.  $V_{BSMP01} = 0$ ), and in effect the output voltage  $V_{OUT}$  becomes equal to  $V_{IN}$ .

### B. Quasi Floating Gate (QFG) Technique

The BDSSF of Fig. 2(a) works well, however, since it is class-A type there is a limitation in its source capability to  $I_{REF}$ , which leads to poor push capability in driving large loads at high speed. To overcome this problem, a circuit design technique proposed by [5] and [6], which is known as QFG, can be utilized to convert the BDSSF of Fig. 2(a) into class-AB operation. Fig. 2(b) illustrates the circuit diagram of a class-AB BDSSF.

The QFG technique utilizes  $R_{LARGE}$  and  $C_{BAT}$  to form a high pass filter, so that the AC element of the gate signal of the sink device MN03 can be propagated to drive the source device MP08 and therefore push capability can be expanded.

The significance of this technique is that a unity-size (i.e. the smallest size for the process) diode-connected MOSFET in the cut-off region can form a substantially large resistance  $R_{LARGE}$ , and hence a moderately small capacitance  $C_{BAT}$  will suffice to achieve a low cut-off frequency  $1/(2\pi R_{LARGE}C_{BAT})$ . In [6], the authors discuss the capacitance of  $C_{BAT}$  in terms of attenuation factor  $\alpha$  ( $\approx 1/(1+C_{SG8}/C_{BAT})$ ), where  $C_{SG8}$  is the source-to-gate capacitance of MP08. The capacitance of  $C_{BAT}$  greater than 5 times  $C_{SG8}$  leads  $\alpha > 0.83$ , which is enough to propagate almost all frequencies except the DC component of the signal. It is remarkable to realize that the DC performance of the circuits in Fig. 2(a) and (b) are exactly identical, i.e. to emphasize further, the QFG technique can convert from class-A to class-AB operation without introducing any extra static current consumption.

## III. PROPOSAL

The design objective for this paper, which is to have a constant DC level shift less than the threshold voltage of a

MOSFET, is simple to achieve by utilizing the BDSSF of Fig. 2(a) and (b). The source to bulk terminal of MP01,  $V_{SB1}$ , becomes reverse-biased by having a wider transistor width for MP01 and/or reducing its drain current  $I_{DS1}$ . The operation principle can be understood using the conventional square law model of a MOSFET. Whether the transistor size or the drain current of MP01 changes, this device maintains as the replica of MP02 and thus it operates in the saturated region. Let's suppose that MP01 is sized to have a relatively long length to minimize the effect of the channel length modulation, so that its drain current  $I_{DS1}$  can be approximated by:

$$I_{DS1} = (\mu_p C_{OX}/2) (W_1/L_1) (V_{SG1} - V_{T1})^2 \quad (1)$$

where  $\mu_p$  is the surface mobility of the pMOS transistor,  $C_{OX}$  is the capacitance of the gate oxide,  $W_1$ ,  $L_1$ ,  $V_{SG1}$ ,  $V_{T1}$  are the width, the length, the source-to-gate voltage, and the threshold voltage of MP01, respectively. If for instance  $W_1$  is increased and/or  $I_{DS1}$  is decreased, then the overdrive voltage  $V_{SG1} - V_{T1}$  needs to be decreased to satisfy the above equation. However, since  $V_{SG1}$ , which is identical to the source-to-gate voltage of MP02, remains unchanged,  $V_{T1}$  needs to be increased.  $V_{T1}$  can be expressed by:

$$V_{T1} = V_{T0} + \gamma \{ (2|\Phi_F| + V_{SB1})^{0.5} - (2|\Phi_F|)^{0.5} \} \quad (2)$$

where  $V_{T0}$  is the zero-bias threshold voltage,  $\gamma$  is the body effect parameter,  $|\Phi_F|$  is the Fermi potential, and  $V_{SB1}$  is the source-to-bulk voltage of MP01. As can be realized from this equation, to increase  $V_{T1}$ ,  $V_{SB1}$  needs to be increased. Thus in summary, increasing  $W_1$  and/or decreasing  $I_{DS1}$  makes MP01 propagate a constant shift down voltage from the input to the output. Fig. 3 shows the simulated parametric sweep analysis of the width of MP01 and the length of MN05, denoted by  $W_1$  and  $L_5$ , respectively (please note for clarification that the x-axis units are in  $\mu m$  and the y-axis ones in mV).

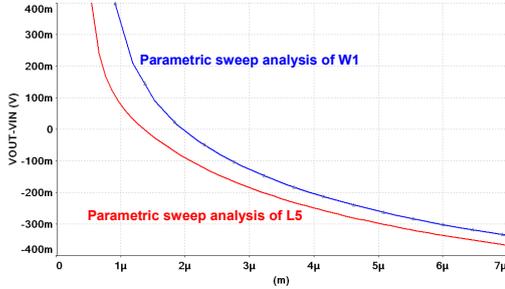


Figure 3. Parametric sweep simulation of Fig. 2(a) and (b)

It is worth noting from Fig. 3 that it is in theory feasible to level shift the input voltage upward as well as downward using the BDSSF of Fig. 2(a) and (b), however from the view point of the effective input capacitance the authors recommend keeping the bulk-driven device MP01 in reverse biased operation. The description of the reverse biased junction capacitance, which is also known as the depletion capacitance  $C_j$ , as given in [8] utilizes the following model:

$$C_j = C_{j0} / (1 + (V_{SB}/\phi_0))^{0.5} \quad (3)$$

where  $C_{j0}$  is the zero-bias ( $V_{SB}=0$ ) junction capacitance,  $V_{SB}$  is the bulk-to-source voltage, and  $\phi_0$  is the bulk junction potential. However, if the bulk of MP01 is in forward biased operation, then another capacitance model called the diffusion capacitance  $C_d$  would be introduced, which can be expressed by:

$$C_d = \tau_T (I_D/V_T) \quad (4)$$

where  $\tau_T$  is the transit time of the junction diode,  $I_D$  is the amount of current through the diode, and  $V_T$  is the thermal voltage ( $\approx 26\text{mV}$  at room temperature). Thus in the results for the forward biased operation of the bulk-driven device, the total input capacitance  $C_T$  would then be expressed as:

$$C_T = C_j + C_d \quad (5)$$

Therefore, in order to avoid introducing the diffusion capacitance at the input, the authors recommend using the proposed level shifter by configuring the bulk-driven device in reverse bias operation, i.e. using Fig. 2(b) to shift down the voltage. For shifting up operation, the authors recommend the use of an nMOS bulk-driven transistor for the input device.

#### IV. SIMULATED RESULTS

Table I shows the simulated results of Fig. 2(b) using the BSIM3 MOSFET models of a  $0.35\mu\text{m}$  CMOS process. To see how different level shift settings and design approaches

affect the overall performances, we designed several BDSSF blocks of Fig. 2(b) for comparison. The overall performance of the BDSSF blocks with 0-volt DC shift, 0.3-volt DC shift down achieved by increasing  $I_{DS1}$ , 0.3-volt DC shift down achieved by decreasing  $I_{DS1}$ , 0.6-volt DC shift effected by modifying both  $W1$  and  $I_{DS1}$  are summarized in Table I.

| Parameter   | Vshift =0V | Vshift =0.3V* | Vshift =0.3V** | Vshift =0.6V |
|---|------------|---------------|----------------|--------------|
| -3dB frequency  | 6.5MHz     | 8MHz          | 4.5MHz         | 5.5MHz       |
| Total current consumption   | 5.2μA      | 5.2μA         | 5.2μA          | 5.2μA        |
| Slew Rate+  | 2.0V/μs    | 2.1V/μs       | 2.1V/μs        | 2.2V/μs      |
| Slew Rate-  | 6.2V/μs    | 5.3V/μs       | 5.0V/μs        | 5.5V/μs      |
| Power Supply Rejection Ratio  | 53dB       | 55dB          | 62dB           | 62dB         |
| 1/f noise at 1kHz   | 3.7μV/√Hz  | 3.7μV/√Hz     | 3.8μV/√Hz      | 4.0μV/√Hz    |
| Total Harmonic Distortion:  |            |               |                |              |
| 0.8Vpp 100kHz   |            |               |                |              |
| CL=10pF   | -67.7dB    | -66.6dB       | -67.1dB        | -63.6dB      |
| CL=22pF   | -62.0dB    | -62.5dB       | -64.1dB        | -61.7dB      |
| CL=47pF   | -55.0dB    | -56.7dB       | -59.7dB        | -58.6dB      |
| 0.8Vpp 500kHz   |            |               |                |              |
| CL=10pF   | -51.6dB    | -53.4dB       | -48.1dB        | -50.1dB      |
| 0.8Vpp 1MHz   |            |               |                |              |
| CL=10pF   | -35.4dB    | -38.8dB       | -31.5dB        | -34.4dB      |
| * $W1=3W2$ , $L5=L6$ ** $W1=W2$ , $L5=3.5L6$  |            |               |                |              |
| Unless stated, the setup condition is as follows:<br>$VDD=3.3V$ , $VSS=0V$ , $VIN=2.5V$ , $CL=10pF$ |            |               |                |              |

TABLE I. SIMULATED RESULTS OF THE OVERALL PERFORMANCE OF FIG. 2(B) WITH DIFFERENT LEVEL SHIFT CONFIGURATIONS

The simulated results for the circuit of Fig. 2(b) where the DC level shift is adjusted to 0.3V downward by modifying  $W1$ , and the input signal of 0.8Vpp at 100kHz is applied to the circuit with a load capacitance  $C_L$  of 10pF is as shown in Fig. 4.

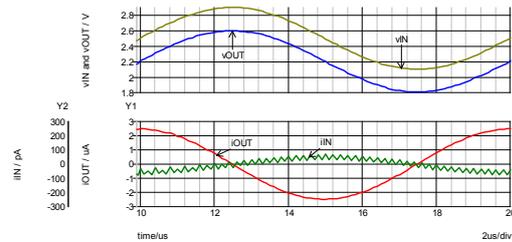


Figure 4. Simulated results of Fig. 2(b) with  $W1=3W2$  and  $I_{DS1}=I_{DS2}$ , where  $v_{IN} = 0.8\text{Vpp}$ , 100kHz sinusoidal wave and  $C_L$  with 10pF

As can be observed from Fig. 4, the input current of only  $\pm 70\text{pA}$  is necessary to apply a 0.8Vpp 100kHz sinusoidal input voltage. It is worth remembering that this low input current would not have been possible to achieve if the bulk-driven input device MP01 was in the forward biased operation due to the significant increase in its input capacitance.

## V. APPLICATION EXAMPLE

As described in the Introduction of this paper, a DC level shifter applied in a current mirror can be useful in reducing the voltage headroom consumption of the input device. Fig. 5(a) illustrates the BDSSF of Fig. 2(b) applied in a simple pMOS current mirror. RC and CC have been added between the input and the output of the BDSSF to minimize the output overshoot against the transient input signal. Given that  $V_{T0}$  of the pMOS transistor for the  $0.35\mu\text{m}$  CMOS process we have chosen is approximately  $0.6\text{V}$ , we redesigned the BDSSF of Fig. 2(b) with a DC shift down of  $0.2\text{V}$ ,  $0.5\text{V}$  and  $0.6\text{V}$  and applied it to the current mirror as shown in Fig. 5(a) to compare the overall performance. Fig. 5(b) and Table II shows the simulated plots of the step response and the summary of the simulation results of Fig. 5(a), respectively.

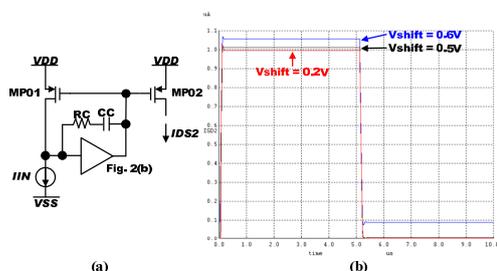


Figure 5. (a) A pMOS current mirror with level shifted BDSSF and (b) simulated plot of  $1\mu\text{A}$  step response

| Parameter  | Fig. 5(a) without Fig. 2(b) | Fig. 5(a) with $V_{\text{shift}} = 0.2\text{V}$ | Fig. 5(a) with $V_{\text{shift}} = 0.5\text{V}$ | Fig. 5(a) with $V_{\text{shift}} = 0.6\text{V}$ |
|--|-----------------------------|---|---|---|
| Static current consumption of Fig. 2(b)  | ---                         | $5.1\mu\text{A}$                                | $5.0\mu\text{A}$                                | $5.1\mu\text{A}$                                |
| -3dB frequency   | 90MHz                       | 70MHz   | 100MHz  | 100MHz  |
| THD $1\mu\text{A}_{\text{app}}$  |                             |   |   |   |
| 1MHz   | -53.3dB                     | -53.6dB   | -53.2dB   | -57.1dB   |
| 10MHz  | -41.3dB                     | -37.0dB   | -37.2dB   | -38.1dB   |
| Setup condition: $V_{DD}=1.8\text{V}$ , $V_{SS}=0\text{V}$ , $I_{IN}=1\mu\text{A}$ , $V_{D2}=V_{DD}-0.5\text{V}$ |                             |   |   |   |

TABLE II. SUMMARY OF THE SIMULATION RESULTS OF FIG. 5(A)

As can be observed from Table II, until  $1\text{MHz}$  operation none of the BDSSF adds distortion noticeably. However, as can be realized from Fig. 5(b) a caution is necessary to determine the amount of DC level shift. A DC level shift too close to  $V_{T0}$  would cause a noticeable offset in the DC current. In the case of the simulated plot of Fig. 5(b), when the level shift is almost identical to  $V_{T0}$  ( $=0.6\text{V}$ ) a DC offset current of approximately  $60\text{nA}$  and  $90\text{nA}$  is introduced when

the input current is  $1\mu\text{A}$  and  $0\mu\text{A}$ , respectively. Even though the level shift was approximately  $100\text{mV}$  below  $V_{T0}$  (i.e. when the level shift is set to approximately  $-0.5\text{V}$ ), the offset current of  $10\text{nA}$  and  $4\text{nA}$  is drawn when the input current is  $1\mu\text{A}$  and  $0\mu\text{A}$ , respectively. Therefore it is advisable not to set the DC level shift too close to  $V_{T0}$ .

## VI. CONCLUSION

A novel design approach for a DC level shifter that can be programmed to a level less than the threshold voltage of a MOSFET has been presented. This technique is based on utilizing the power efficient BDSSF, with the bulk-driven input device forced to be reverse-biased to generate the constant DC voltage. SPICE simulations of the proposed block set up in a current mirror demonstrated that until  $1\text{MHz}$  operation the proposed block does not introduce additional distortion, whilst the extra static current consumption spent is as little as  $5\mu\text{A}$ . This proposed block has been shown to be an excellent solution for reducing the voltage headroom consumption of a current mirror but without introducing DC offset current.

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## Appendix B Supplementary Information to Chapter 6

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This appendix lists the supplementary information of the work presented in Chapter

6. The followings are included in this appendix:

- SPICE code for simulating the input capacitance
- IC layout of the whole die
- Bonding diagram
- More snapshots of the microphotograph of the fabricated device
- Test board

### *B.1 SPICE Code for Simulating the Input Capacitance*

```
* Spice Script for simulating -3dB point with RIN=1meg to determine the input
capacitance
*
* ntyp.txt and ptyp.txt are the files containing BSIM3 parameters for p-type and
*n-type of MOSFET of On-Semiconductor's 0.35um CMOS process, respectively.
* buffer_monitor.spi is the file containing the extracted postlayout netlist of
*the bulk-driven buffer.
*
.lib ntyp.txt
.lib ptyp.txt
.lib buffer_monitor.spi
*
* Pin assignment
* Xbuffer_monitor INNB INNC INPB INPC INPG OUT REF VS gnd vdd buffer_monitor
*****
.control
run
let mag1s=vecmax(IN1S)-vecmin(IN1S)
let mag1o=vecmax(IN1O)-vecmin(IN1O)
let mag2s=vecmax(IN2S)-vecmin(IN2S)
let mag2o=vecmax(IN2O)-vecmin(IN2O)
let mag3s=vecmax(IN3S)-vecmin(IN3S)
let mag3o=vecmax(IN3O)-vecmin(IN3O)
let mag4s=vecmax(IN4S)-vecmin(IN4S)
let mag4o=vecmax(IN4O)-vecmin(IN4O)
let mag5s=vecmax(IN5S)-vecmin(IN5S)
let mag5o=vecmax(IN5O)-vecmin(IN5O)
let mag6s=vecmax(IN6S)-vecmin(IN6S)
let mag6o=vecmax(IN6O)-vecmin(IN6O)
let mag7s=vecmax(IN7S)-vecmin(IN7S)
let mag7o=vecmax(IN7O)-vecmin(IN7O)
let mag8s=vecmax(IN8S)-vecmin(IN8S)
let mag8o=vecmax(IN8O)-vecmin(IN8O)
let mag9s=vecmax(IN9S)-vecmin(IN9S)
let mag9o=vecmax(IN9O)-vecmin(IN9O)
print mag1s mag1o mag2s mag2o mag3s mag3o mag4s mag4o
+ mag5s mag5o mag6s mag6o mag7s mag7o mag8s mag8o
+ mag9s mag9o
plot IN1SS IN1S xunits s
plot IN1OO IN1O xunits s
plot IN2SS IN2S xunits s
plot IN2OO IN2O xunits s
plot IN3SS IN3S xunits s
plot IN3OO IN3O xunits s
```

```

plot IN4SS IN4S xunits s
plot IN400 IN4O xunits s
plot IN5SS IN5S xunits s
plot IN500 IN5O xunits s
plot IN6SS IN6S xunits s
plot IN600 IN6O xunits s
plot IN7SS IN7S xunits s
plot IN700 IN7O xunits s
plot IN8SS IN8S xunits s
plot IN800 IN8O xunits s
plot IN9SS IN9S xunits s
plot IN900 IN9O xunits s
.endc
*****
.tran 10n 10u
*****
VDD vdd 0 DC 1
*****
*****
VIN1S IN1SS 0 DC sin(0.1 0.05 105k 10ns 0)
RIN1S IN1SS IN1S 1meg
RREF1S vdd REF1S 220k
X1S OUT1S OUT1S IN1S IN1S INPG1S OUT1S REF1S VS1S 0 vdd buffer_monitor
*****
VIN1O IN100 0 DC sin(0.1 0.05 114k 10ns 0)
RIN1O IN100 IN1O 1meg
RREF1O vdd REF1O 220k
X1O OUT1O 0 IN1O 0 INPG1O OUT1O REF1O VS1O 0 vdd buffer_monitor
*****
VIN2S IN2SS 0 DC sin(0.2 0.05 113k 10ns 0)
RIN2S IN2SS IN2S 1meg
RREF2S vdd REF2S 220k
X2S OUT2S OUT2S IN2S IN2S INPG2S OUT2S REF2S VS2S 0 vdd buffer_monitor
*****
VIN2O IN200 0 DC sin(0.2 0.05 124k 10ns 0)
RIN2O IN200 IN2O 1meg
RREF2O vdd REF2O 220k
X2O OUT2O 0 IN2O 0 INPG2O OUT2O REF2O VS2O 0 vdd buffer_monitor
*****
VIN3S IN3SS 0 DC sin(0.3 0.05 117k 10ns 0)
RIN3S IN3SS IN3S 1meg
RREF3S vdd REF3S 220k
X3S OUT3S OUT3S IN3S IN3S INPG3S OUT3S REF3S VS3S 0 vdd buffer_monitor
*****
VIN3O IN300 0 DC sin(0.3 0.05 128k 10ns 0)
RIN3O IN300 IN3O 1meg
RREF3O vdd REF3O 220k
X3O OUT3O 0 IN3O 0 INPG3O OUT3O REF3O VS3O 0 vdd buffer_monitor
*****
VIN4S IN4SS 0 DC sin(0.4 0.05 120k 10ns 0)
RIN4S IN4SS IN4S 1meg
RREF4S vdd REF4S 220k
X4S OUT4S OUT4S IN4S IN4S INPG4S OUT4S REF4S VS4S 0 vdd buffer_monitor
*****
VIN4O IN400 0 DC sin(0.4 0.05 132k 10ns 0)
RIN4O IN400 IN4O 1meg
RREF4O vdd REF4O 220k
X4O OUT4O 0 IN4O 0 INPG4O OUT4O REF4O VS4O 0 vdd buffer_monitor
*****
VIN5S IN5SS 0 DC sin(0.5 0.05 123k 10ns 0)
RIN5S IN5SS IN5S 1meg
RREF5S vdd REF5S 220k
X5S OUT5S OUT5S IN5S IN5S INPG5S OUT5S REF5S VS5S 0 vdd buffer_monitor
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VIN5O IN500 0 DC sin(0.5 0.05 136k 10ns 0)
RIN5O IN500 IN5O 1meg
RREF5O vdd REF5O 220k
X5O OUT5O 0 IN5O 0 INPG5O OUT5O REF5O VS5O 0 vdd buffer_monitor
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VIN6S IN6SS 0 DC sin(0.6 0.05 126k 10ns 0)
RIN6S IN6SS IN6S 1meg
RREF6S vdd REF6S 220k
X6S OUT6S OUT6S IN6S IN6S INPG6S OUT6S REF6S VS6S 0 vdd buffer_monitor
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VIN6O IN600 0 DC sin(0.6 0.05 139k 10ns 0)
RIN6O IN600 IN6O 1meg
RREF6O vdd REF6O 220k
X6O OUT6O 0 IN6O 0 INPG6O OUT6O REF6O VS6O 0 vdd buffer_monitor
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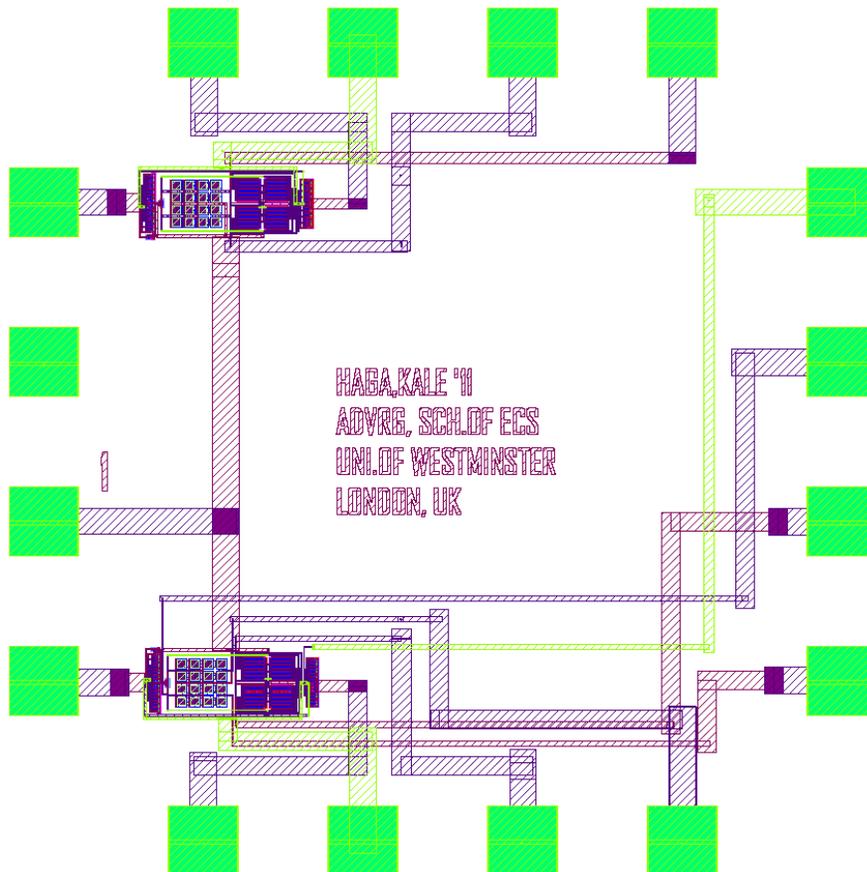
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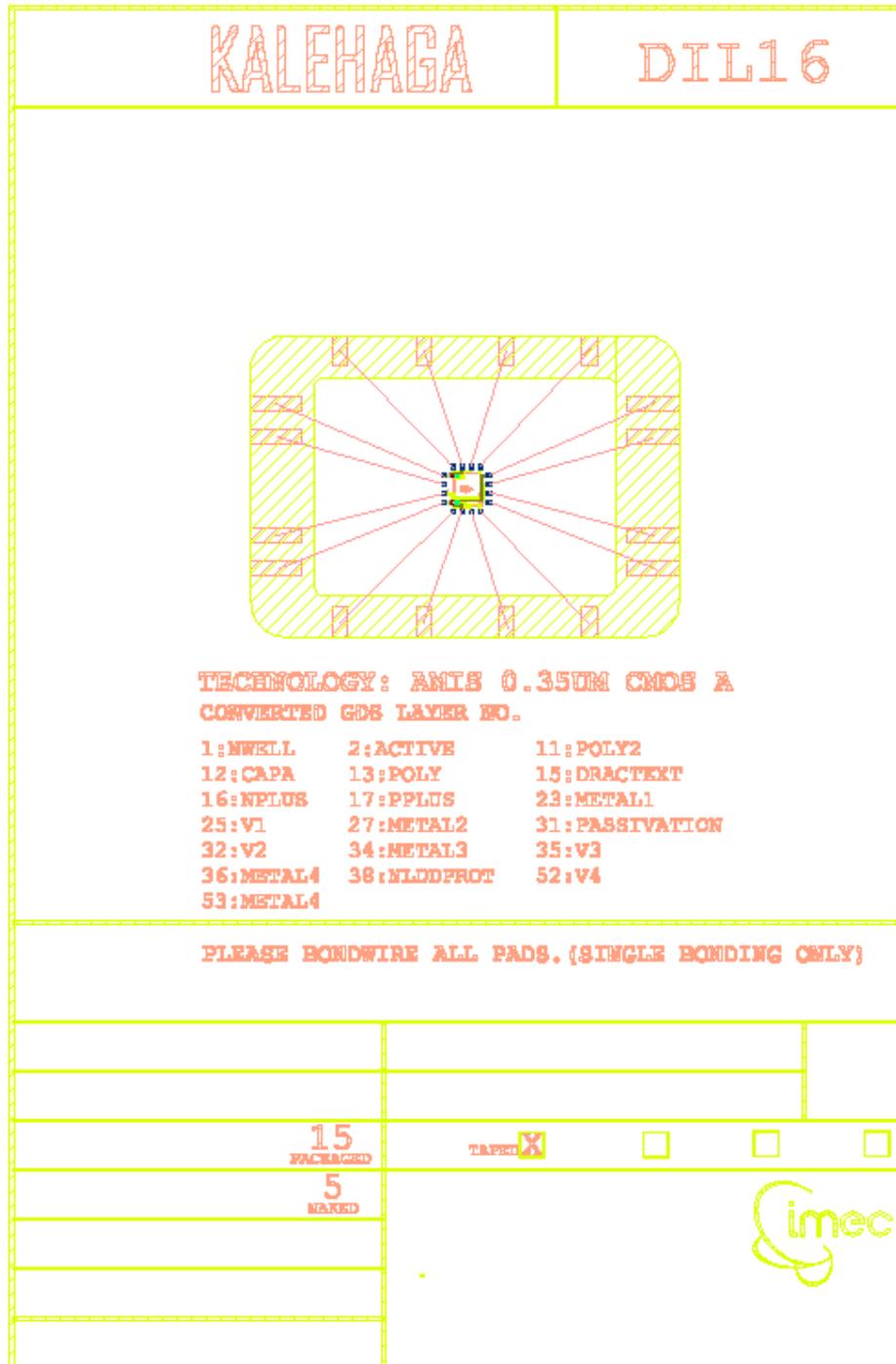
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RREF7O vdd REF7O 220k
X7O OUT7O 0 IN7O 0 INPG7O OUT7O REF7O VS7O 0 vdd buffer_monitor
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X8S OUT8S OUT8S IN8S IN8S INPG8S OUT8S REF8S VS8S 0 vdd buffer_monitor
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RIN8O IN8O0 IN8O 1meg
RREF8O vdd REF8O 220k
X8O OUT8O 0 IN8O 0 INPG8O OUT8O REF8O VS8O 0 vdd buffer_monitor
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RREF9S vdd REF9S 220k
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RREF9O vdd REF9O 220k
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*****
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```

## B.2 IC Layout of the Whole Die

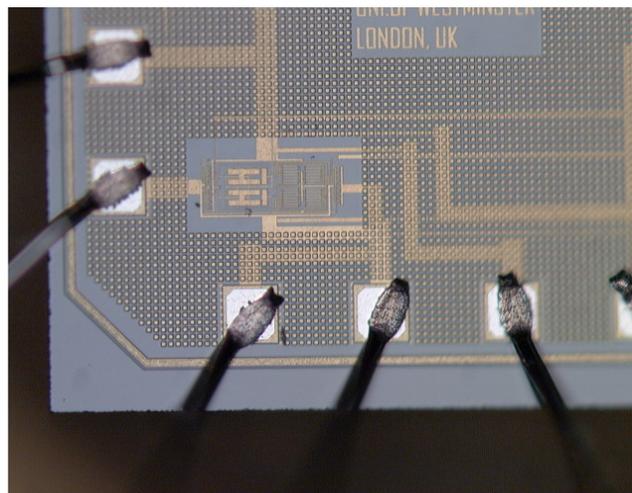
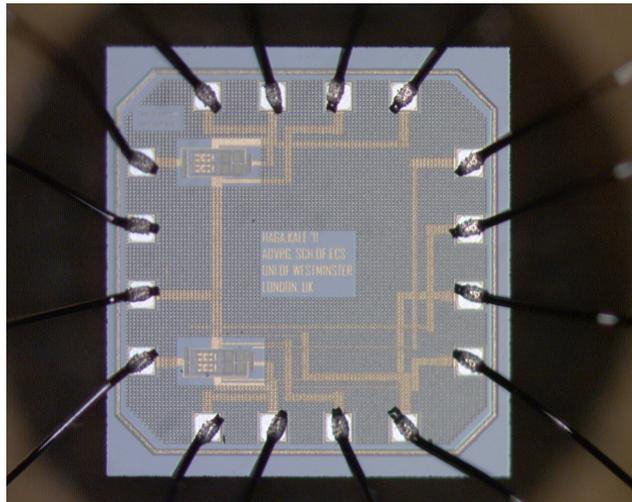
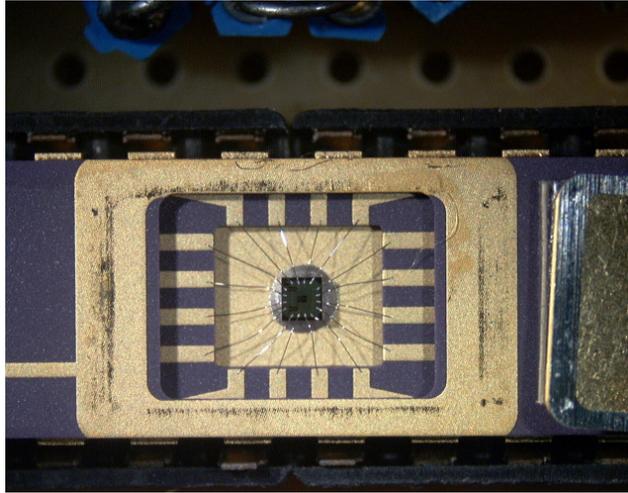


### B.3 Bonding Diagram

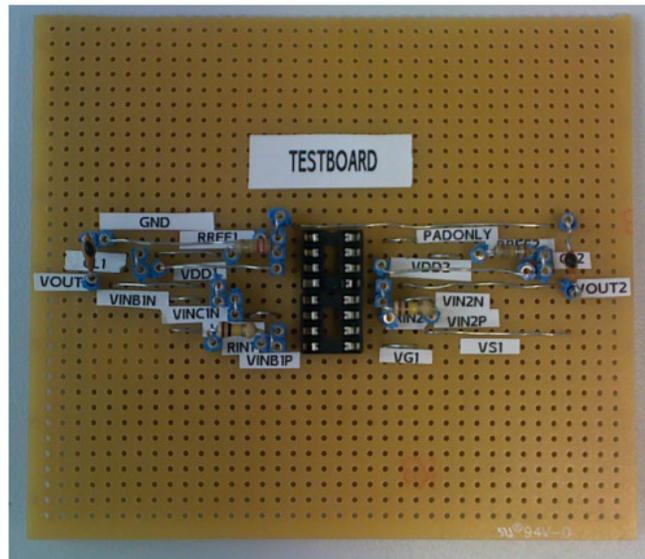
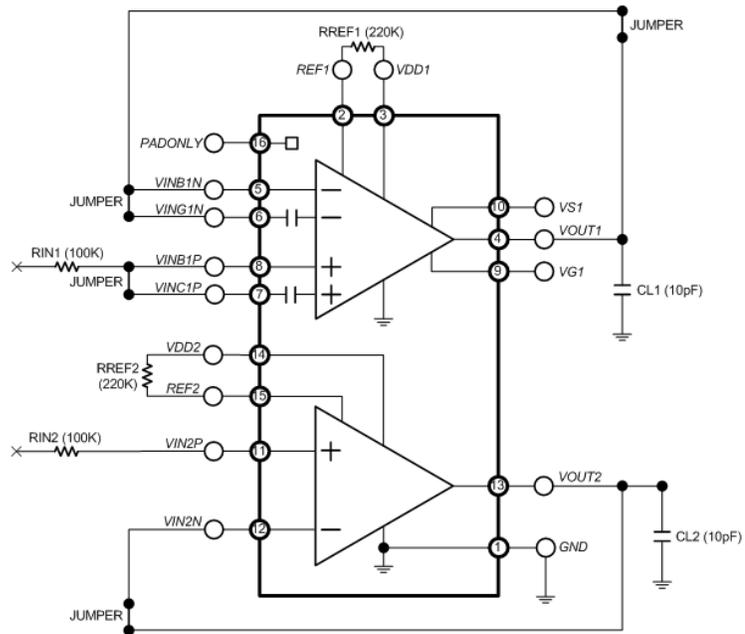


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***B.4 More Snapshots of the Microphotograph of the Fabricated Device***



## B.5 Test Board



## Appendix C Logs of Measurement Data

This appendix lists all the logs of the measurement data which have been used to determine the overall input capacitance of the fabricated device described in Chapter 6. Table C-1 shown below gives the summary of the comparison between the measured and simulated results.

**Table C-1 Comparison of the Summary of the Measurement Results to the Simulation Results**

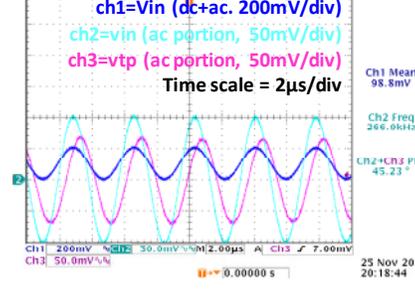
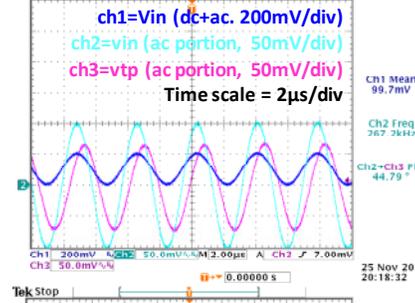
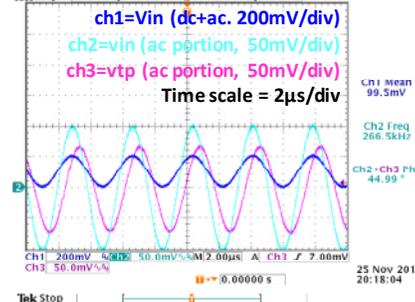
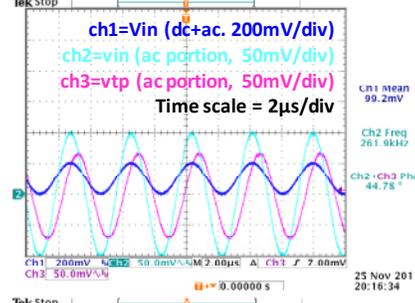
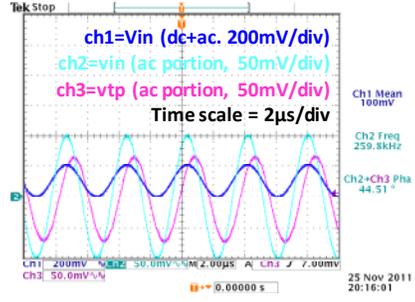
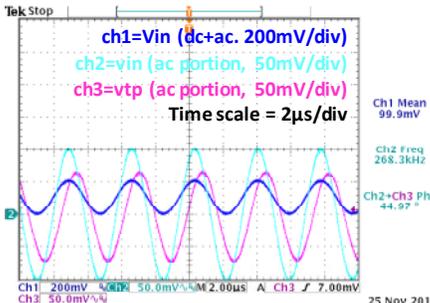
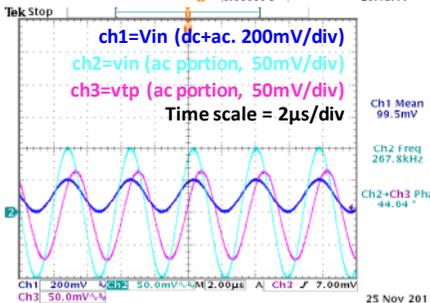
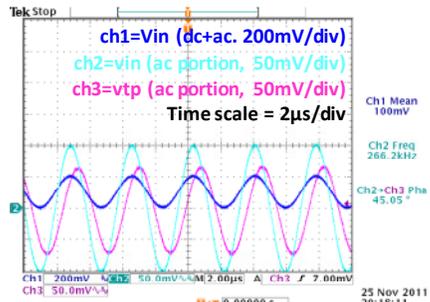
| VBIAS | @ noQFG node   |                      | @ QFG node  |                      |
|-------|--|----------------------|---|----------------------|
|       | Measured Results   | Simulated Results    | Measured Results  | Simulated Results    |
| 0.1   | C_Total= 1.258E-11 ± 1.7E-13<br>C_Stray= 1.128E-11 ± 1.7E-13<br><b>Cin= 1.30E-12 ± 3.4E-13</b> | <b>Cin= 1.40E-12</b> | C_Total= 1.297E-11 ± 1.3E-13<br>C_Stray= use left<br><b>Cin= 1.69E-12 ± 3.0E-13</b> | <b>Cin= 1.52E-12</b> |
| 0.2   | C_Total= 1.267E-11 ± 1.3E-13<br>C_Stray= 1.124E-11 ± 1.3E-13<br><b>Cin= 1.43E-12 ± 2.7E-13</b> | <b>Cin= 1.28E-12</b> | C_Total= 1.294E-11 ± 1.5E-13<br>C_Stray= use left<br><b>Cin= 1.70E-12 ± 2.8E-13</b> | <b>Cin= 1.41E-12</b> |
| 0.3   | C_Total= 1.282E-11 ± 1.1E-13<br>C_Stray= 1.126E-11 ± 1.3E-13<br><b>Cin= 1.56E-12 ± 2.3E-13</b> | <b>Cin= 1.24E-12</b> | C_Total= 1.293E-11 ± 1.1E-13<br>C_Stray= use left<br><b>Cin= 1.67E-12 ± 2.3E-13</b> | <b>Cin= 1.36E-12</b> |
| 0.4   | C_Total= 1.255E-11 ± 1.3E-13<br>C_Stray= 1.125E-11 ± 1.3E-13<br><b>Cin= 1.30E-12 ± 2.6E-13</b> | <b>Cin= 1.21E-12</b> | C_Total= 1.277E-11 ± 1.3E-13<br>C_Stray= use left<br><b>Cin= 1.52E-12 ± 2.6E-13</b> | <b>Cin= 1.33E-12</b> |
| 0.5   | C_Total= 1.253E-11 ± 2.3E-13<br>C_Stray= 1.147E-11 ± 1.2E-13<br><b>Cin= 1.06E-12 ± 3.5E-13</b> | <b>Cin= 1.17E-12</b> | C_Total= 1.277E-11 ± 1.4E-13<br>C_Stray= use left<br><b>Cin= 1.30E-12 ± 2.6E-13</b> | <b>Cin= 1.29E-12</b> |
| 0.6   | C_Total= 1.213E-11 ± 1.1E-13<br>C_Stray= 1.121E-11 ± 1.3E-13<br><b>Cin= 9.2E-13 ± 2.4E-13</b>  | <b>Cin= 1.15E-12</b> | C_Total= 1.266E-11 ± 9.5E-14<br>C_Stray= use left<br><b>Cin= 1.45E-12 ± 2.2E-13</b> | <b>Cin= 1.26E-12</b> |
| 0.7   | C_Total= 1.222E-11 ± 1.3E-13<br>C_Stray= 1.132E-11 ± 1.3E-13<br><b>Cin= 9.0E-13 ± 2.6E-13</b>  | <b>Cin= 1.12E-12</b> | C_Total= 1.274E-11 ± 1.1E-13<br>C_Stray= use left<br><b>Cin= 1.41E-12 ± 2.4E-13</b> | <b>Cin= 1.24E-12</b> |
| 0.8   | C_Total= 1.232E-11 ± 1.2E-13<br>C_Stray= 1.125E-11 ± 1.3E-13<br><b>Cin= 1.07E-12 ± 2.5E-13</b> | <b>Cin= 1.14E-12</b> | C_Total= 1.292E-11 ± 1.1E-13<br>C_Stray= use left<br><b>Cin= 1.67E-12 ± 2.4E-13</b> | <b>Cin= 1.26E-12</b> |
| 0.9   | C_Total= 1.238E-11 ± 1.2E-13<br>C_Stray= 1.128E-11 ± 1.4E-13<br><b>Cin= 1.10E-12 ± 2.5E-13</b> | <b>Cin= 1.22E-12</b> | C_Total= 1.295E-11 ± 1.2E-13<br>C_Stray= use left<br><b>Cin= 1.67E-12 ± 2.6E-13</b> | <b>Cin= 1.37E-12</b> |

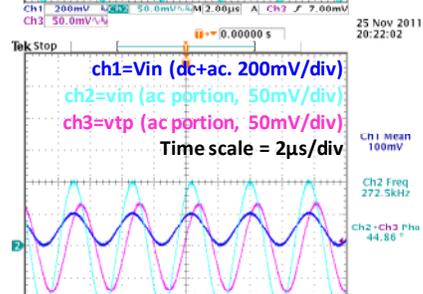
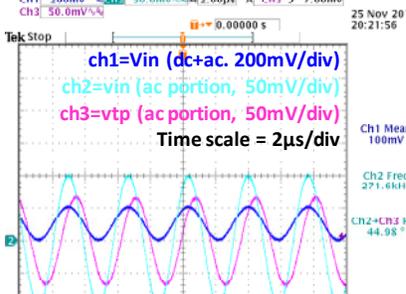
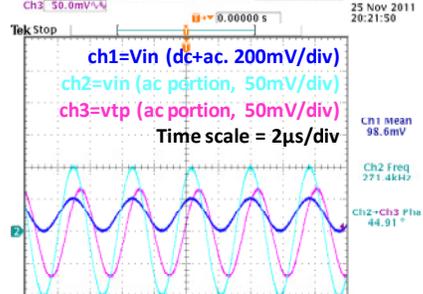
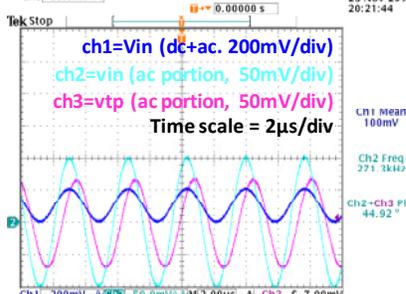
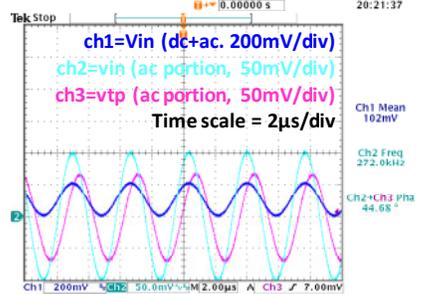
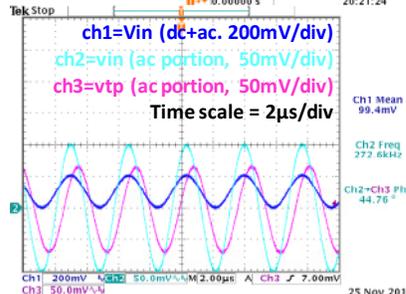
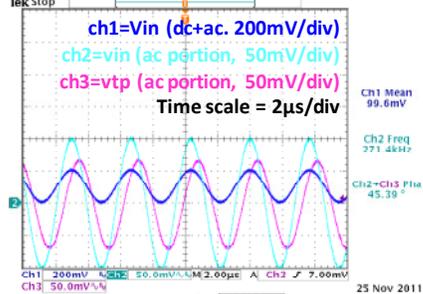
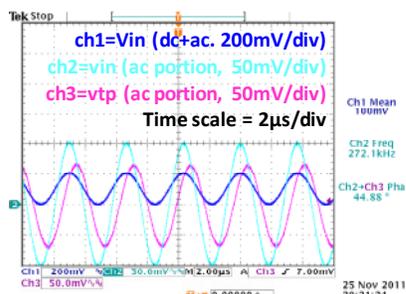
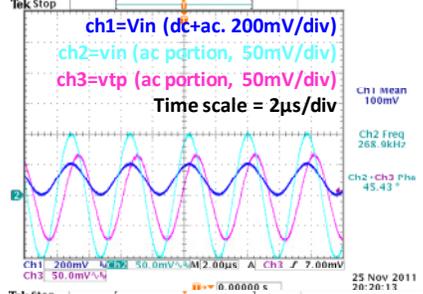
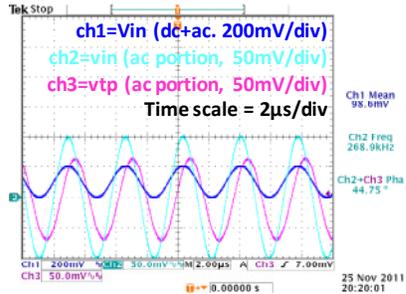
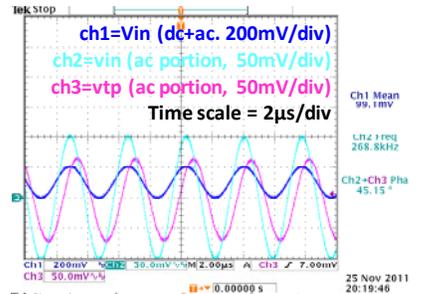
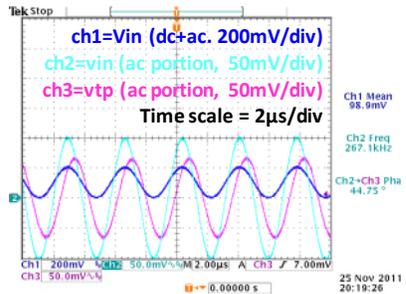
# Measurements at **NoQFG** point with **VBIAS=0.1V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.51 | 2.598E+05 | 1.28E-11 |
| 2          | 44.78 | 2.619E+05 | 1.28E-11 |
| 3          | 44.99 | 2.665E+05 | 1.27E-11 |
| 4          | 45.05 | 2.662E+05 | 1.28E-11 |
| 5          | 44.79 | 2.672E+05 | 1.26E-11 |
| 6          | 44.64 | 2.678E+05 | 1.25E-11 |
| 7          | 45.23 | 2.669E+05 | 1.28E-11 |
| 8          | 44.97 | 2.683E+05 | 1.26E-11 |
| 9          | 44.75 | 2.671E+05 | 1.26E-11 |
| 10         | 45.15 | 2.688E+05 | 1.27E-11 |
| 11         | 44.75 | 2.689E+05 | 1.25E-11 |
| 12         | 45.43 | 2.689E+05 | 1.28E-11 |
| 13         | 44.88 | 2.721E+05 | 1.24E-11 |
| 14         | 45.39 | 2.714E+05 | 1.27E-11 |
| 15         | 44.76 | 2.726E+05 | 1.23E-11 |
| 16         | 44.68 | 2.720E+05 | 1.23E-11 |
| 17         | 44.92 | 2.713E+05 | 1.25E-11 |
| 18         | 44.91 | 2.714E+05 | 1.24E-11 |
| 19         | 44.98 | 2.716E+05 | 1.25E-11 |
| 20         | 44.86 | 2.725E+05 | 1.24E-11 |

Average 44.92 2.687E+05 1.258E-11  
 STD 0.24 3.460E+03 1.698E-13



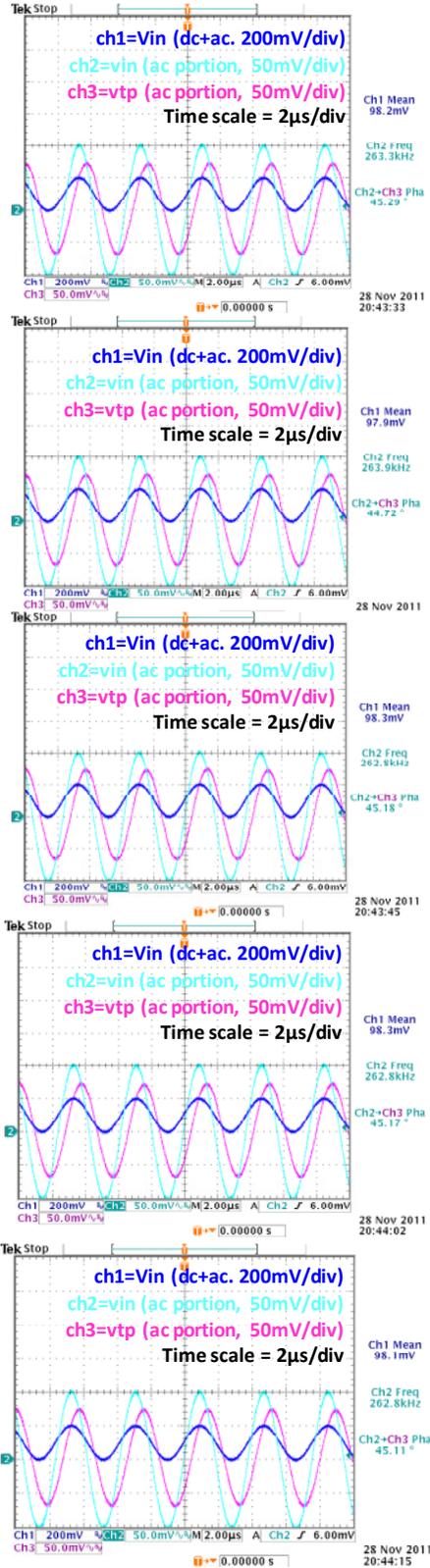
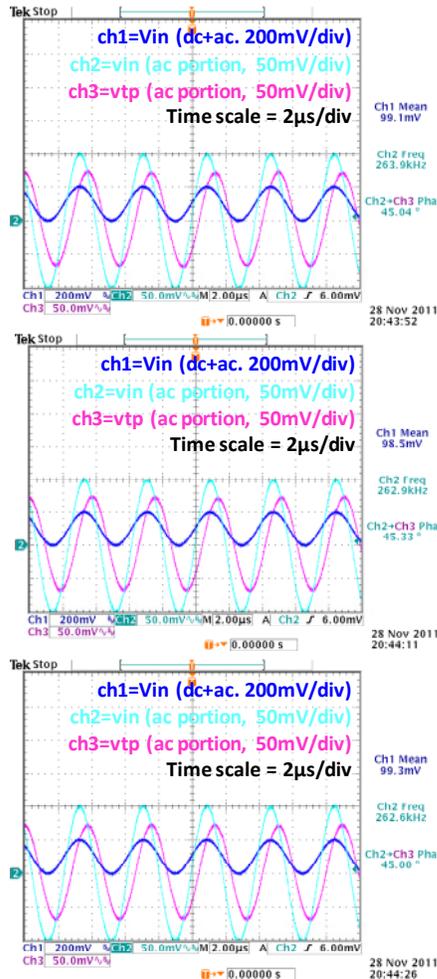


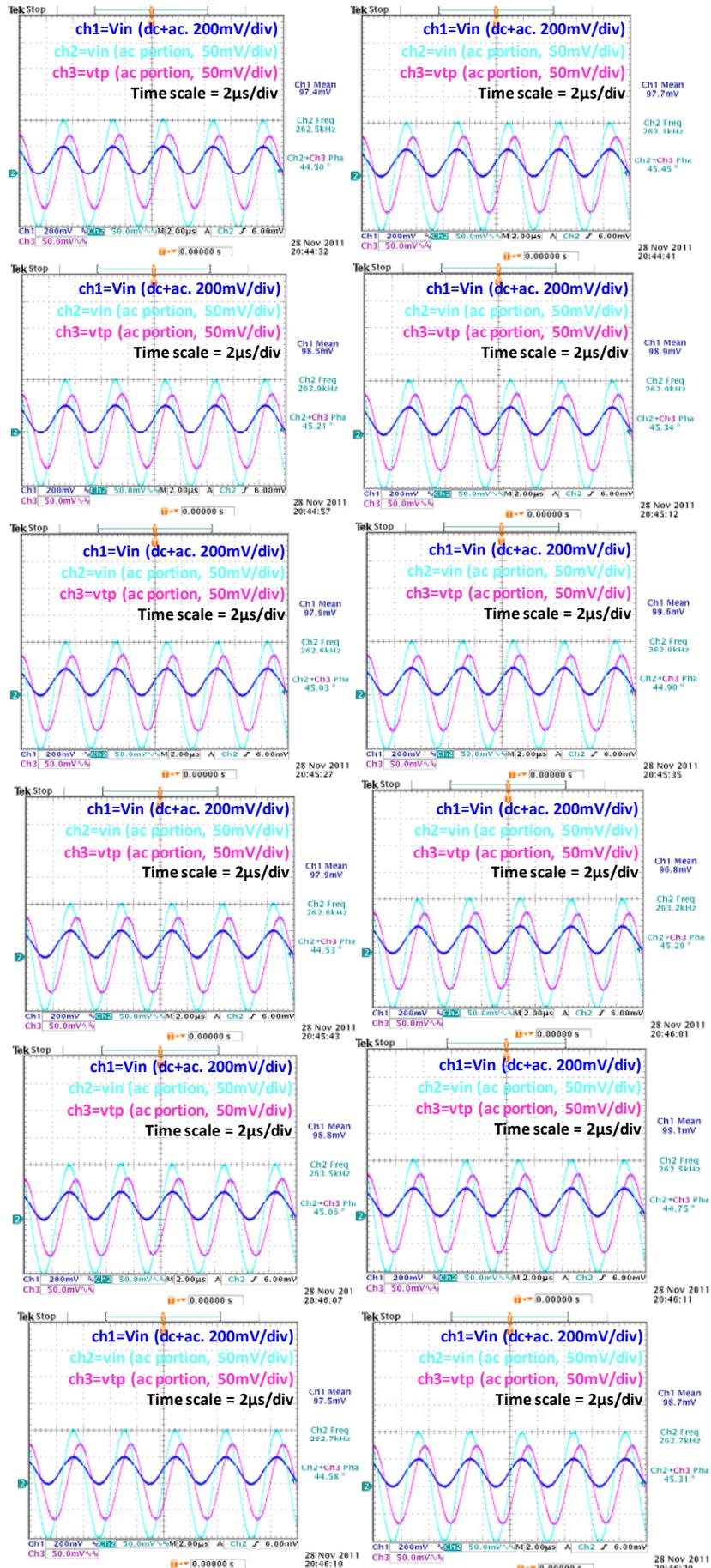
# Measurements at QFG point with **VBIAS=0.1V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.29 | 2.633E+05 | 1.30E-11 |
| 2          | 44.72 | 2.639E+05 | 1.27E-11 |
| 3          | 45.18 | 2.628E+05 | 1.30E-11 |
| 4          | 45.04 | 2.639E+05 | 1.29E-11 |
| 5          | 45.17 | 2.628E+05 | 1.30E-11 |
| 6          | 45.33 | 2.629E+05 | 1.30E-11 |
| 7          | 45.11 | 2.628E+05 | 1.29E-11 |
| 8          | 45.00 | 2.626E+05 | 1.29E-11 |
| 9          | 45.50 | 2.625E+05 | 1.31E-11 |
| 10         | 45.45 | 2.631E+05 | 1.31E-11 |
| 11         | 45.21 | 2.639E+05 | 1.29E-11 |
| 12         | 45.34 | 2.629E+05 | 1.30E-11 |
| 13         | 45.03 | 2.626E+05 | 1.29E-11 |
| 14         | 44.90 | 2.629E+05 | 1.28E-11 |
| 15         | 45.53 | 2.626E+05 | 1.31E-11 |
| 16         | 45.29 | 2.632E+05 | 1.30E-11 |
| 17         | 45.06 | 2.635E+05 | 1.29E-11 |
| 18         | 45.75 | 2.625E+05 | 1.33E-11 |
| 19         | 44.58 | 2.627E+05 | 1.27E-11 |
| 20         | 45.31 | 2.627E+05 | 1.30E-11 |

Average 45.19 2.630E+05 **1.297E-11**  
 STD 0.28 4.662E+02 **1.344E-13**



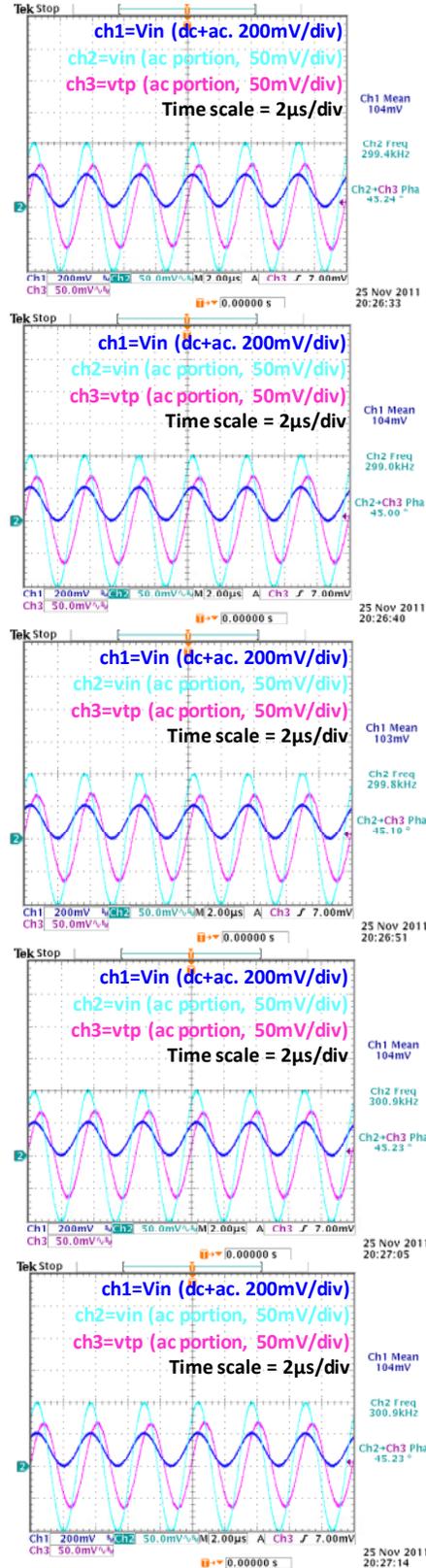
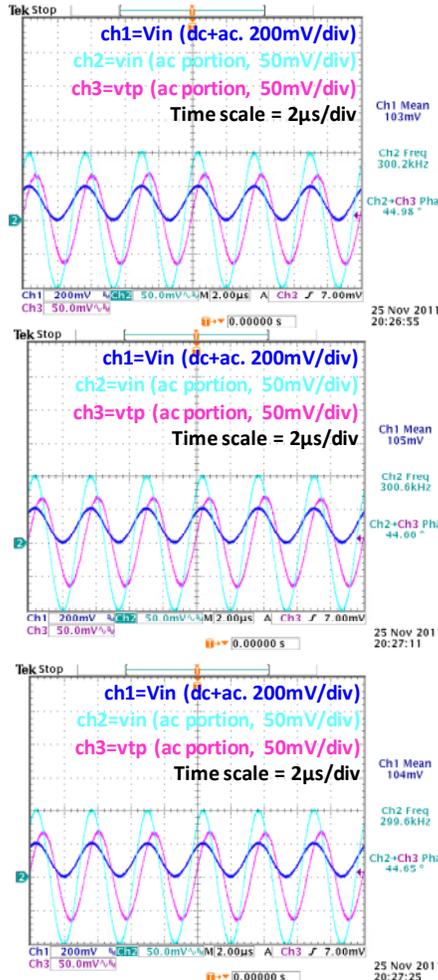


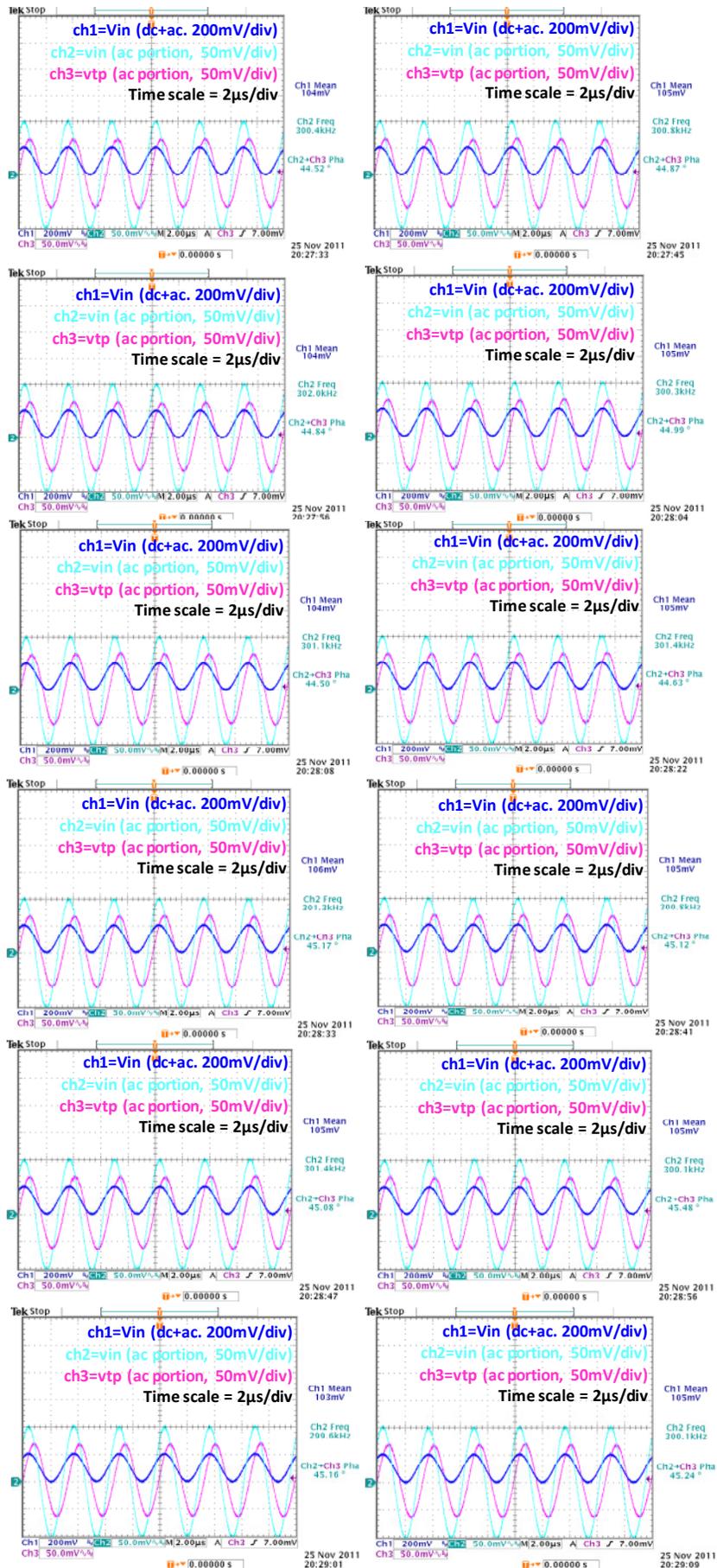
# Measurements at **PADONLY** point with **VBIAS=0.1V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.24 | 2.994E+05 | 1.14E-11 |
| 2          | 45.00 | 2.990E+05 | 1.13E-11 |
| 3          | 45.19 | 2.988E+05 | 1.14E-11 |
| 4          | 44.98 | 3.002E+05 | 1.13E-11 |
| 5          | 45.23 | 3.009E+05 | 1.14E-11 |
| 6          | 44.66 | 3.006E+05 | 1.11E-11 |
| 7          | 45.23 | 3.009E+05 | 1.14E-11 |
| 8          | 44.65 | 2.996E+05 | 1.12E-11 |
| 9          | 44.52 | 3.004E+05 | 1.11E-11 |
| 10         | 44.87 | 3.008E+05 | 1.12E-11 |
| 11         | 44.84 | 3.020E+05 | 1.12E-11 |
| 12         | 44.99 | 3.003E+05 | 1.13E-11 |
| 13         | 44.50 | 3.011E+05 | 1.11E-11 |
| 14         | 44.63 | 3.014E+05 | 1.11E-11 |
| 15         | 45.17 | 3.013E+05 | 1.13E-11 |
| 16         | 45.12 | 3.008E+05 | 1.13E-11 |
| 17         | 45.08 | 3.014E+05 | 1.13E-11 |
| 18         | 45.48 | 3.001E+05 | 1.15E-11 |
| 19         | 45.61 | 2.996E+05 | 1.16E-11 |
| 20         | 45.24 | 3.001E+05 | 1.14E-11 |

Average 45.01 3.004E+05 1.128E-11  
 STD 0.31 8.499E+02 1.349E-13



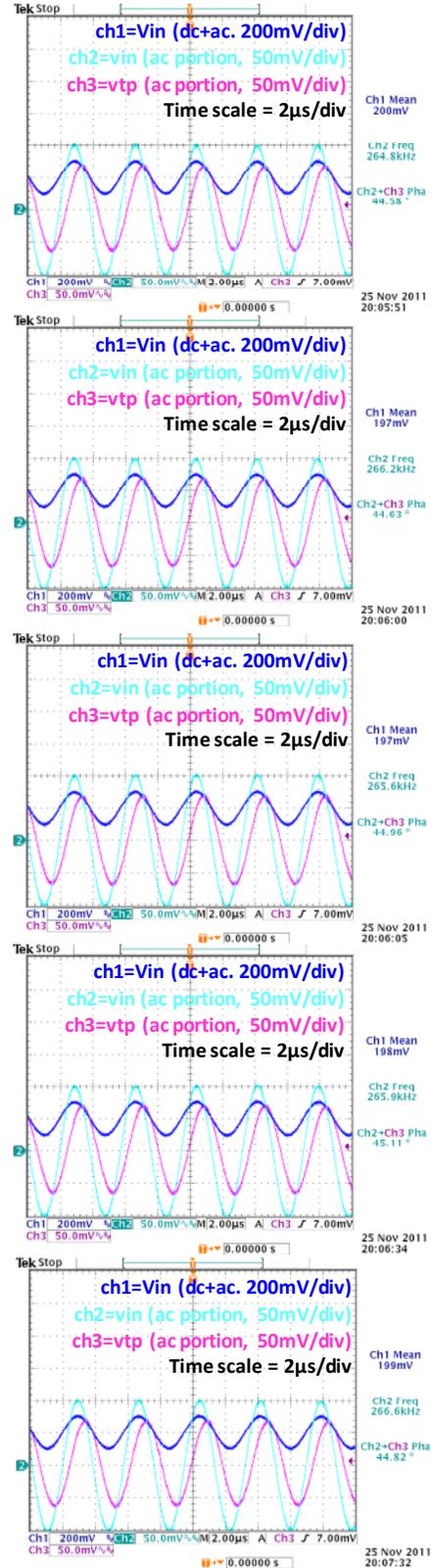
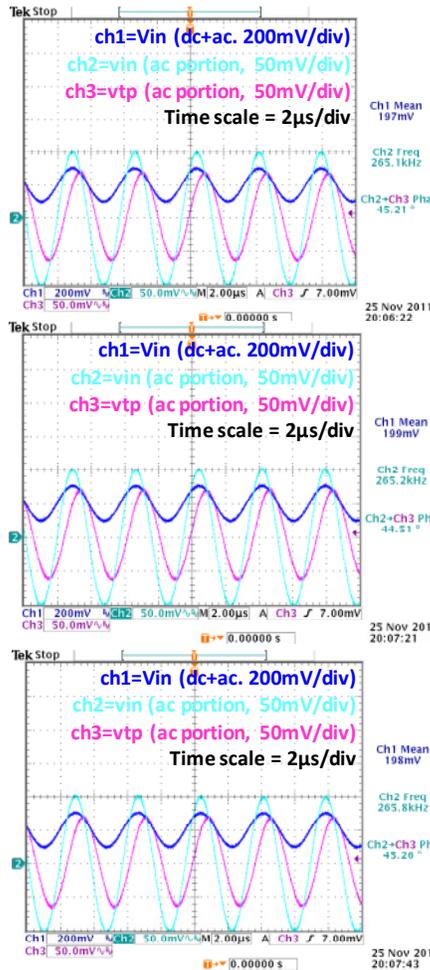


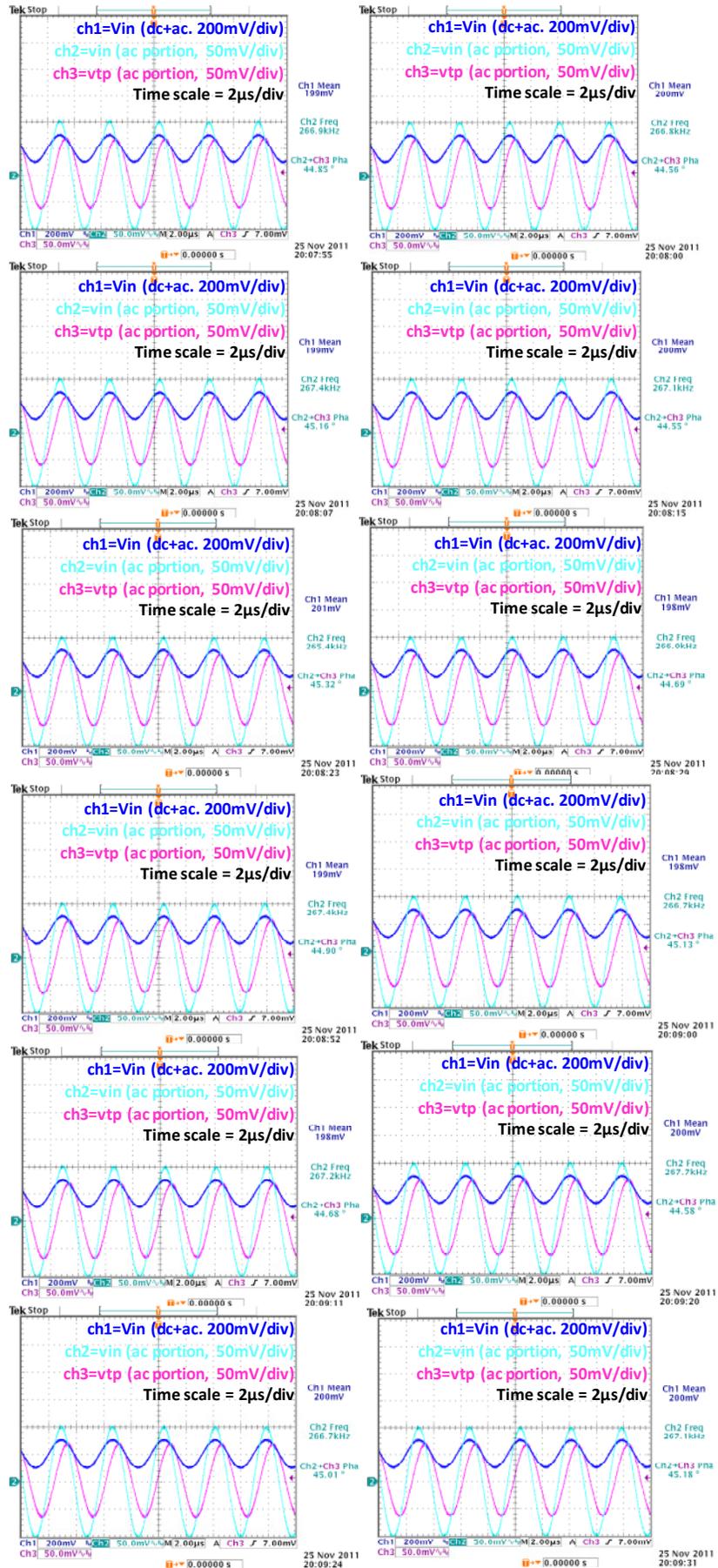
# Measurements at **NoQFG** point with **VBIAS=0.2V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.58 | 2.648E+05 | 1.26E-11 |
| 2          | 44.63 | 2.662E+05 | 1.26E-11 |
| 3          | 44.96 | 2.656E+05 | 1.27E-11 |
| 4          | 45.21 | 2.651E+05 | 1.29E-11 |
| 5          | 45.11 | 2.659E+05 | 1.28E-11 |
| 6          | 44.51 | 2.652E+05 | 1.26E-11 |
| 7          | 44.82 | 2.666E+05 | 1.26E-11 |
| 8          | 45.26 | 2.658E+05 | 1.29E-11 |
| 9          | 44.85 | 2.669E+05 | 1.26E-11 |
| 10         | 44.56 | 2.668E+05 | 1.25E-11 |
| 11         | 45.16 | 2.674E+05 | 1.27E-11 |
| 12         | 44.55 | 2.671E+05 | 1.25E-11 |
| 13         | 45.32 | 2.654E+05 | 1.29E-11 |
| 14         | 44.69 | 2.660E+05 | 1.26E-11 |
| 15         | 44.90 | 2.674E+05 | 1.26E-11 |
| 16         | 45.13 | 2.667E+05 | 1.28E-11 |
| 17         | 44.68 | 2.672E+05 | 1.25E-11 |
| 18         | 44.58 | 2.677E+05 | 1.25E-11 |
| 19         | 45.01 | 2.667E+05 | 1.27E-11 |
| 20         | 45.18 | 2.671E+05 | 1.28E-11 |

Average 44.88 2.664E+05 **1.267E-11**  
 STD 0.27 8.606E+02 **1.326E-13**



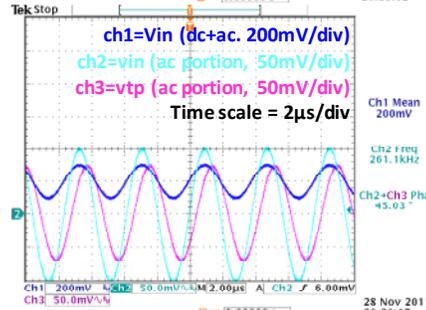
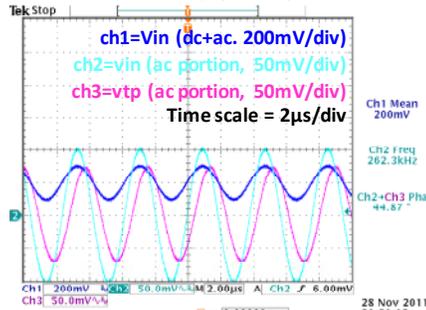
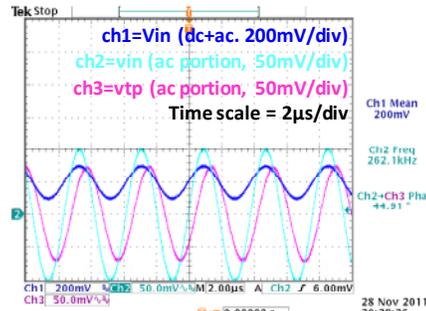
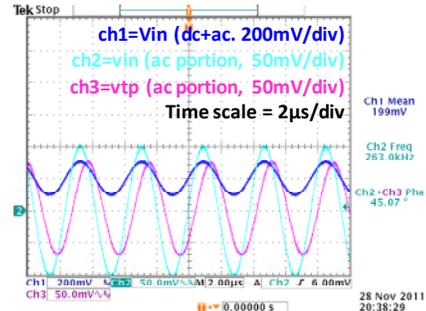
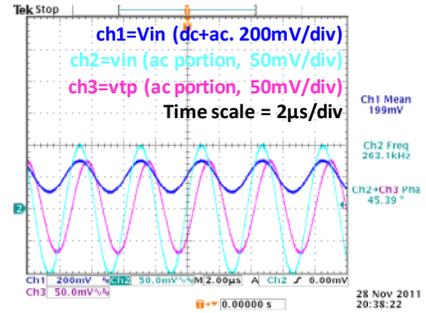
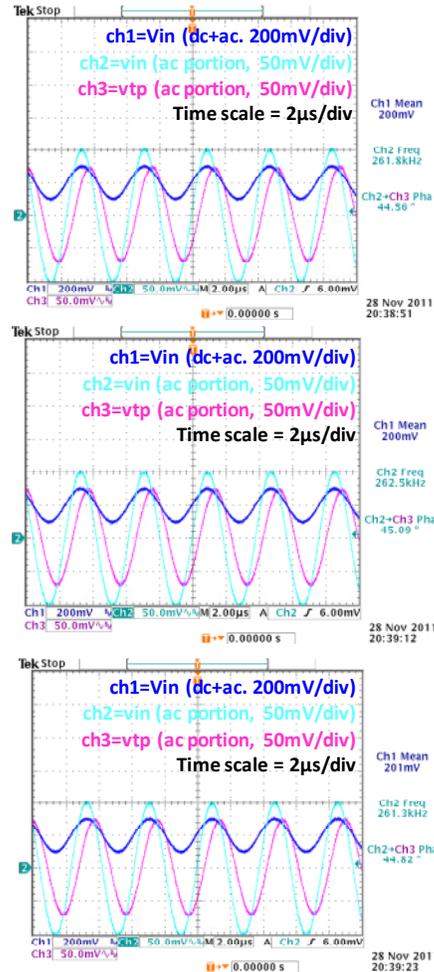


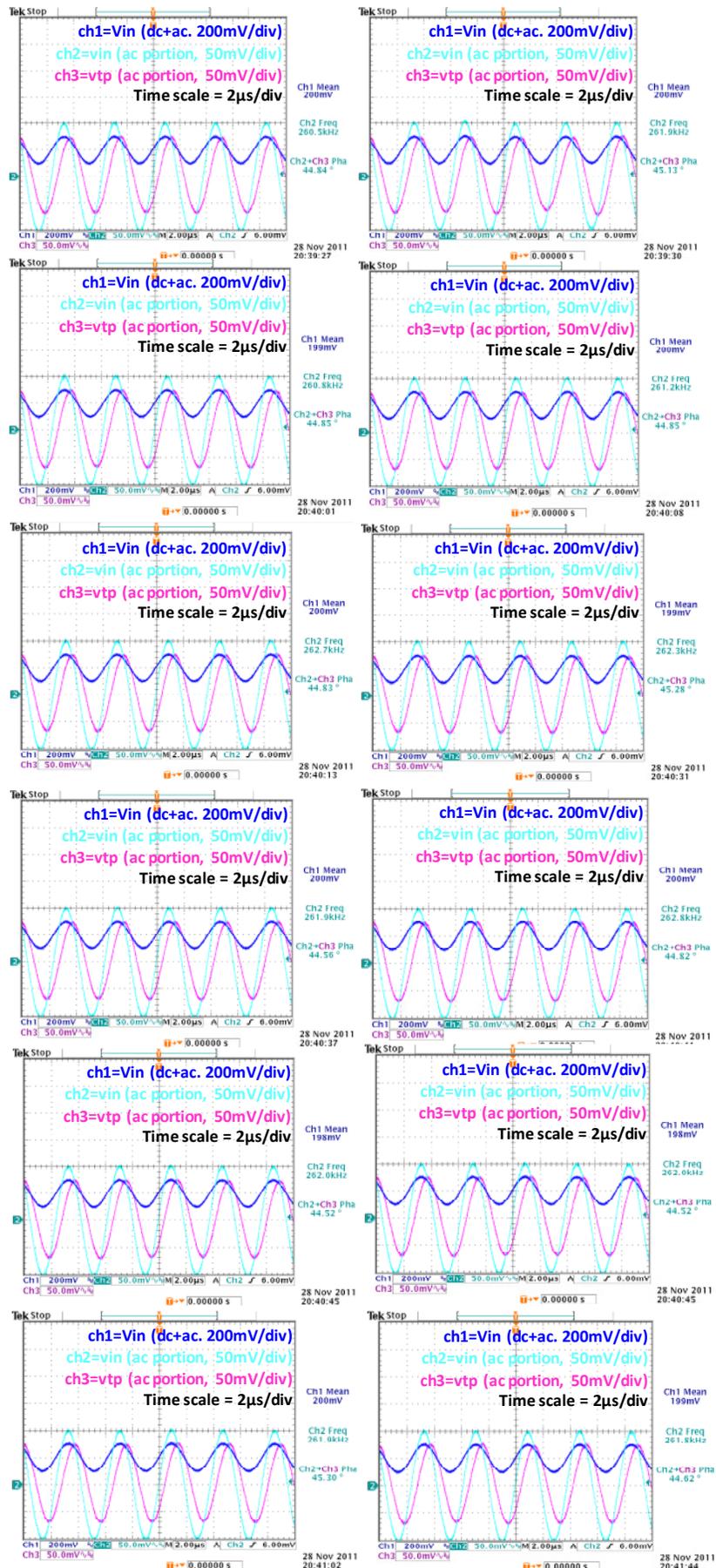
# Measurements at QFG point with VBIAS=0.2V

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.39 | 2.631E+05 | 1.31E-11 |
| 2          | 45.07 | 2.630E+05 | 1.29E-11 |
| 3          | 45.91 | 2.621E+05 | 1.33E-11 |
| 4          | 45.56 | 2.618E+05 | 1.32E-11 |
| 5          | 44.87 | 2.623E+05 | 1.29E-11 |
| 6          | 45.09 | 2.625E+05 | 1.29E-11 |
| 7          | 45.03 | 2.611E+05 | 1.30E-11 |
| 8          | 44.82 | 2.613E+05 | 1.29E-11 |
| 9          | 44.84 | 2.605E+05 | 1.29E-11 |
| 10         | 45.13 | 2.619E+05 | 1.30E-11 |
| 11         | 44.85 | 2.608E+05 | 1.29E-11 |
| 12         | 44.85 | 2.612E+05 | 1.29E-11 |
| 13         | 44.83 | 2.627E+05 | 1.28E-11 |
| 14         | 45.28 | 2.623E+05 | 1.30E-11 |
| 15         | 44.56 | 2.619E+05 | 1.27E-11 |
| 16         | 44.82 | 2.628E+05 | 1.28E-11 |
| 17         | 44.52 | 2.620E+05 | 1.27E-11 |
| 18         | 45.00 | 2.626E+05 | 1.29E-11 |
| 19         | 45.30 | 2.619E+05 | 1.31E-11 |
| 20         | 44.62 | 2.618E+05 | 1.28E-11 |

Average 45.02 2.620E+05 1.294E-11  
 STD 0.34 7.208E+02 1.520E-13



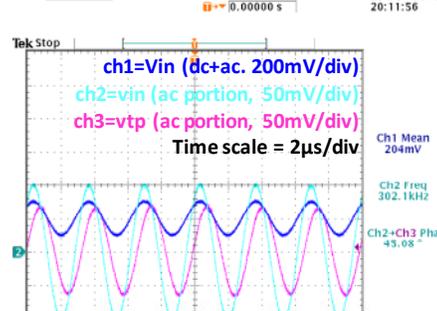
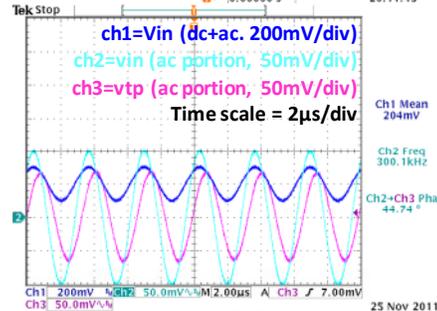
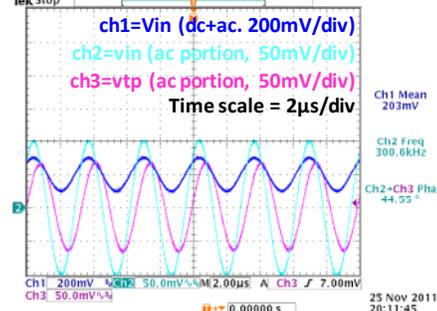
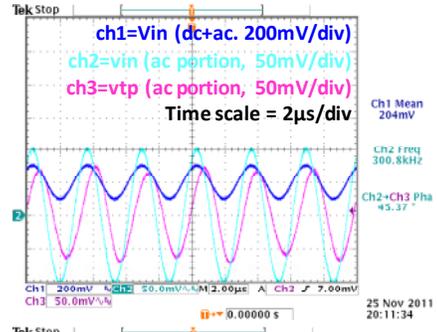
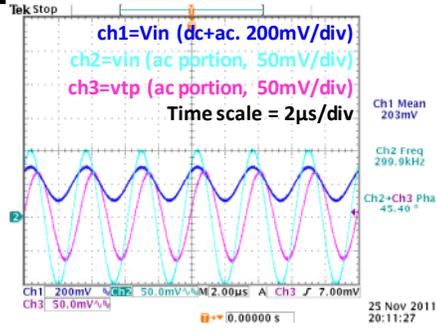
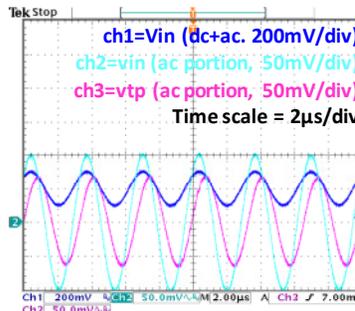
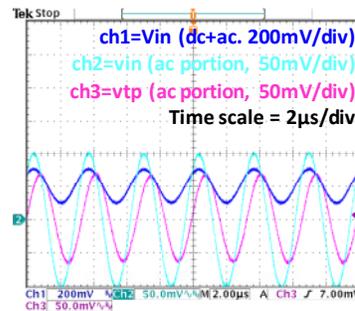
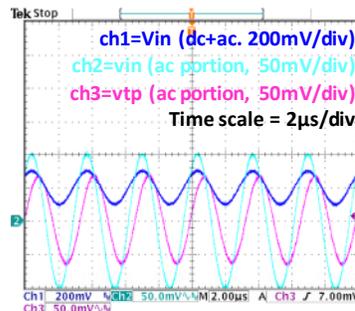


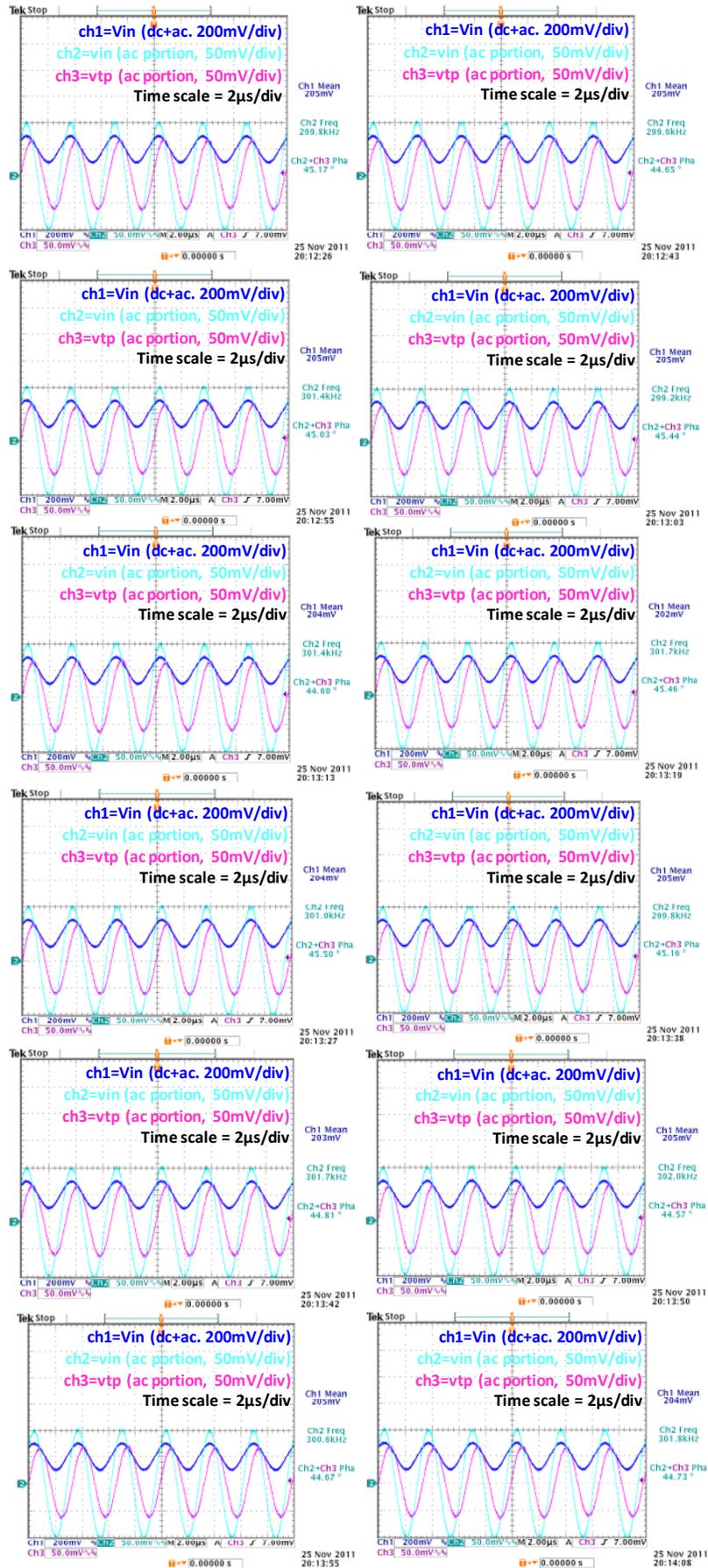
# Measurements at **PADONLY** point with **VBIAS=0.2V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.40 | 2.999E+05 | 1.15E-11 |
| 2          | 45.37 | 3.008E+05 | 1.14E-11 |
| 3          | 44.55 | 3.006E+05 | 1.11E-11 |
| 4          | 45.32 | 2.994E+05 | 1.14E-11 |
| 5          | 44.74 | 3.001E+05 | 1.12E-11 |
| 6          | 44.73 | 3.000E+05 | 1.12E-11 |
| 7          | 45.08 | 3.021E+05 | 1.12E-11 |
| 8          | 44.68 | 3.018E+05 | 1.11E-11 |
| 9          | 45.17 | 2.998E+05 | 1.14E-11 |
| 10         | 44.65 | 2.996E+05 | 1.12E-11 |
| 11         | 45.03 | 3.014E+05 | 1.13E-11 |
| 12         | 45.44 | 2.992E+05 | 1.15E-11 |
| 13         | 44.60 | 3.014E+05 | 1.11E-11 |
| 14         | 45.46 | 3.017E+05 | 1.14E-11 |
| 15         | 45.50 | 3.010E+05 | 1.15E-11 |
| 16         | 44.16 | 2.998E+05 | 1.10E-11 |
| 17         | 44.81 | 3.017E+05 | 1.12E-11 |
| 18         | 44.57 | 3.020E+05 | 1.11E-11 |
| 19         | 44.67 | 3.006E+05 | 1.11E-11 |
| 20         | 44.73 | 3.018E+05 | 1.11E-11 |

Average 44.93 3.007E+05 **1.124E-11**  
 STD 0.39 9.571E+02 **1.602E-13**



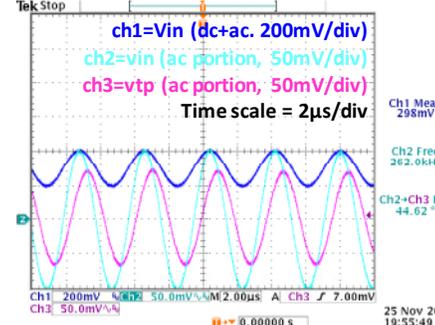
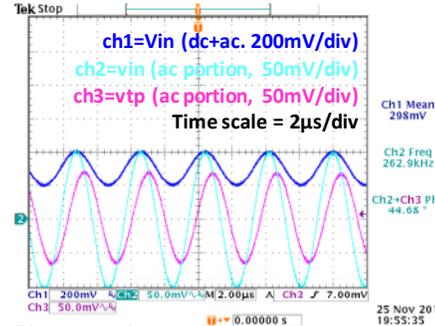
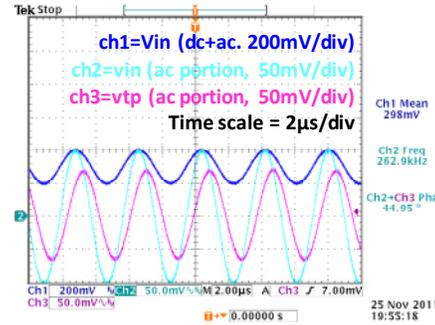
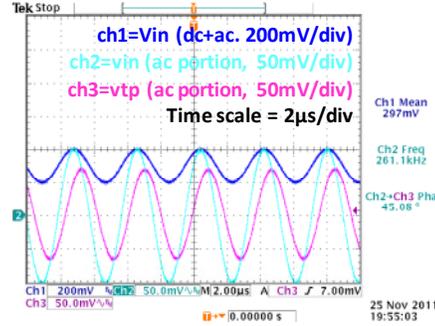
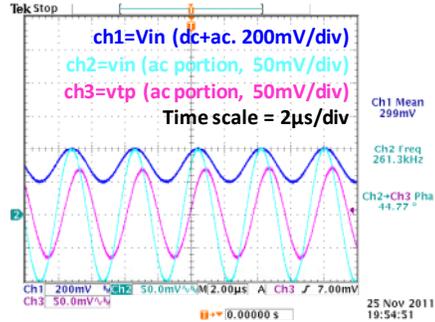
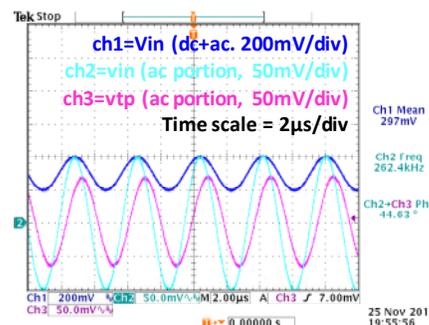
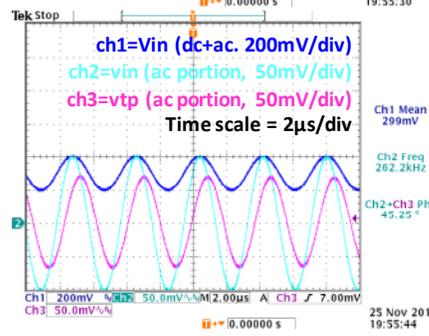
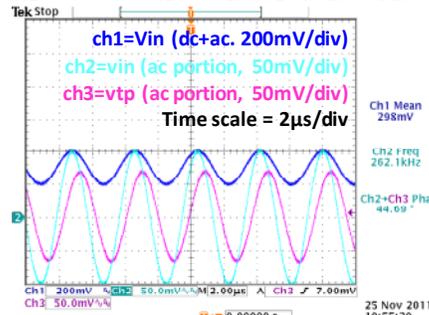


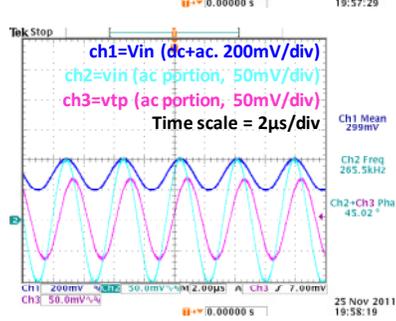
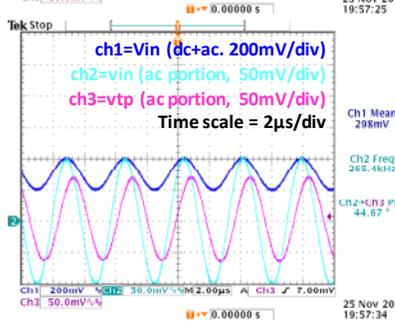
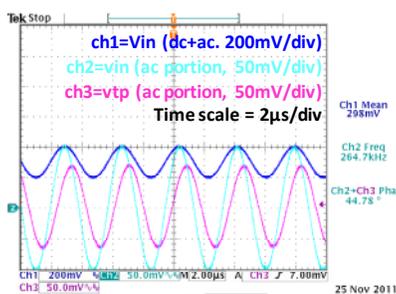
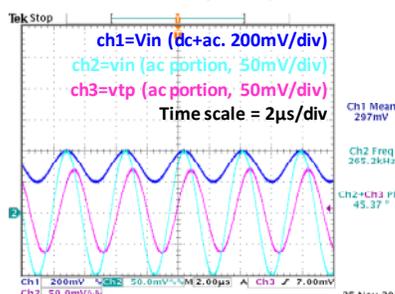
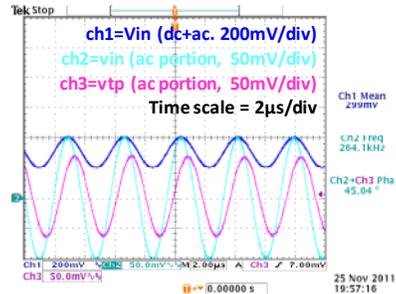
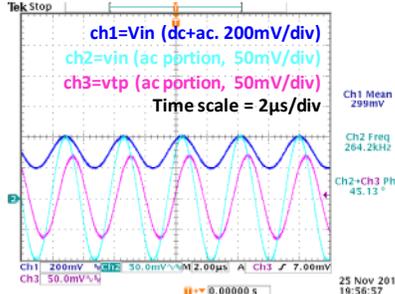
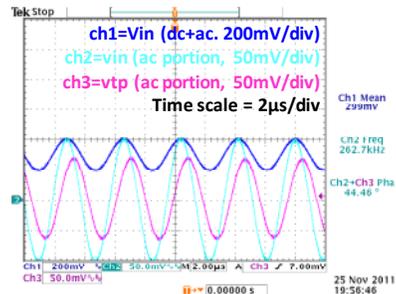
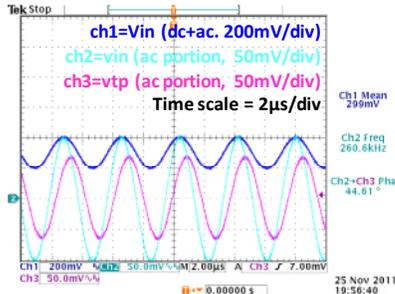
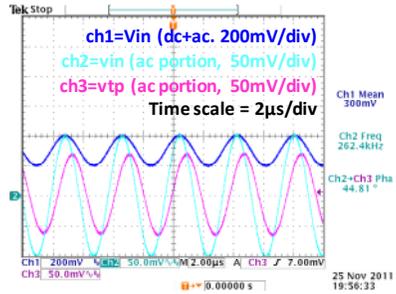
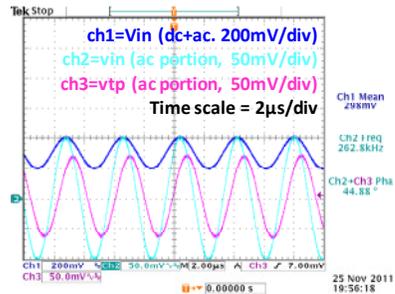
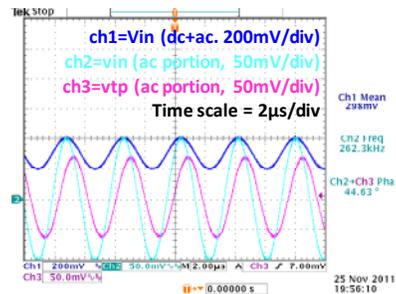
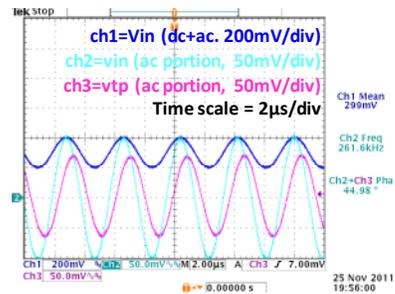
# Measurements at **NoQFG** point with **VBIAS=0.3V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.77 | 2.613E+05 | 1.29E-11 |
| 2          | 45.08 | 2.611E+05 | 1.30E-11 |
| 3          | 44.95 | 2.629E+05 | 1.29E-11 |
| 4          | 44.69 | 2.621E+05 | 1.28E-11 |
| 5          | 44.68 | 2.629E+05 | 1.27E-11 |
| 6          | 45.25 | 2.622E+05 | 1.30E-11 |
| 7          | 44.62 | 2.620E+05 | 1.28E-11 |
| 8          | 44.63 | 2.624E+05 | 1.27E-11 |
| 9          | 44.98 | 2.616E+05 | 1.29E-11 |
| 10         | 44.63 | 2.623E+05 | 1.28E-11 |
| 11         | 44.88 | 2.628E+05 | 1.28E-11 |
| 12         | 44.81 | 2.624E+05 | 1.28E-11 |
| 13         | 44.61 | 2.606E+05 | 1.28E-11 |
| 14         | 44.46 | 2.627E+05 | 1.27E-11 |
| 15         | 45.13 | 2.642E+05 | 1.29E-11 |
| 16         | 45.04 | 2.641E+05 | 1.28E-11 |
| 17         | 45.37 | 2.652E+05 | 1.29E-11 |
| 18         | 44.78 | 2.647E+05 | 1.27E-11 |
| 19         | 44.67 | 2.654E+05 | 1.26E-11 |
| 20         | 45.02 | 2.655E+05 | 1.28E-11 |

Average 44.85 2.629E+05 1.282E-11  
 STD 0.24 1.456E+03 1.090E-13



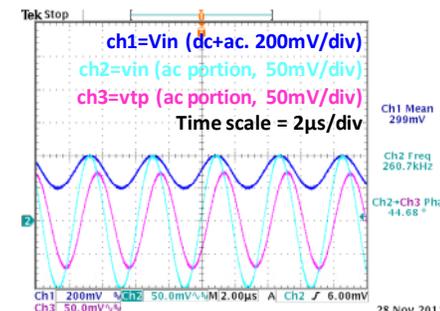
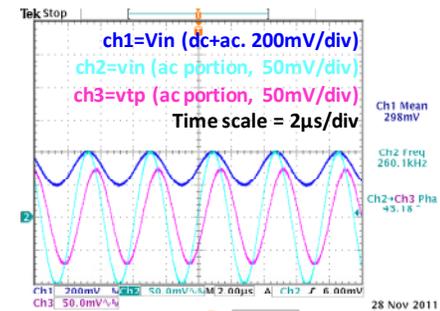
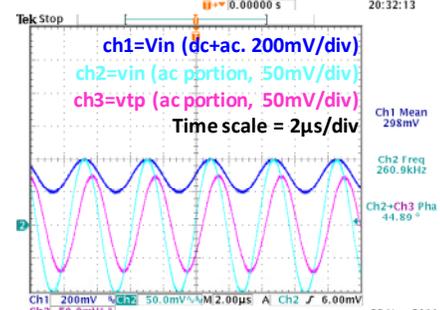
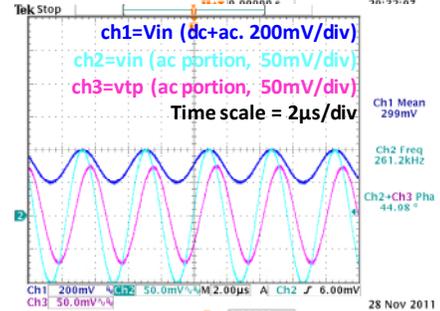
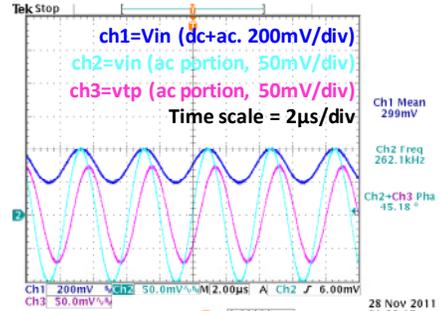
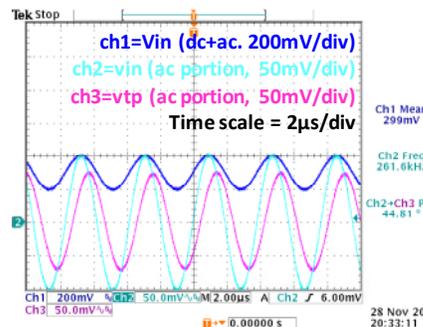
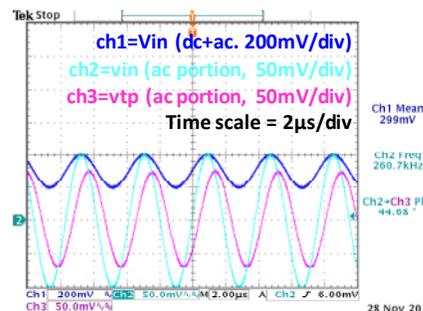
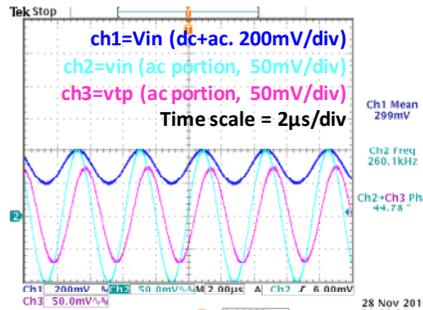


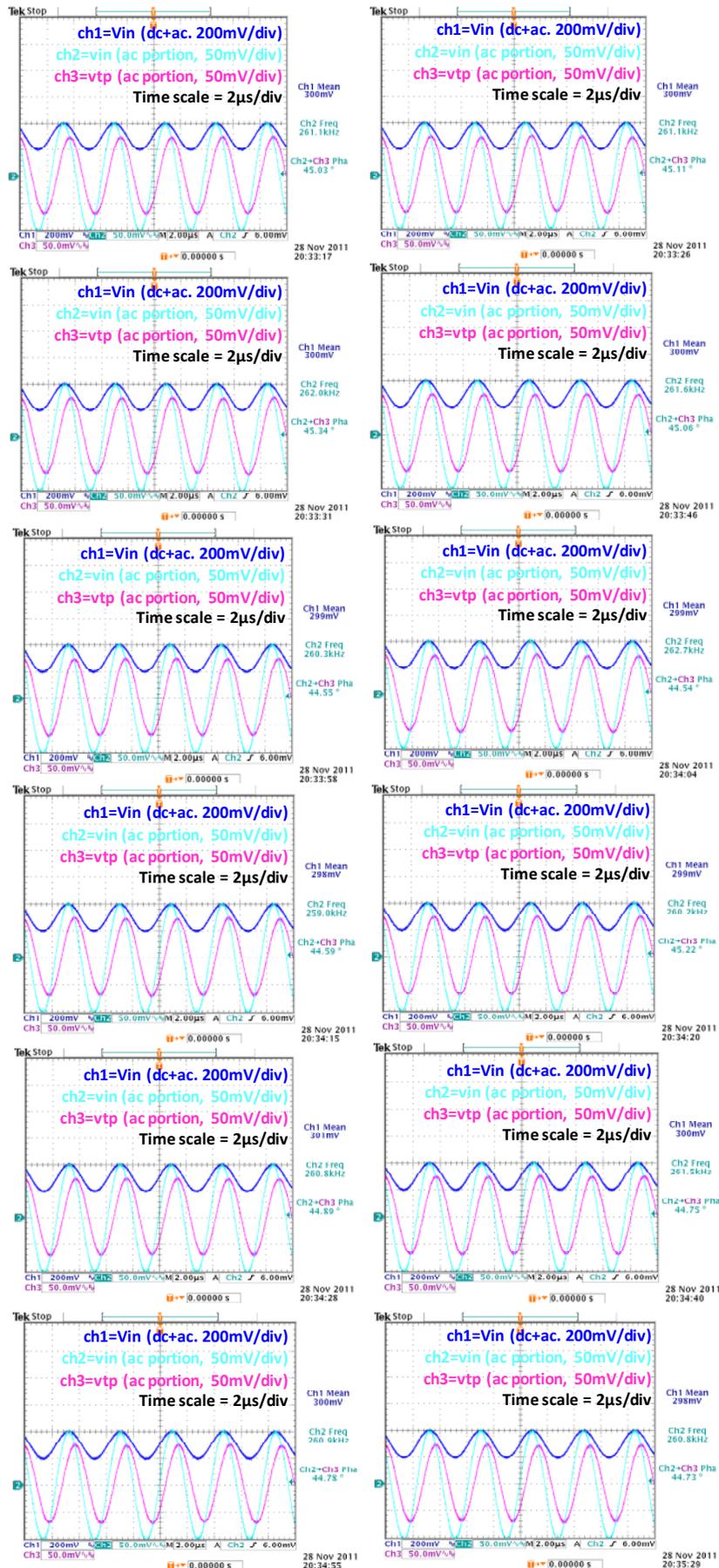
# Measurements at QFG point with VBIAS=0.3V

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.18 | 2.621E+05 | 1.30E-11 |
| 2          | 44.98 | 2.612E+05 | 1.30E-11 |
| 3          | 44.89 | 2.609E+05 | 1.29E-11 |
| 4          | 44.78 | 2.601E+05 | 1.29E-11 |
| 5          | 45.18 | 2.601E+05 | 1.31E-11 |
| 6          | 44.68 | 2.607E+05 | 1.29E-11 |
| 7          | 44.81 | 2.616E+05 | 1.29E-11 |
| 8          | 45.03 | 2.611E+05 | 1.30E-11 |
| 9          | 45.11 | 2.611E+05 | 1.30E-11 |
| 10         | 45.34 | 2.620E+05 | 1.31E-11 |
| 11         | 45.06 | 2.616E+05 | 1.30E-11 |
| 12         | 44.55 | 2.603E+05 | 1.28E-11 |
| 13         | 44.55 | 2.603E+05 | 1.28E-11 |
| 14         | 44.54 | 2.627E+05 | 1.27E-11 |
| 15         | 44.59 | 2.590E+05 | 1.29E-11 |
| 16         | 45.22 | 2.602E+05 | 1.31E-11 |
| 17         | 44.89 | 2.608E+05 | 1.29E-11 |
| 18         | 44.75 | 2.615E+05 | 1.28E-11 |
| 19         | 44.78 | 2.609E+05 | 1.29E-11 |
| 20         | 44.73 | 2.608E+05 | 1.29E-11 |

Average 44.88 2.610E+05 1.293E-11  
 STD 0.25 8.432E+02 1.085E-13



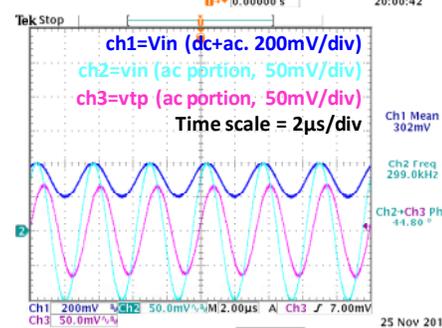
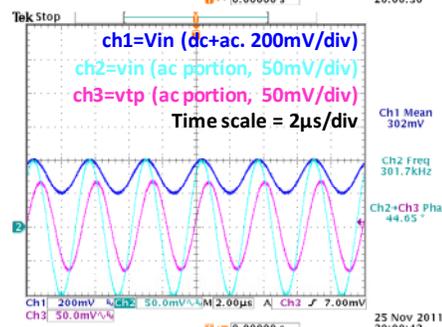
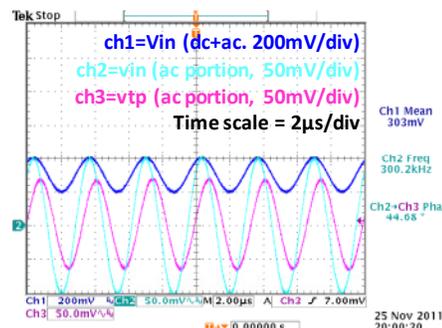
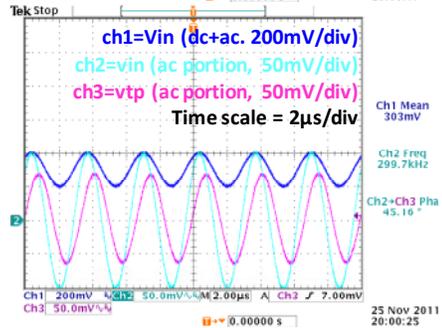
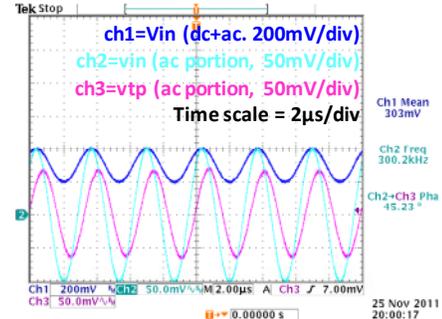
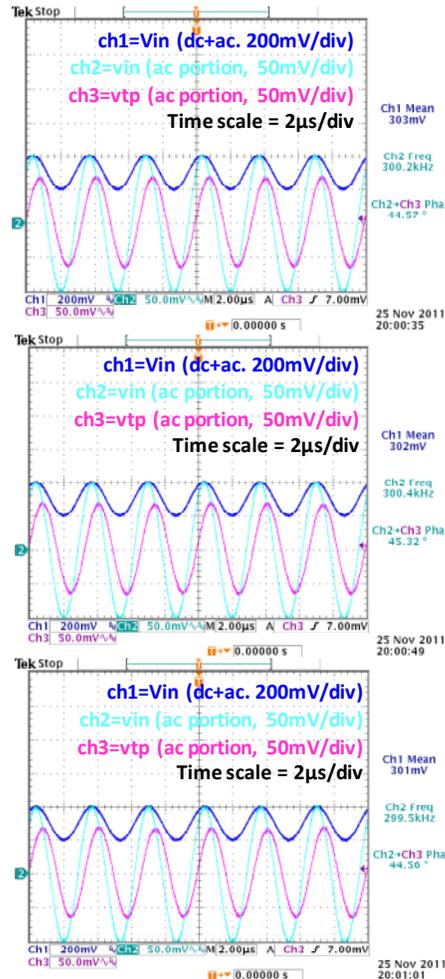


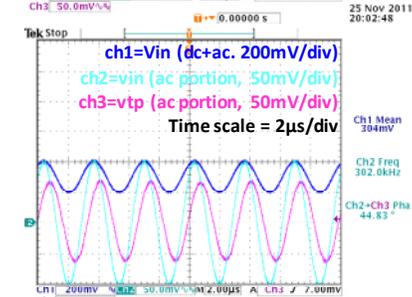
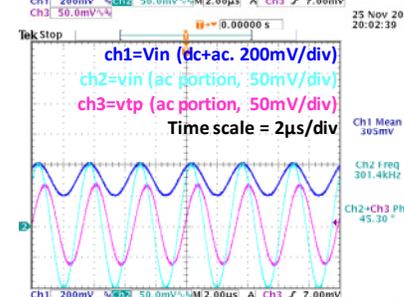
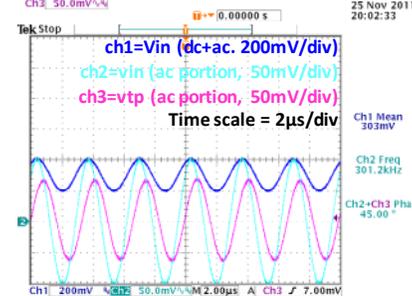
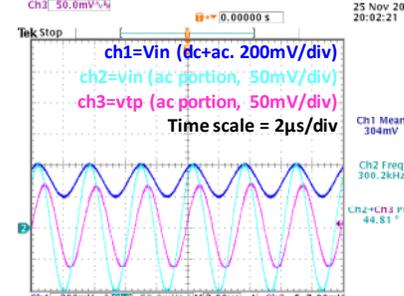
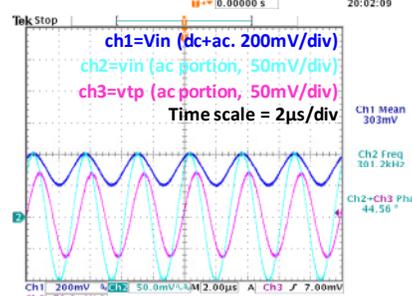
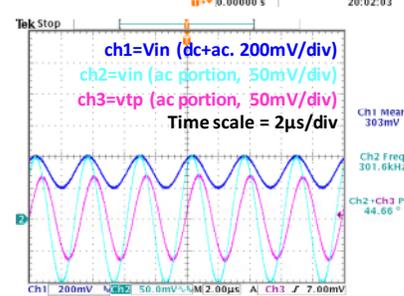
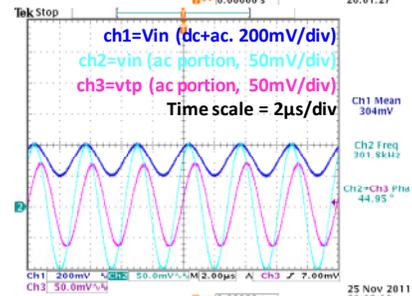
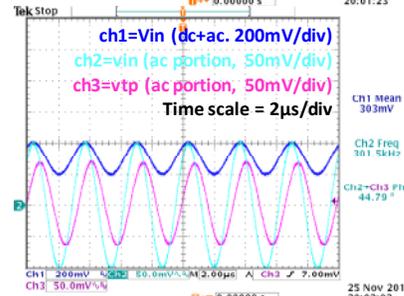
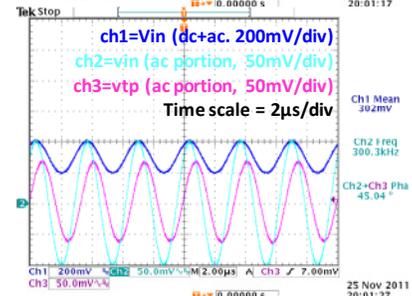
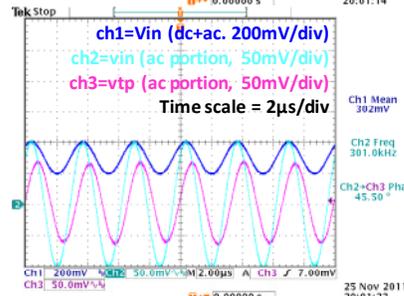
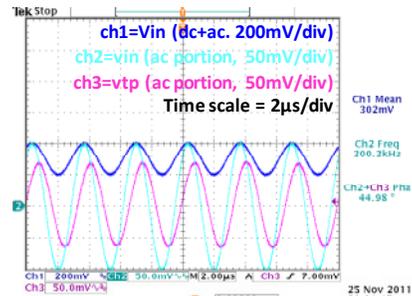
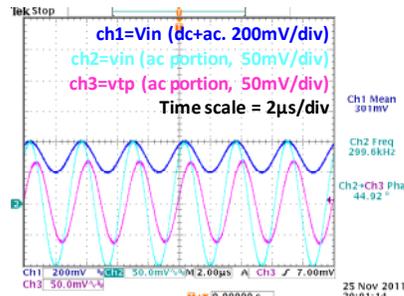
# Measurements at **PADONLY** point with **VBIAS=0.3V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.23 | 3.002E+05 | 1.14E-11 |
| 2          | 45.16 | 2.997E+05 | 1.14E-11 |
| 3          | 44.68 | 3.002E+05 | 1.12E-11 |
| 4          | 45.57 | 3.002E+05 | 1.15E-11 |
| 5          | 44.65 | 3.017E+05 | 1.11E-11 |
| 6          | 45.32 | 3.004E+05 | 1.14E-11 |
| 7          | 44.80 | 2.990E+05 | 1.13E-11 |
| 8          | 44.56 | 2.995E+05 | 1.11E-11 |
| 9          | 44.92 | 2.996E+05 | 1.13E-11 |
| 10         | 44.98 | 3.003E+05 | 1.13E-11 |
| 11         | 45.50 | 3.010E+05 | 1.15E-11 |
| 12         | 45.04 | 3.003E+05 | 1.13E-11 |
| 13         | 44.79 | 3.015E+05 | 1.12E-11 |
| 14         | 44.95 | 3.018E+05 | 1.12E-11 |
| 15         | 44.66 | 3.016E+05 | 1.11E-11 |
| 16         | 44.56 | 3.012E+05 | 1.11E-11 |
| 17         | 44.81 | 3.002E+05 | 1.12E-11 |
| 18         | 45.00 | 3.012E+05 | 1.12E-11 |
| 19         | 45.30 | 3.014E+05 | 1.14E-11 |
| 20         | 44.83 | 3.020E+05 | 1.12E-11 |

Average 44.97 3.007E+05 1.126E-11  
 STD 0.30 8.685E+02 1.253E-13



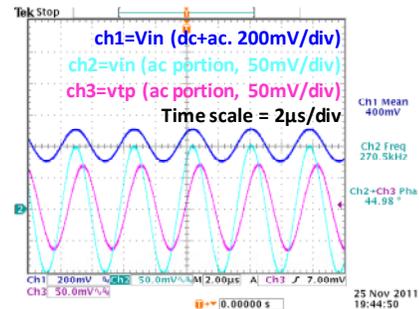
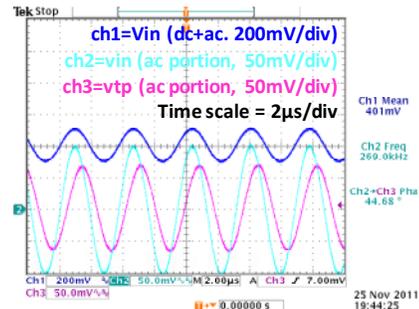
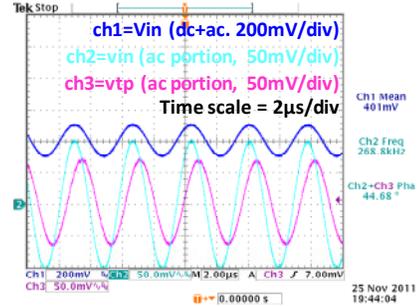
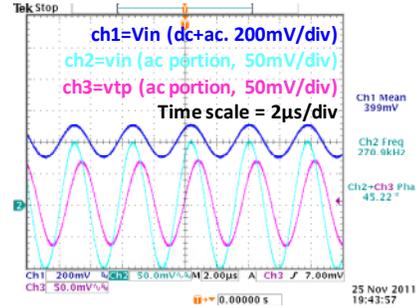
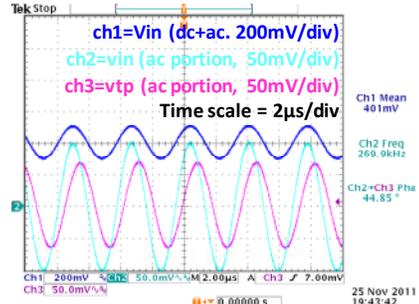
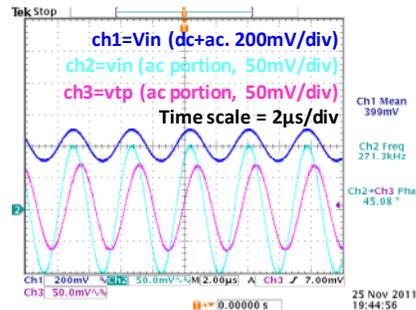
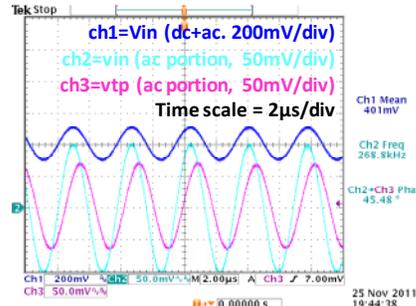
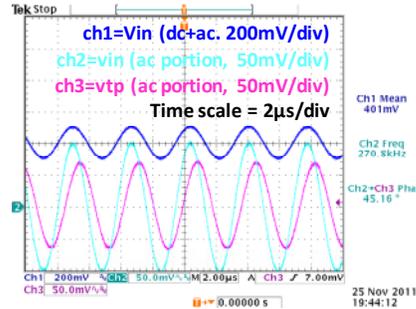


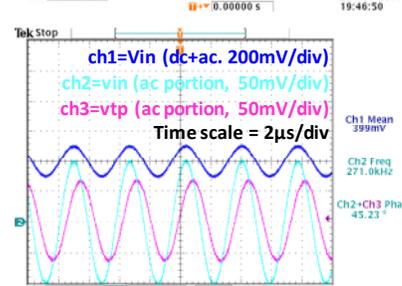
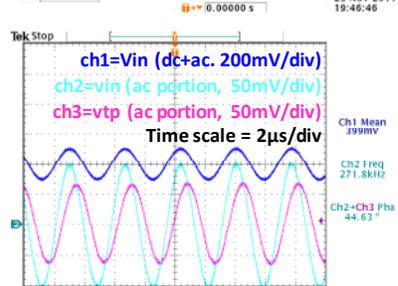
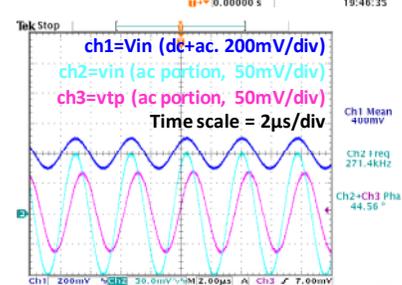
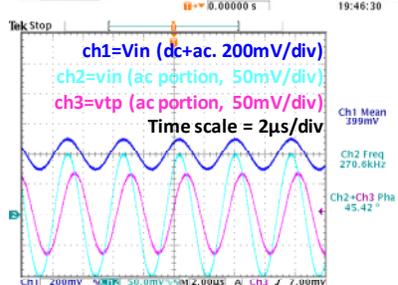
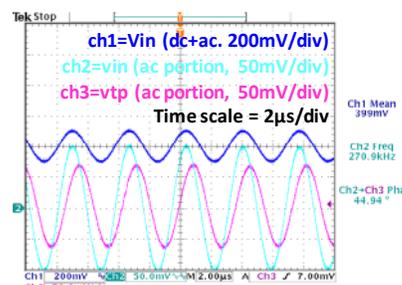
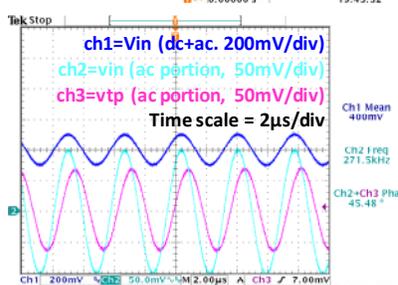
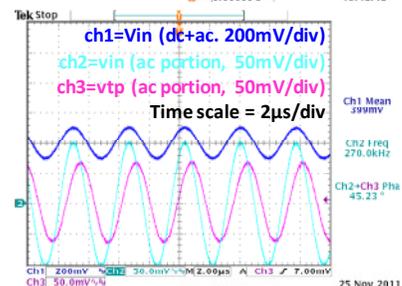
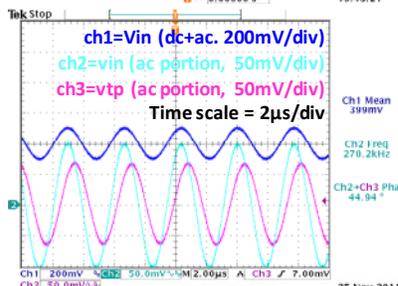
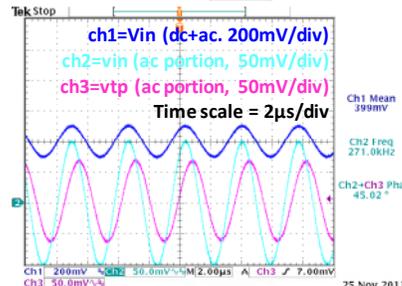
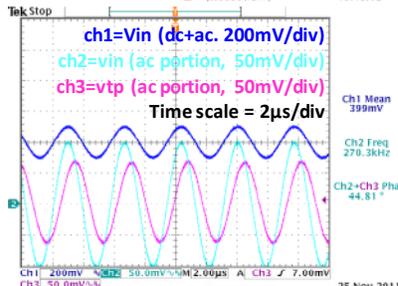
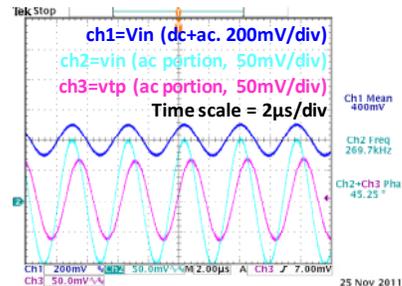
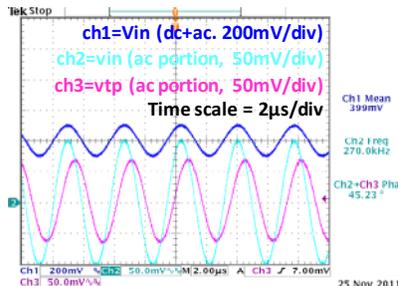
# Measurements at **NoQFG** point with **VBIAS=0.4V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.85 | 2.699E+05 | 1.25E-11 |
| 2          | 45.22 | 2.709E+05 | 1.26E-11 |
| 3          | 44.68 | 2.688E+05 | 1.25E-11 |
| 4          | 45.16 | 2.708E+05 | 1.26E-11 |
| 5          | 44.68 | 2.690E+05 | 1.25E-11 |
| 6          | 45.48 | 2.688E+05 | 1.28E-11 |
| 7          | 44.98 | 2.705E+05 | 1.25E-11 |
| 8          | 45.08 | 2.713E+05 | 1.25E-11 |
| 9          | 45.23 | 2.700E+05 | 1.27E-11 |
| 10         | 45.25 | 2.687E+05 | 1.27E-11 |
| 11         | 44.81 | 2.703E+05 | 1.25E-11 |
| 12         | 45.02 | 2.710E+05 | 1.25E-11 |
| 13         | 44.94 | 2.702E+05 | 1.25E-11 |
| 14         | 45.11 | 2.699E+05 | 1.26E-11 |
| 15         | 45.48 | 2.715E+05 | 1.27E-11 |
| 16         | 44.94 | 2.709E+05 | 1.25E-11 |
| 17         | 45.42 | 2.706E+05 | 1.27E-11 |
| 18         | 44.56 | 2.714E+05 | 1.23E-11 |
| 19         | 44.63 | 2.718E+05 | 1.23E-11 |
| 20         | 45.23 | 2.710E+05 | 1.26E-11 |

Average 45.04 2.704E+05 1.255E-11  
 STD 0.28 9.477E+02 1.315E-13



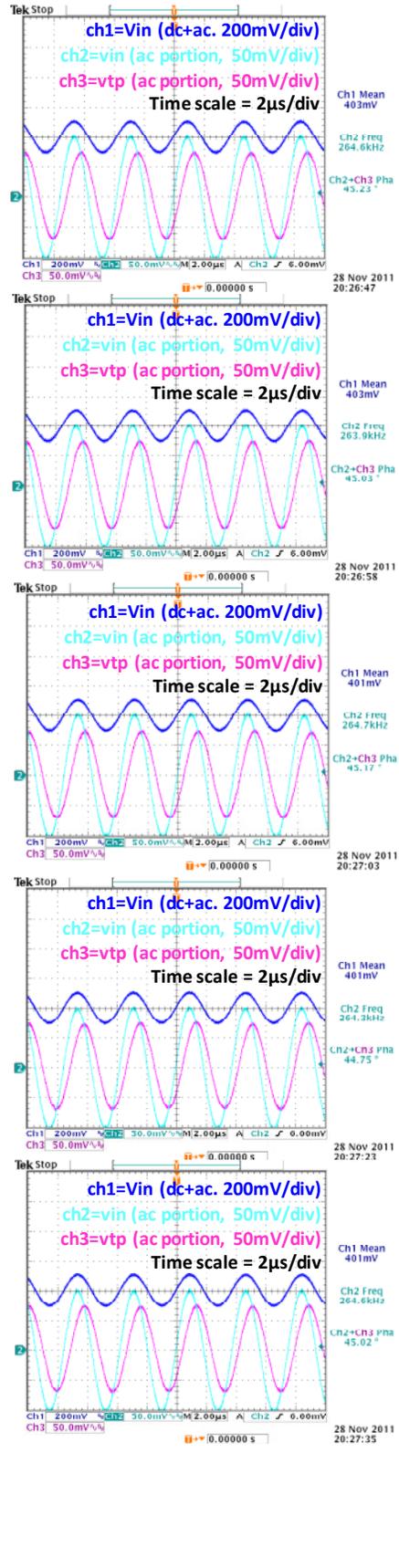
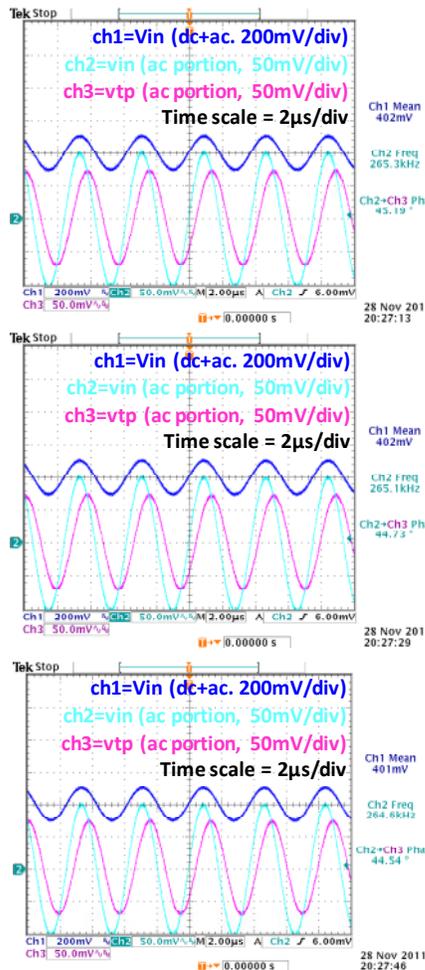


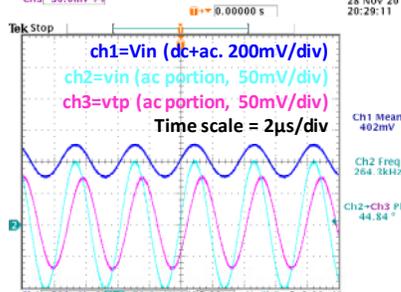
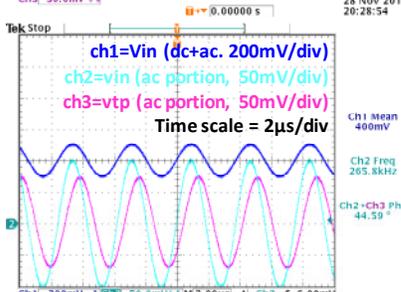
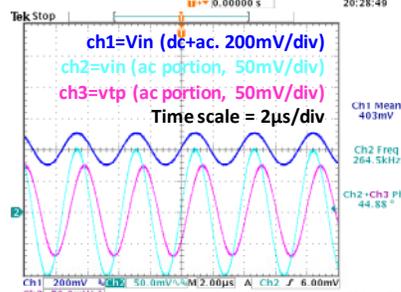
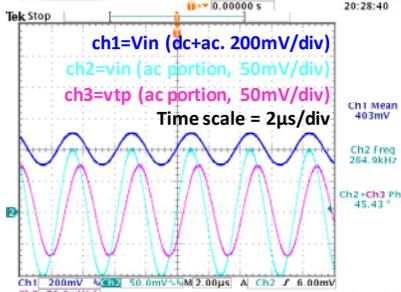
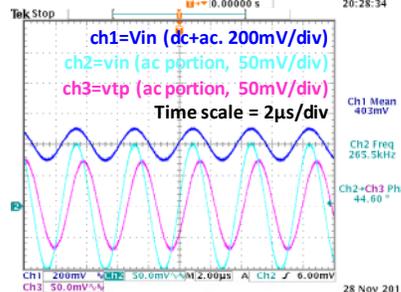
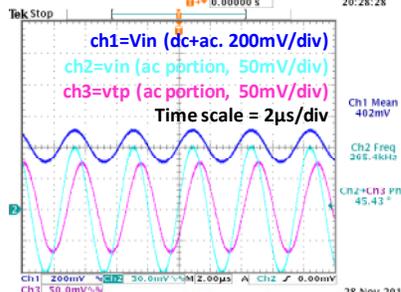
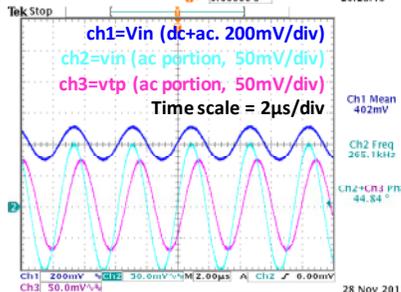
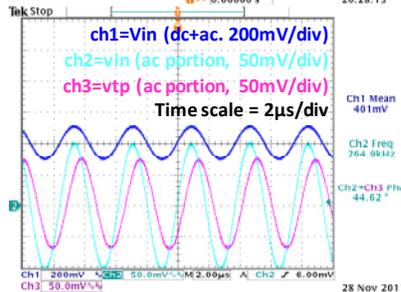
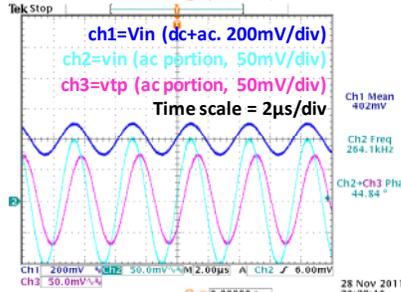
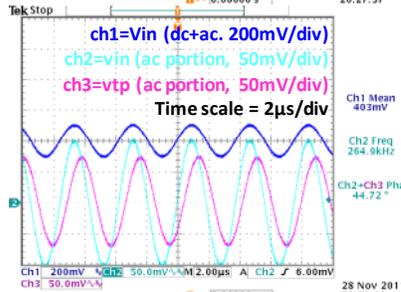
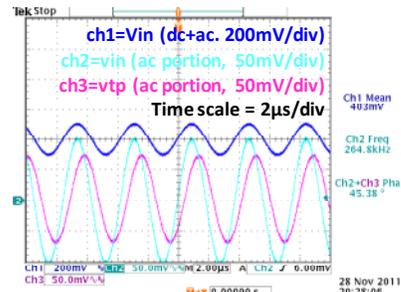
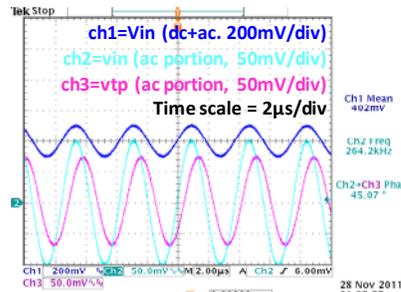
# Measurements at QFG point with VBIAS=0.4V

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.23 | 2.646E+05 | 1.29E-11 |
| 2          | 45.03 | 2.639E+05 | 1.29E-11 |
| 3          | 45.17 | 2.647E+05 | 1.29E-11 |
| 4          | 45.19 | 2.653E+05 | 1.29E-11 |
| 5          | 44.75 | 2.643E+05 | 1.27E-11 |
| 6          | 44.73 | 2.651E+05 | 1.27E-11 |
| 7          | 45.02 | 2.644E+05 | 1.28E-11 |
| 8          | 44.54 | 2.646E+05 | 1.26E-11 |
| 9          | 45.07 | 2.642E+05 | 1.29E-11 |
| 10         | 45.38 | 2.648E+05 | 1.30E-11 |
| 11         | 44.72 | 2.649E+05 | 1.27E-11 |
| 12         | 44.84 | 2.641E+05 | 1.28E-11 |
| 13         | 44.62 | 2.649E+05 | 1.26E-11 |
| 14         | 44.84 | 2.651E+05 | 1.27E-11 |
| 15         | 45.43 | 2.654E+05 | 1.30E-11 |
| 16         | 44.60 | 2.655E+05 | 1.26E-11 |
| 17         | 45.43 | 2.649E+05 | 1.30E-11 |
| 18         | 44.88 | 2.645E+05 | 1.28E-11 |
| 19         | 44.59 | 2.658E+05 | 1.26E-11 |
| 20         | 44.84 | 2.643E+05 | 1.27E-11 |

Average 44.95 2.648E+05 1.277E-11  
 STD 0.29 5.019E+02 1.322E-13



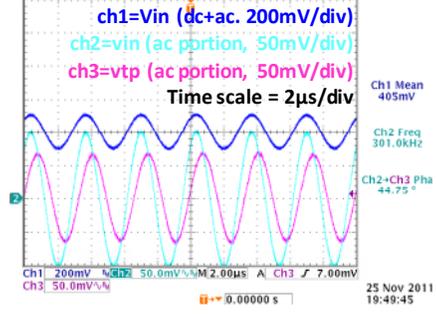
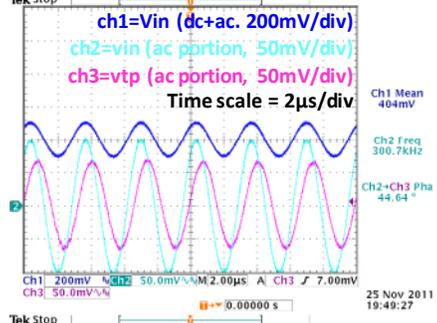
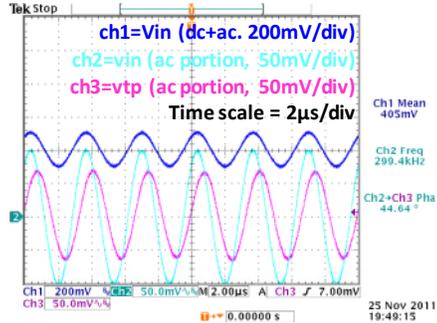
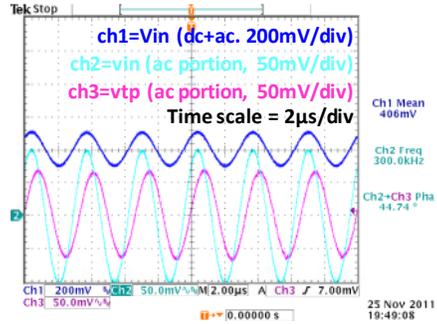
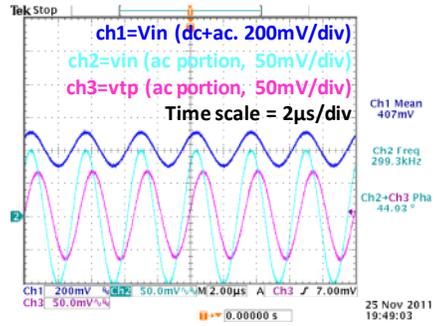
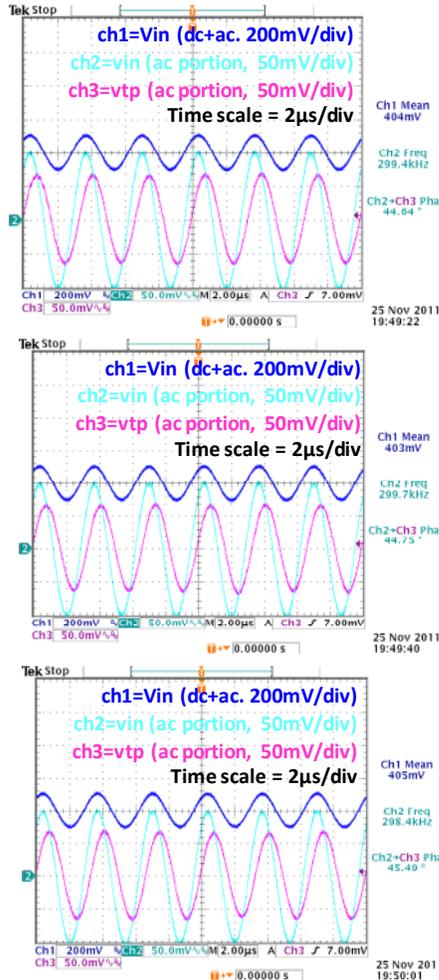


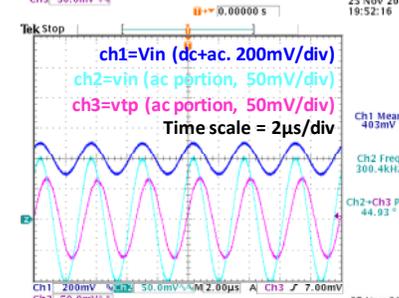
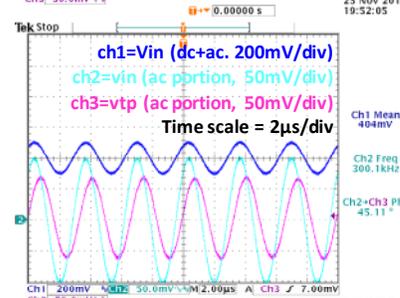
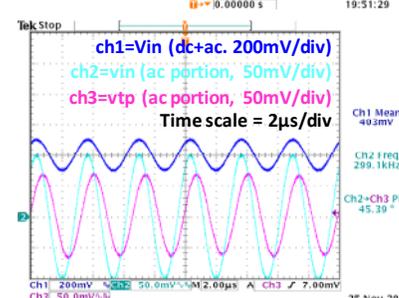
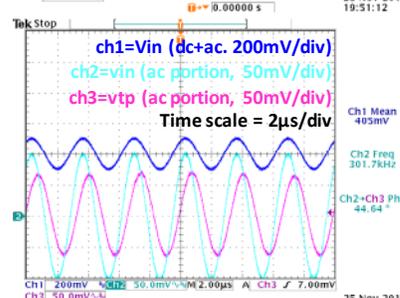
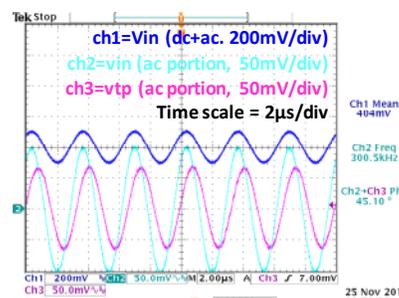
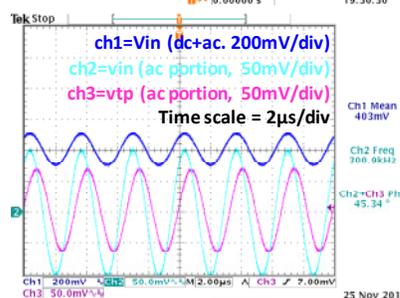
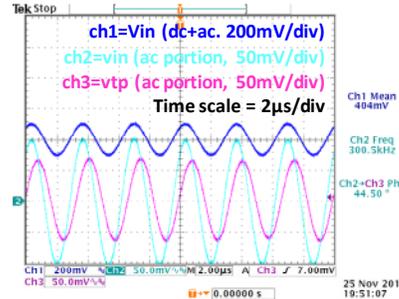
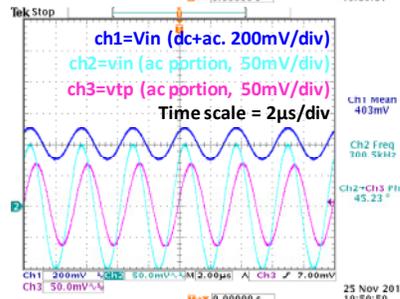
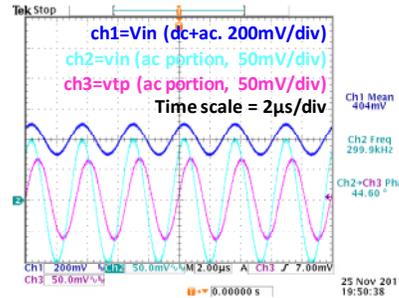
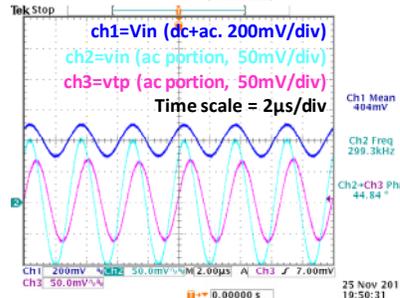
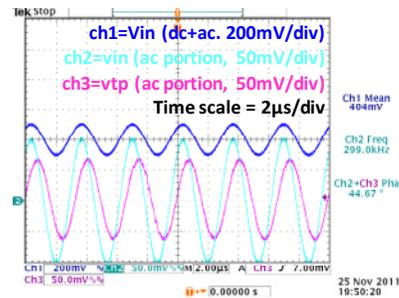
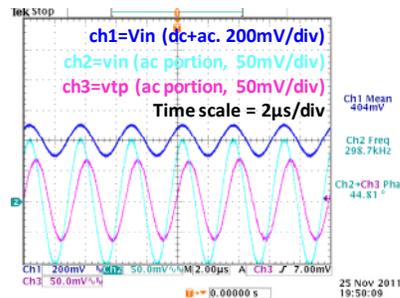
# Measurements at **PADONLY** point with **VBIAS=0.4V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.93 | 2.993E+05 | 1.13E-11 |
| 2          | 44.74 | 3.000E+05 | 1.12E-11 |
| 3          | 44.64 | 2.994E+05 | 1.12E-11 |
| 4          | 44.64 | 3.007E+05 | 1.11E-11 |
| 5          | 44.64 | 3.007E+05 | 1.11E-11 |
| 6          | 44.75 | 2.997E+05 | 1.12E-11 |
| 7          | 44.75 | 3.010E+05 | 1.12E-11 |
| 8          | 45.49 | 2.984E+05 | 1.16E-11 |
| 9          | 44.81 | 2.987E+05 | 1.13E-11 |
| 10         | 44.67 | 2.990E+05 | 1.12E-11 |
| 11         | 44.84 | 2.993E+05 | 1.13E-11 |
| 12         | 44.60 | 2.999E+05 | 1.11E-11 |
| 13         | 45.23 | 3.005E+05 | 1.14E-11 |
| 14         | 44.50 | 3.005E+05 | 1.11E-11 |
| 15         | 45.34 | 3.009E+05 | 1.14E-11 |
| 16         | 45.10 | 3.005E+05 | 1.13E-11 |
| 17         | 44.64 | 3.017E+05 | 1.11E-11 |
| 18         | 45.39 | 2.991E+05 | 1.15E-11 |
| 19         | 45.11 | 3.001E+05 | 1.13E-11 |
| 20         | 44.93 | 3.004E+05 | 1.13E-11 |

Average 44.89 3.000E+05 **1.125E-11**  
 STD 0.29 8.614E+02 **1.278E-13**



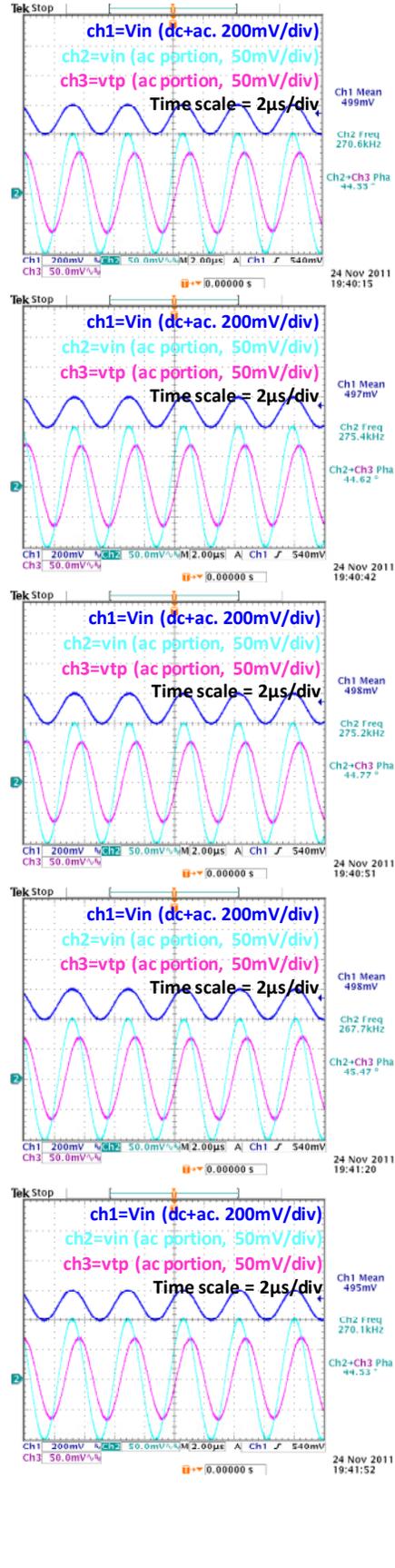
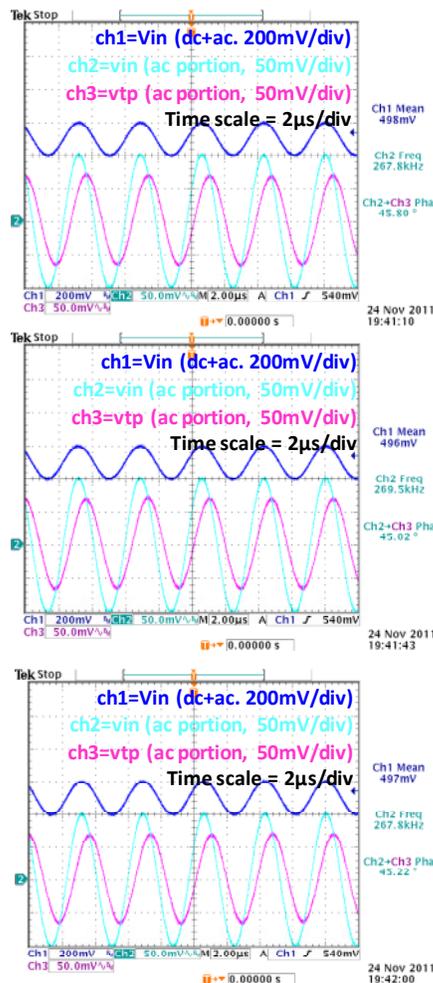


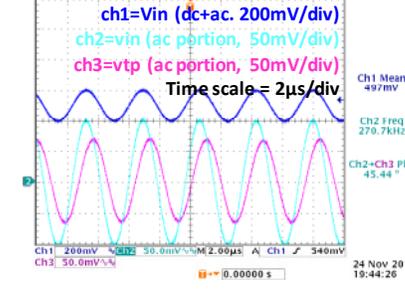
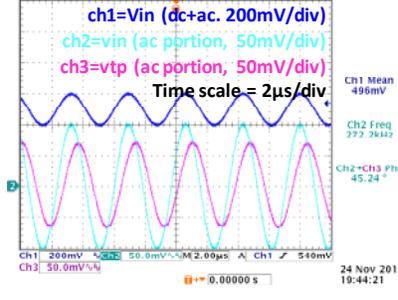
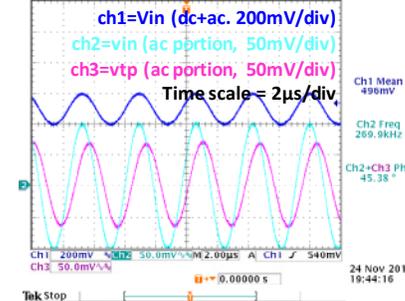
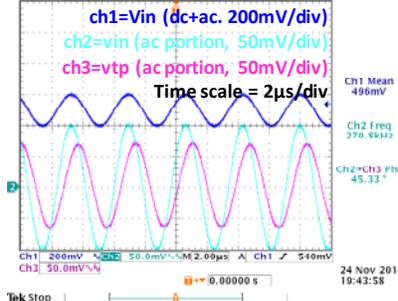
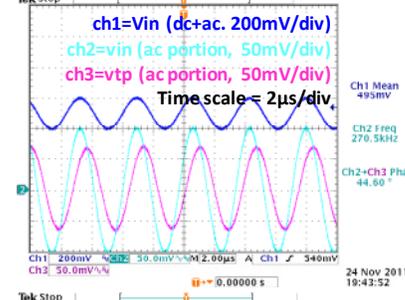
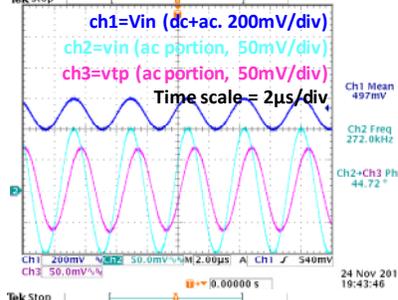
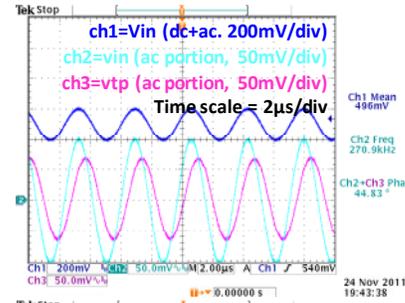
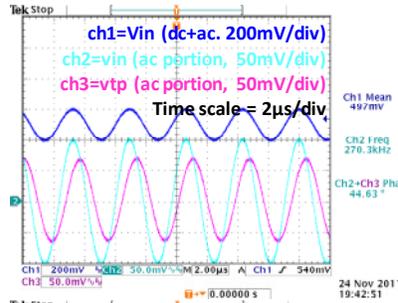
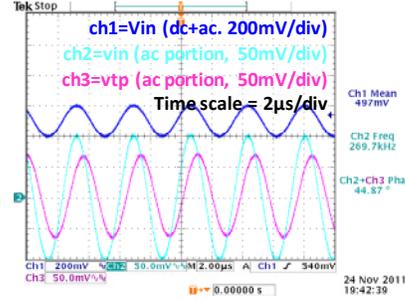
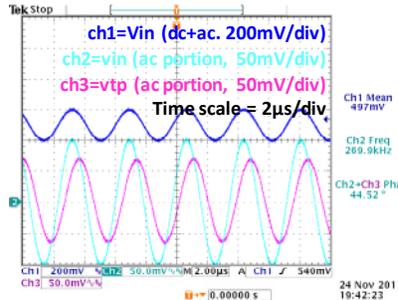
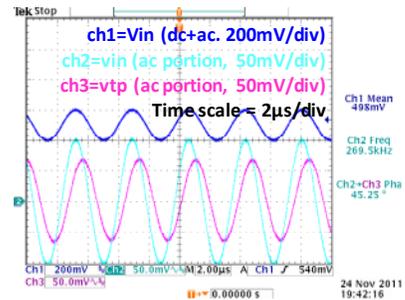
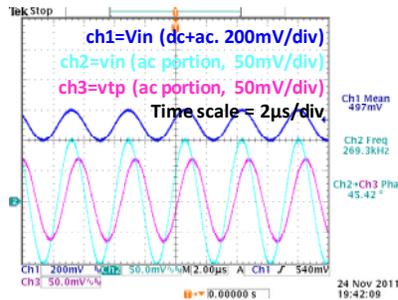
# Measurements at **NoQFG** point with **VBIAS=0.5V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.55 | 2.706E+05 | 1.23E-11 |
| 2          | 44.62 | 2.754E+05 | 1.21E-11 |
| 3          | 44.77 | 2.752E+05 | 1.22E-11 |
| 4          | 45.80 | 2.678E+05 | 1.30E-11 |
| 5          | 45.47 | 2.677E+05 | 1.29E-11 |
| 6          | 45.02 | 2.695E+05 | 1.26E-11 |
| 7          | 44.53 | 2.701E+05 | 1.23E-11 |
| 8          | 45.22 | 2.678E+05 | 1.28E-11 |
| 9          | 45.42 | 2.693E+05 | 1.28E-11 |
| 10         | 45.25 | 2.699E+05 | 1.27E-11 |
| 11         | 44.52 | 2.699E+05 | 1.23E-11 |
| 12         | 44.87 | 2.697E+05 | 1.25E-11 |
| 13         | 44.63 | 2.703E+05 | 1.24E-11 |
| 14         | 44.83 | 2.709E+05 | 1.24E-11 |
| 15         | 44.60 | 2.705E+05 | 1.24E-11 |
| 16         | 45.33 | 2.708E+05 | 1.27E-11 |
| 17         | 45.38 | 2.699E+05 | 1.27E-11 |
| 18         | 45.24 | 2.722E+05 | 1.26E-11 |
| 19         | 45.44 | 2.707E+05 | 1.27E-11 |
| 20         | 44.63 | 2.713E+05 | 1.23E-11 |

Average 45.01 2.705E+05 **1.253E-11**  
 STD 0.40 2.017E+03 **3.328E-13**



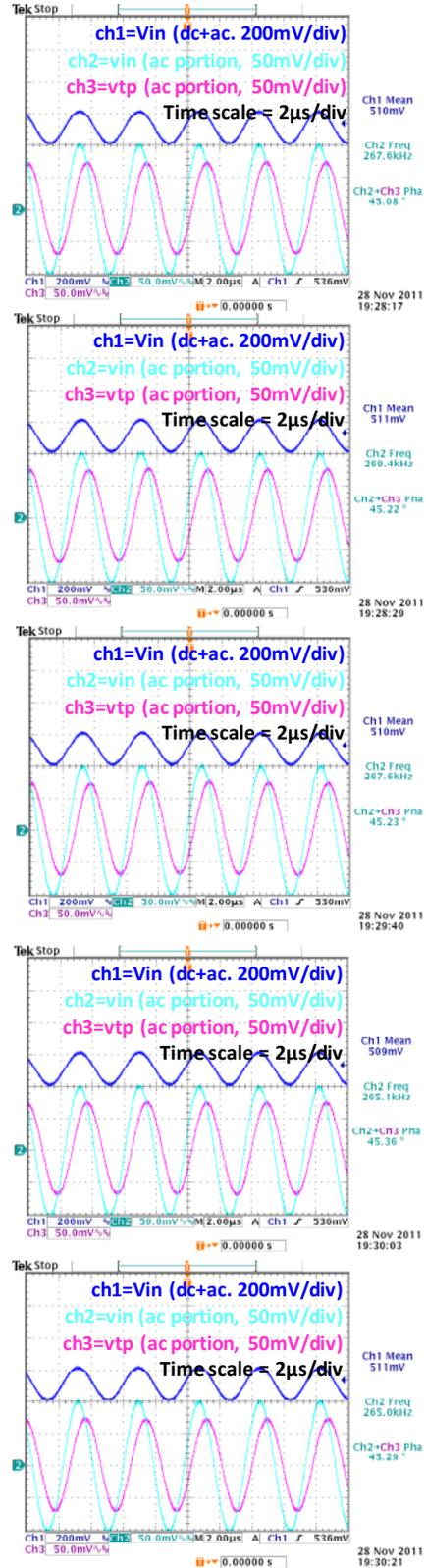
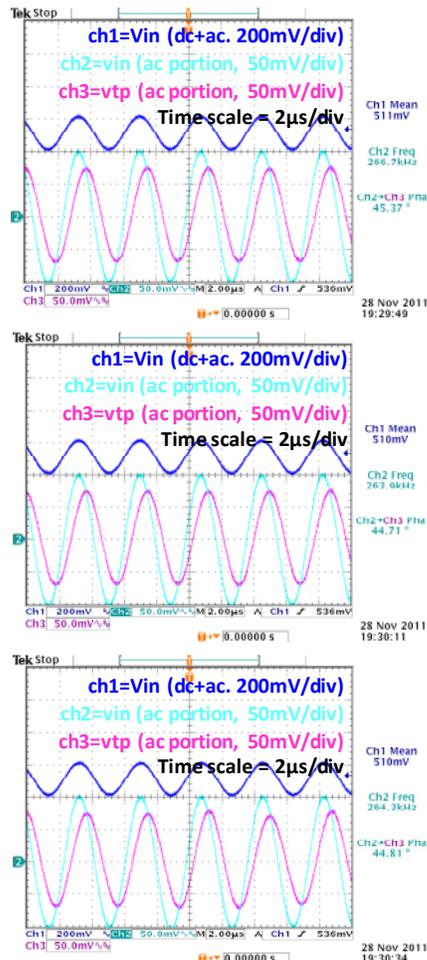


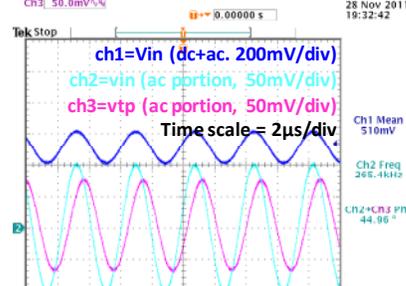
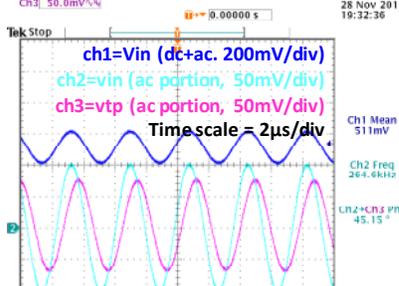
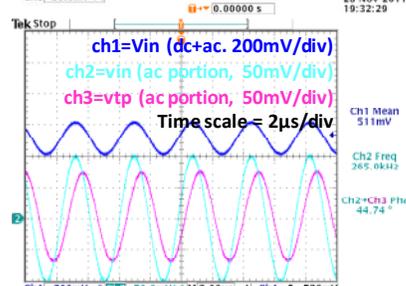
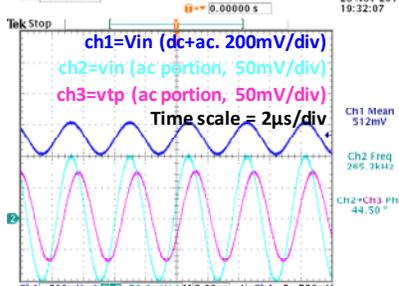
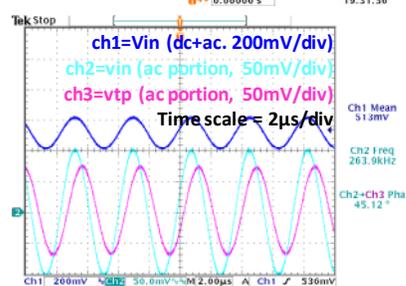
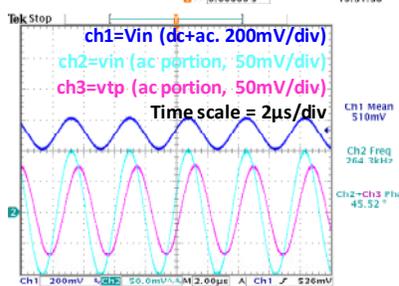
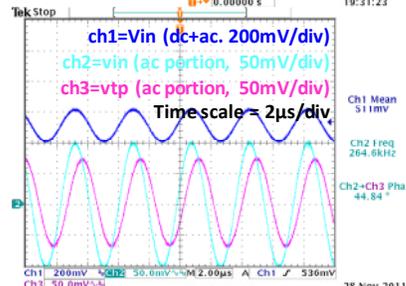
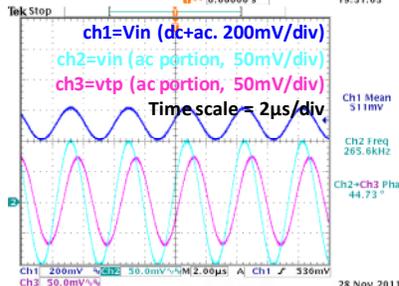
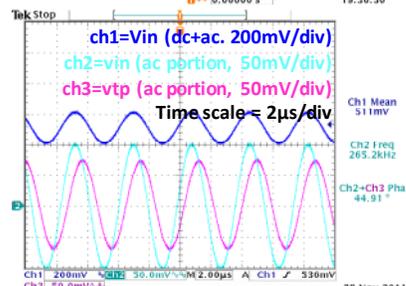
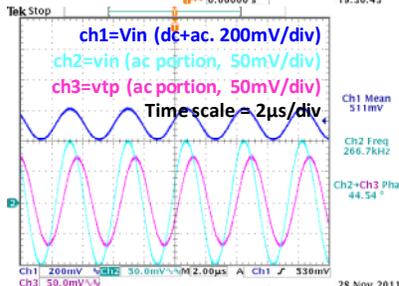
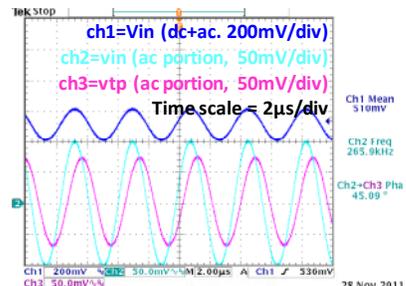
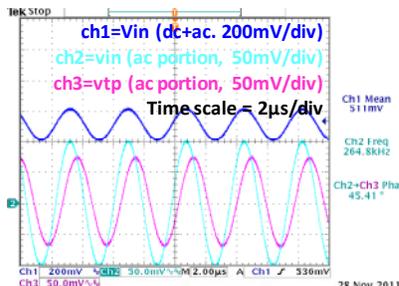
# Measurements at QFG point with **VBIAS=0.5V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.08 | 2.676E+05 | 1.27E-11 |
| 2          | 45.22 | 2.694E+05 | 1.27E-11 |
| 3          | 45.23 | 2.677E+05 | 1.28E-11 |
| 4          | 45.37 | 2.667E+05 | 1.29E-11 |
| 5          | 45.36 | 2.651E+05 | 1.29E-11 |
| 6          | 44.71 | 2.639E+05 | 1.27E-11 |
| 7          | 45.29 | 2.650E+05 | 1.29E-11 |
| 8          | 44.81 | 2.643E+05 | 1.27E-11 |
| 9          | 45.41 | 2.648E+05 | 1.30E-11 |
| 10         | 45.09 | 2.659E+05 | 1.28E-11 |
| 11         | 44.54 | 2.667E+05 | 1.25E-11 |
| 12         | 44.91 | 2.652E+05 | 1.27E-11 |
| 13         | 44.73 | 2.656E+05 | 1.26E-11 |
| 14         | 44.84 | 2.646E+05 | 1.27E-11 |
| 15         | 45.52 | 2.643E+05 | 1.31E-11 |
| 16         | 45.12 | 2.639E+05 | 1.29E-11 |
| 17         | 44.50 | 2.653E+05 | 1.26E-11 |
| 18         | 44.74 | 2.650E+05 | 1.27E-11 |
| 19         | 45.15 | 2.646E+05 | 1.29E-11 |
| 20         | 44.96 | 2.654E+05 | 1.27E-11 |

Average 45.03 2.656E+05 **1.277E-11**  
 STD 0.30 1.421E+03 **1.417E-13**



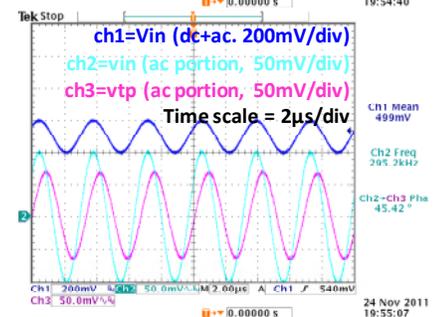
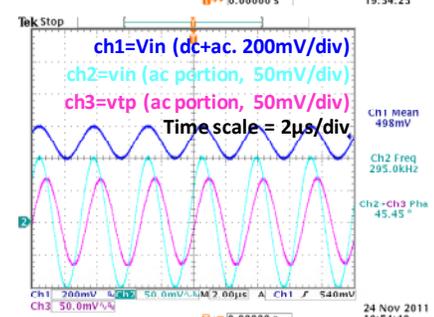
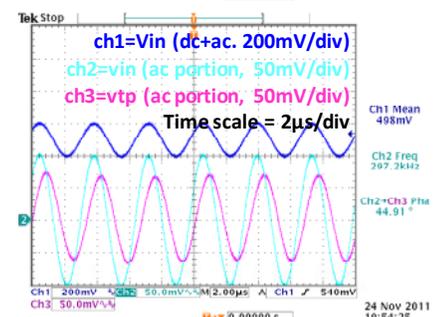
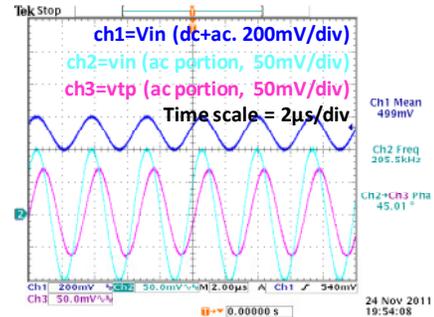
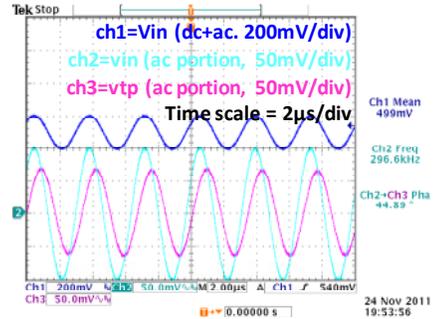
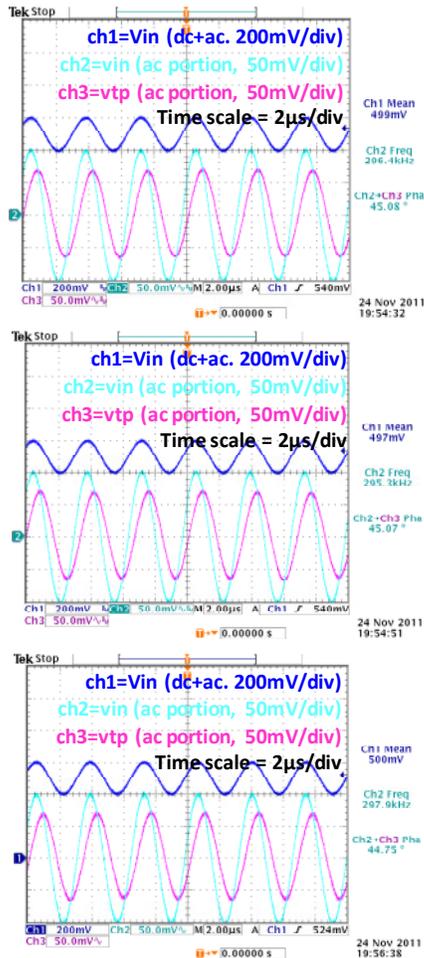


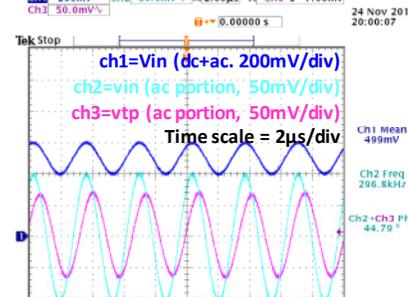
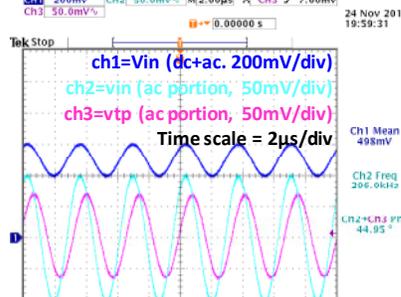
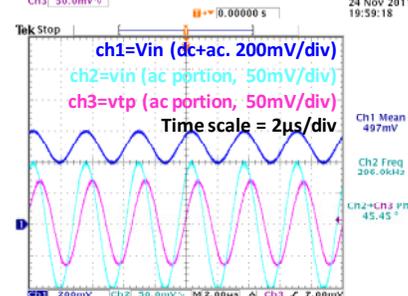
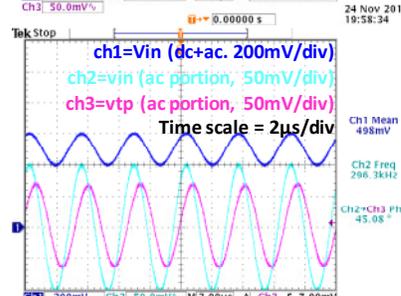
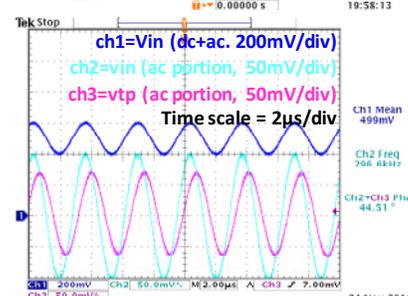
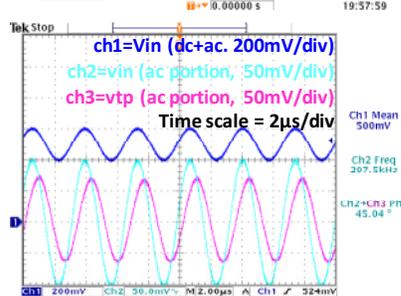
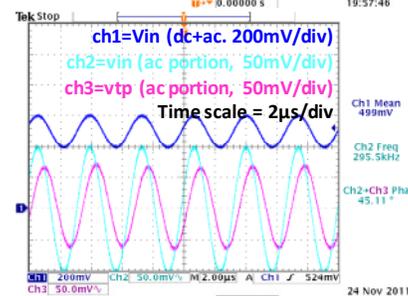
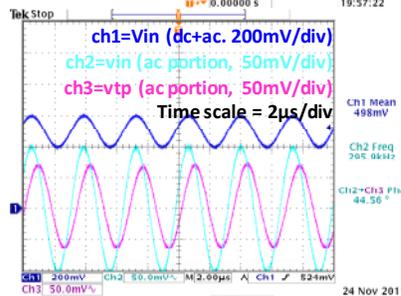
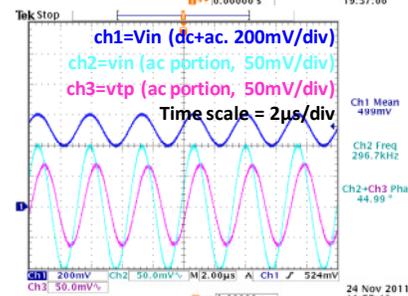
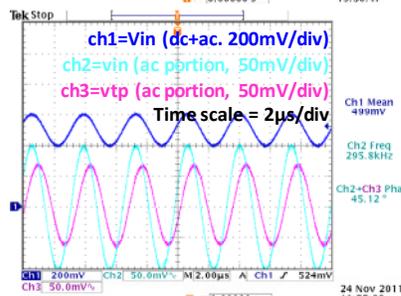
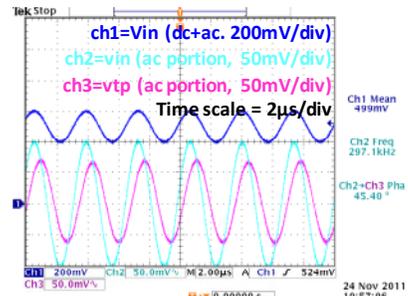
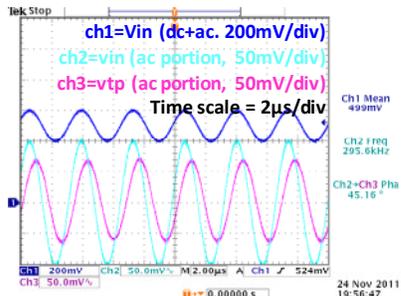
# Measurements at **PADONLY** point with **VBIAS=0.5V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.89 | 2.966E+05 | 1.14E-11 |
| 2          | 45.01 | 2.955E+05 | 1.15E-11 |
| 3          | 44.91 | 2.972E+05 | 1.14E-11 |
| 4          | 45.08 | 2.964E+05 | 1.15E-11 |
| 5          | 45.45 | 2.950E+05 | 1.17E-11 |
| 6          | 45.07 | 2.953E+05 | 1.15E-11 |
| 7          | 45.42 | 2.952E+05 | 1.16E-11 |
| 8          | 44.75 | 2.979E+05 | 1.13E-11 |
| 9          | 45.16 | 2.956E+05 | 1.15E-11 |
| 10         | 45.40 | 2.971E+05 | 1.16E-11 |
| 11         | 45.12 | 2.958E+05 | 1.15E-11 |
| 12         | 44.99 | 2.967E+05 | 1.14E-11 |
| 13         | 44.56 | 2.955E+05 | 1.13E-11 |
| 14         | 45.04 | 2.975E+05 | 1.14E-11 |
| 15         | 45.51 | 2.966E+05 | 1.16E-11 |
| 16         | 45.08 | 2.963E+05 | 1.15E-11 |
| 17         | 45.45 | 2.960E+05 | 1.16E-11 |
| 18         | 44.95 | 2.960E+05 | 1.14E-11 |
| 19         | 44.79 | 2.968E+05 | 1.13E-11 |
| 20         | 45.20 | 2.964E+05 | 1.15E-11 |

Average 45.09 2.963E+05 1.147E-11  
 STD 0.26 7.994E+02 1.155E-13



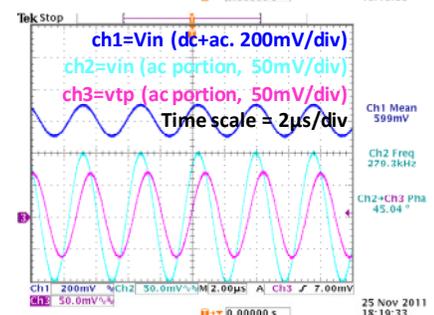
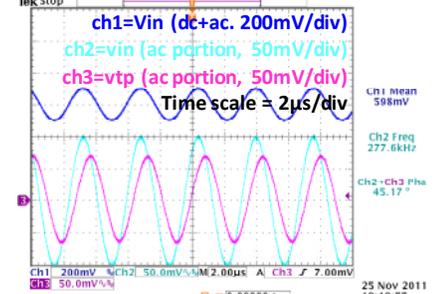
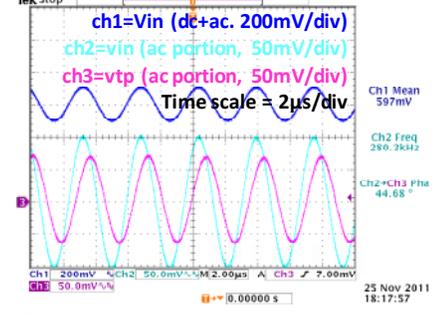
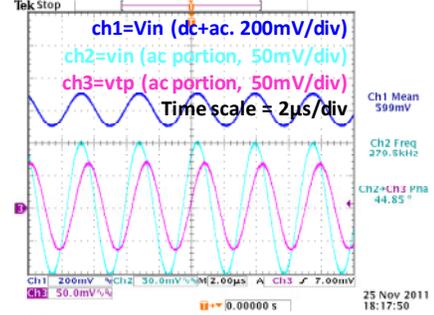
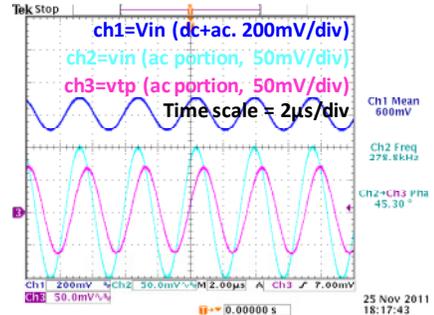
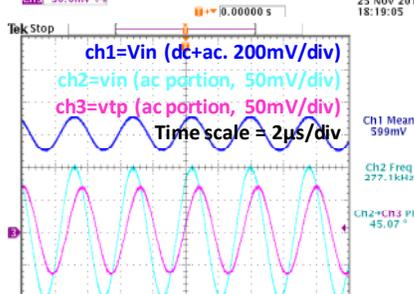
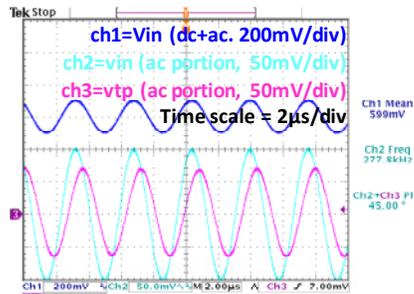
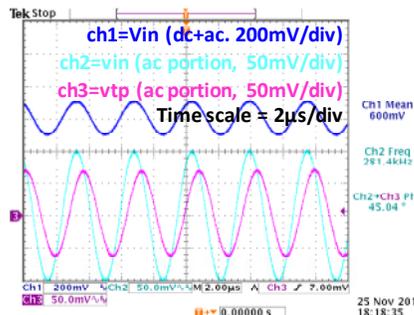


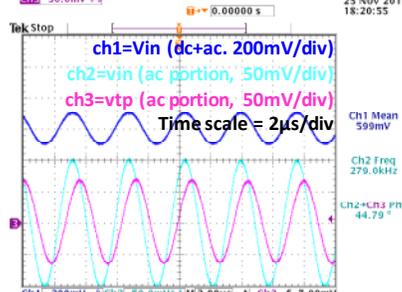
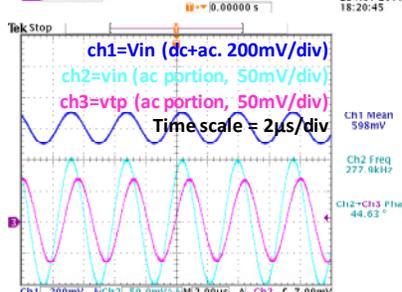
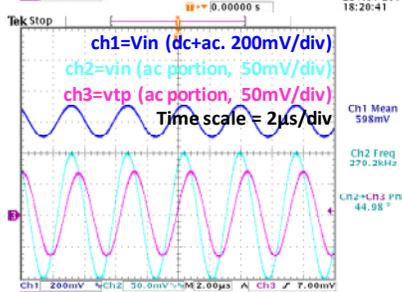
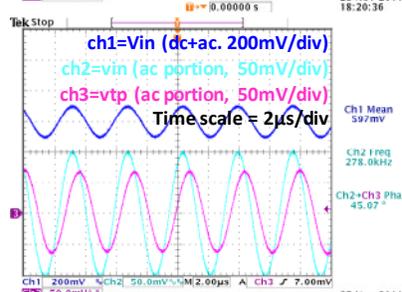
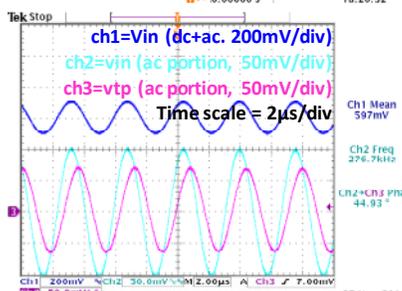
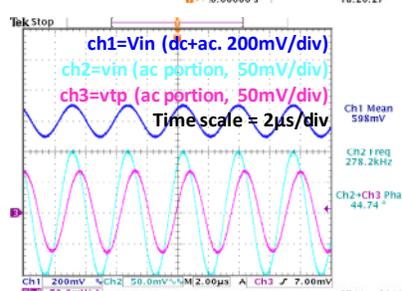
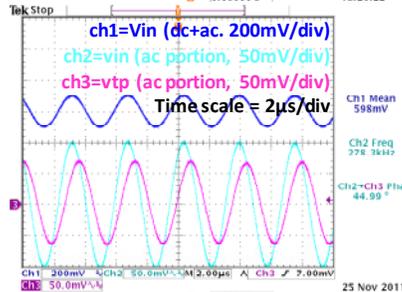
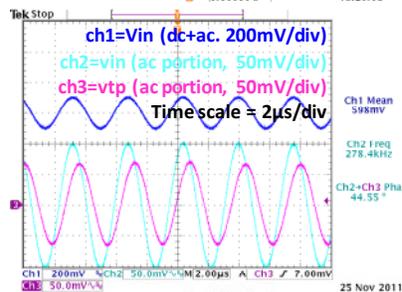
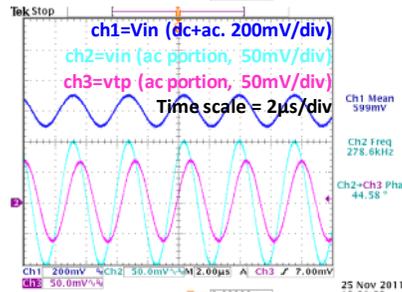
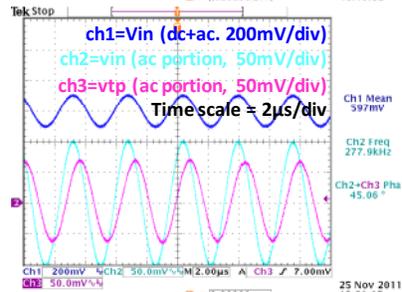
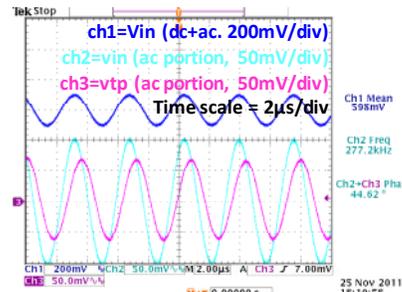
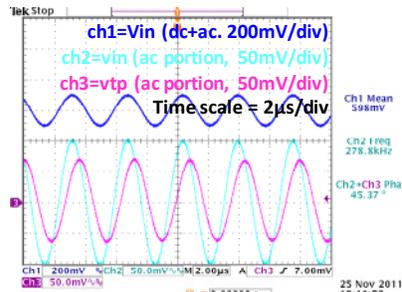
# Measurements at **NoQFG** point with **VBIAS=0.6V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.30 | 2.788E+05 | 1.23E-11 |
| 2          | 44.85 | 2.795E+05 | 1.21E-11 |
| 3          | 44.68 | 2.803E+05 | 1.20E-11 |
| 4          | 45.04 | 2.814E+05 | 1.21E-11 |
| 5          | 45.17 | 2.776E+05 | 1.23E-11 |
| 6          | 45.00 | 2.778E+05 | 1.22E-11 |
| 7          | 45.04 | 2.793E+05 | 1.21E-11 |
| 8          | 45.07 | 2.771E+05 | 1.23E-11 |
| 9          | 45.37 | 2.788E+05 | 1.23E-11 |
| 10         | 44.62 | 2.772E+05 | 1.21E-11 |
| 11         | 45.06 | 2.779E+05 | 1.22E-11 |
| 12         | 44.58 | 2.786E+05 | 1.20E-11 |
| 13         | 44.55 | 2.784E+05 | 1.20E-11 |
| 14         | 44.99 | 2.783E+05 | 1.22E-11 |
| 15         | 44.74 | 2.782E+05 | 1.21E-11 |
| 16         | 44.93 | 2.767E+05 | 1.22E-11 |
| 17         | 45.07 | 2.780E+05 | 1.22E-11 |
| 18         | 44.98 | 2.792E+05 | 1.21E-11 |
| 19         | 44.63 | 2.779E+05 | 1.20E-11 |
| 20         | 44.79 | 2.790E+05 | 1.21E-11 |

Average 44.92 2.785E+05 **1.213E-11**  
 STD 0.24 1.113E+03 **1.100E-13**



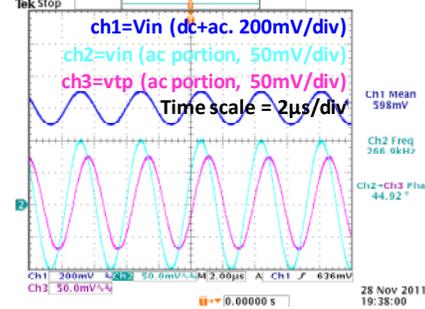
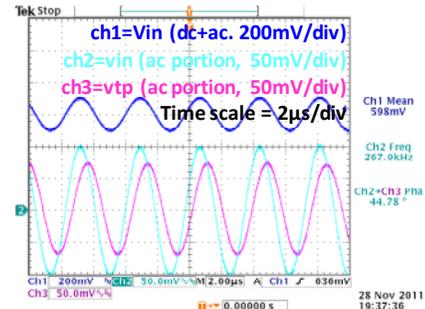
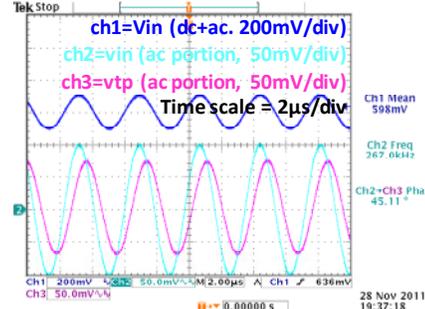
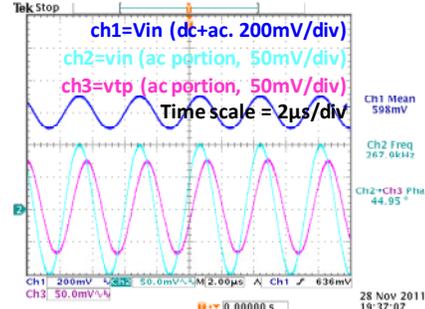
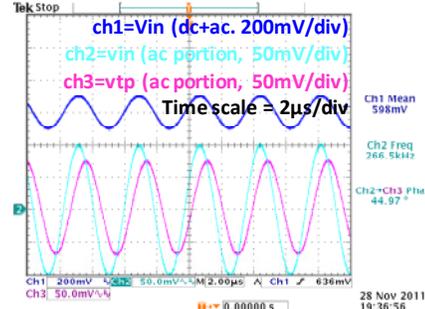
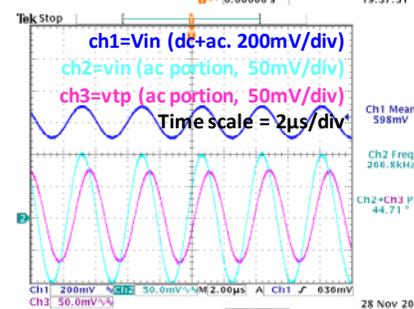
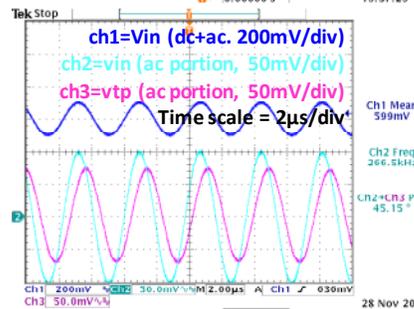
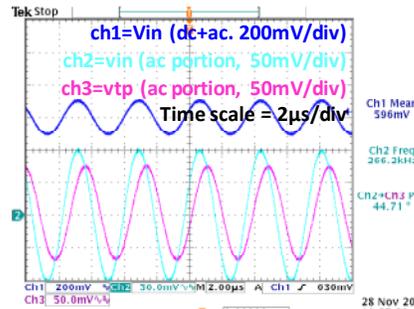


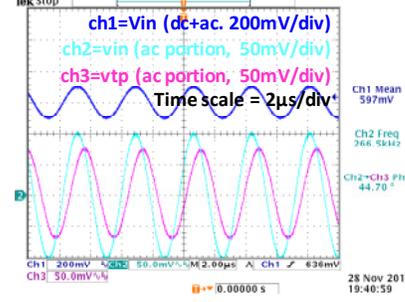
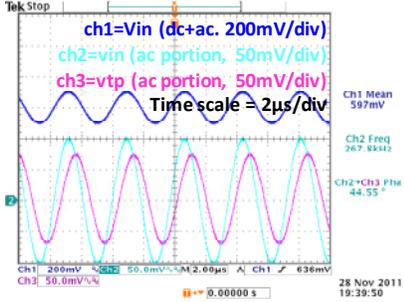
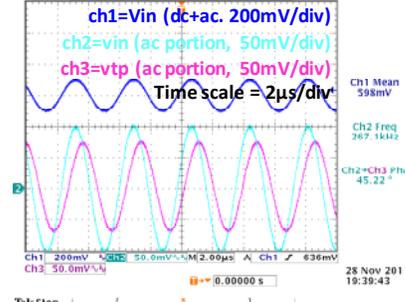
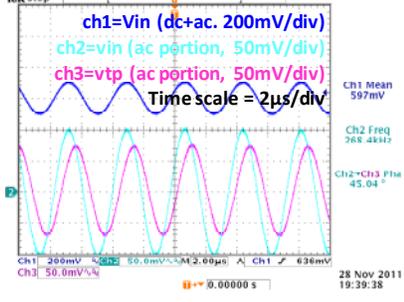
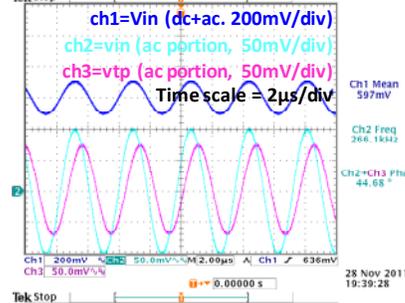
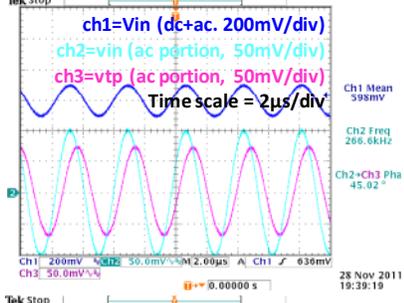
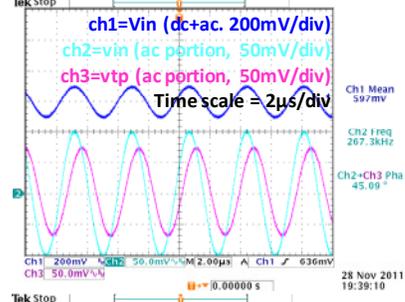
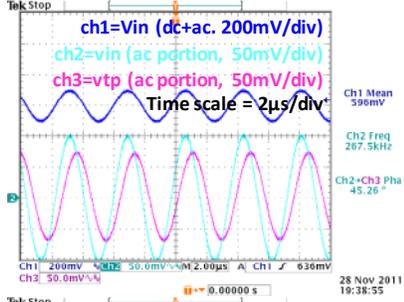
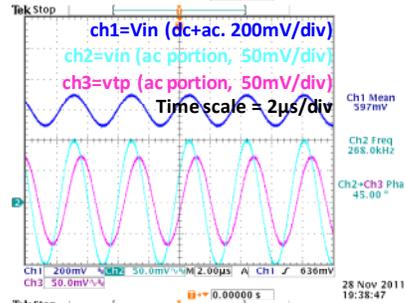
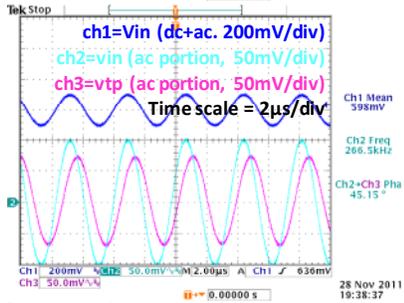
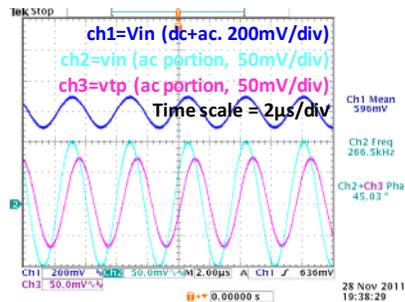
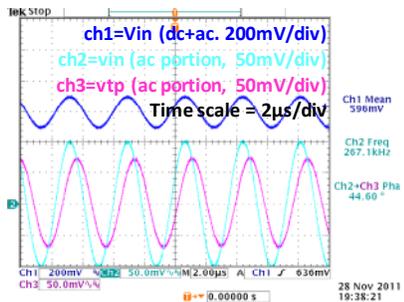
# Measurements at QFG point with VBIAS=0.6V

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.97 | 2.665E+05 | 1.27E-11 |
| 2          | 44.95 | 2.679E+05 | 1.26E-11 |
| 3          | 45.11 | 2.670E+05 | 1.27E-11 |
| 4          | 44.71 | 2.662E+05 | 1.26E-11 |
| 5          | 44.78 | 2.670E+05 | 1.26E-11 |
| 6          | 45.15 | 2.665E+05 | 1.28E-11 |
| 7          | 44.92 | 2.669E+05 | 1.27E-11 |
| 8          | 44.71 | 2.668E+05 | 1.26E-11 |
| 9          | 44.60 | 2.671E+05 | 1.25E-11 |
| 10         | 45.03 | 2.665E+05 | 1.27E-11 |
| 11         | 45.15 | 2.665E+05 | 1.28E-11 |
| 12         | 45.00 | 2.680E+05 | 1.26E-11 |
| 13         | 45.26 | 2.675E+05 | 1.28E-11 |
| 14         | 45.09 | 2.673E+05 | 1.27E-11 |
| 15         | 45.02 | 2.666E+05 | 1.27E-11 |
| 16         | 44.68 | 2.661E+05 | 1.26E-11 |
| 17         | 45.04 | 2.684E+05 | 1.26E-11 |
| 18         | 45.22 | 2.671E+05 | 1.28E-11 |
| 19         | 44.55 | 2.678E+05 | 1.25E-11 |
| 20         | 44.70 | 2.665E+05 | 1.26E-11 |

Average 44.93 2.670E+05 1.266E-11  
 STD 0.21 6.357E+02 9.494E-14



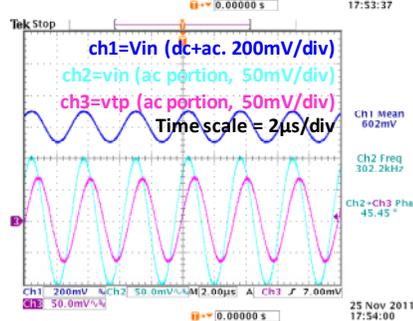
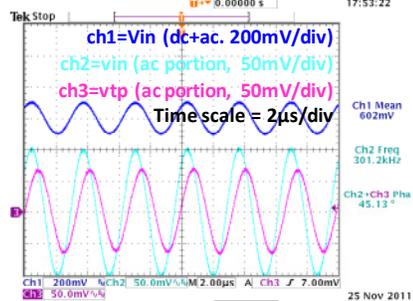
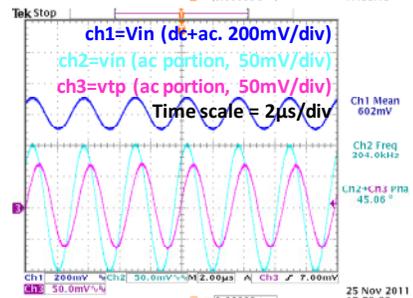
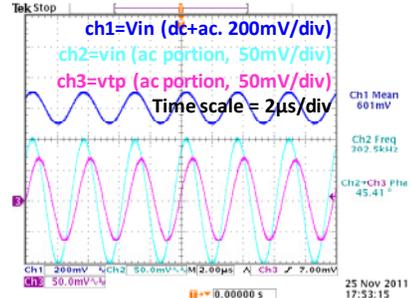
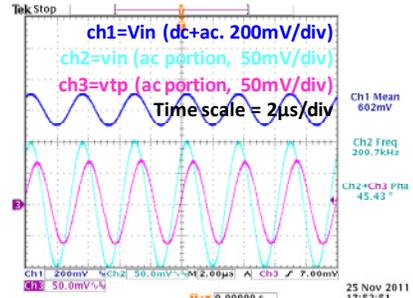
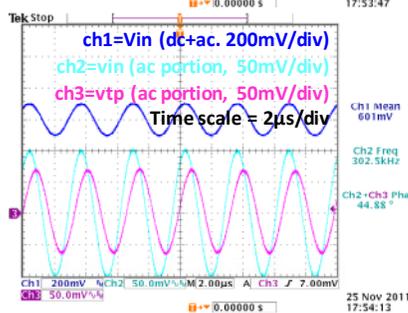
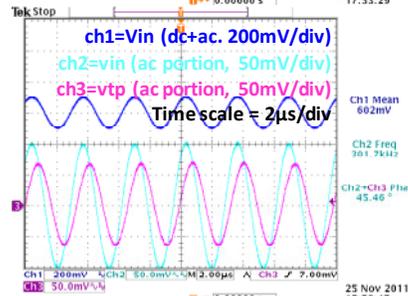
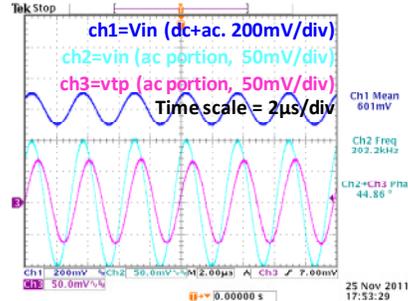


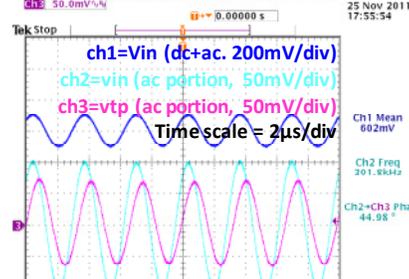
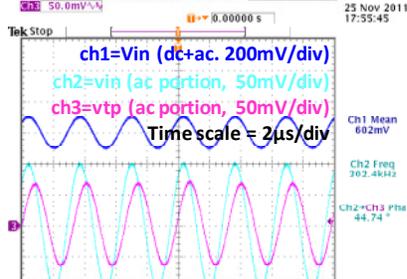
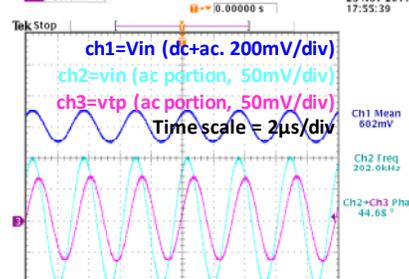
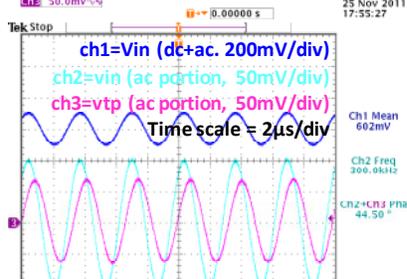
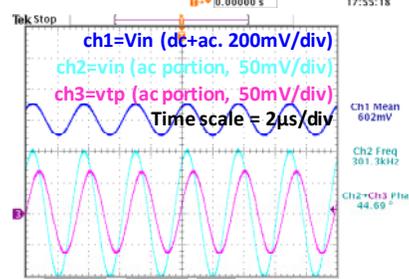
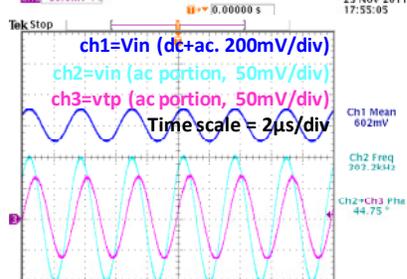
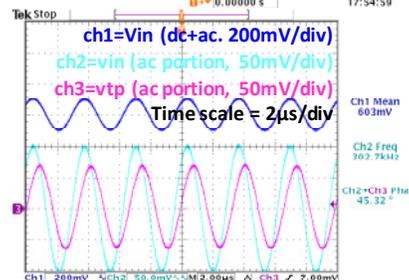
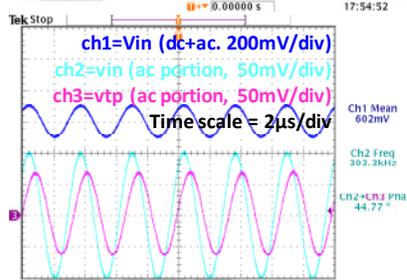
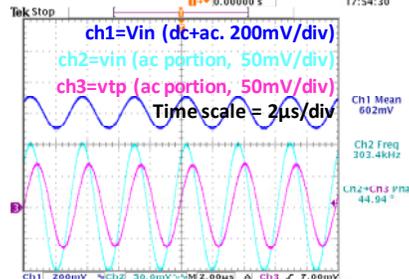
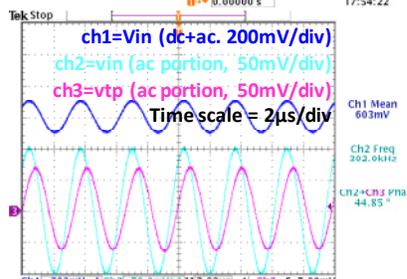
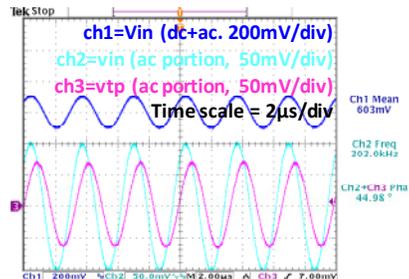
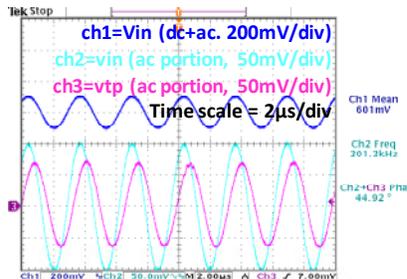
# Measurements at **PADONLY** point with **VBIAS=0.6V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.43 | 2.997E+05 | 1.15E-11 |
| 2          | 45.41 | 3.025E+05 | 1.14E-11 |
| 3          | 45.06 | 3.040E+05 | 1.12E-11 |
| 4          | 44.86 | 3.032E+05 | 1.11E-11 |
| 5          | 45.13 | 3.012E+05 | 1.13E-11 |
| 6          | 45.56 | 3.017E+05 | 1.15E-11 |
| 7          | 45.45 | 3.022E+05 | 1.14E-11 |
| 8          | 44.88 | 3.025E+05 | 1.12E-11 |
| 9          | 44.92 | 3.013E+05 | 1.12E-11 |
| 10         | 44.98 | 3.030E+05 | 1.12E-11 |
| 11         | 44.85 | 3.020E+05 | 1.12E-11 |
| 12         | 44.94 | 3.034E+05 | 1.11E-11 |
| 13         | 44.77 | 3.033E+05 | 1.11E-11 |
| 14         | 45.32 | 3.027E+05 | 1.13E-11 |
| 15         | 44.75 | 3.032E+05 | 1.11E-11 |
| 16         | 44.69 | 3.013E+05 | 1.11E-11 |
| 17         | 44.50 | 3.000E+05 | 1.11E-11 |
| 18         | 44.68 | 3.020E+05 | 1.11E-11 |
| 19         | 44.74 | 3.024E+05 | 1.11E-11 |
| 20         | 44.98 | 3.018E+05 | 1.12E-11 |

Average 45.00 3.022E+05 1.121E-11  
 STD 0.30 1.105E+03 1.265E-13



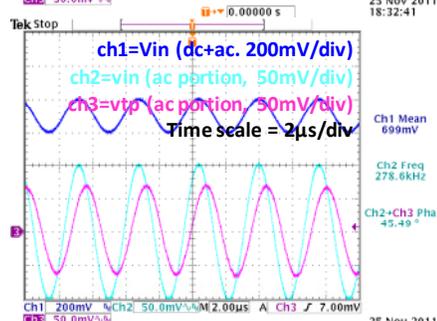
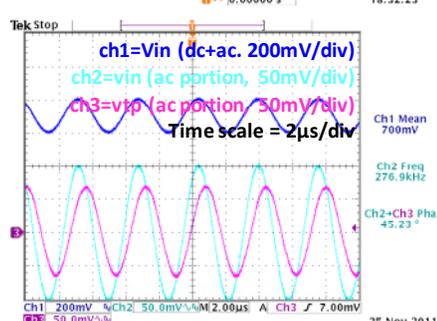
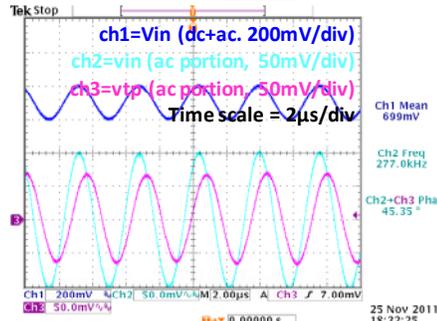
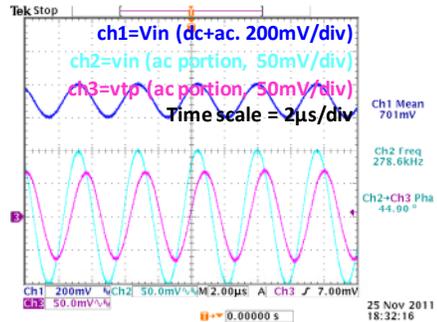
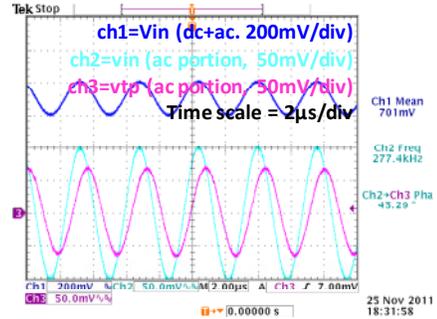
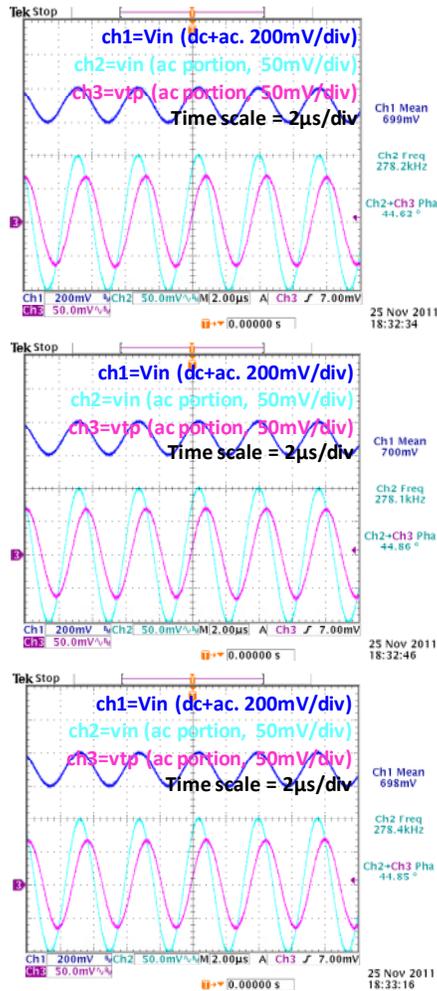


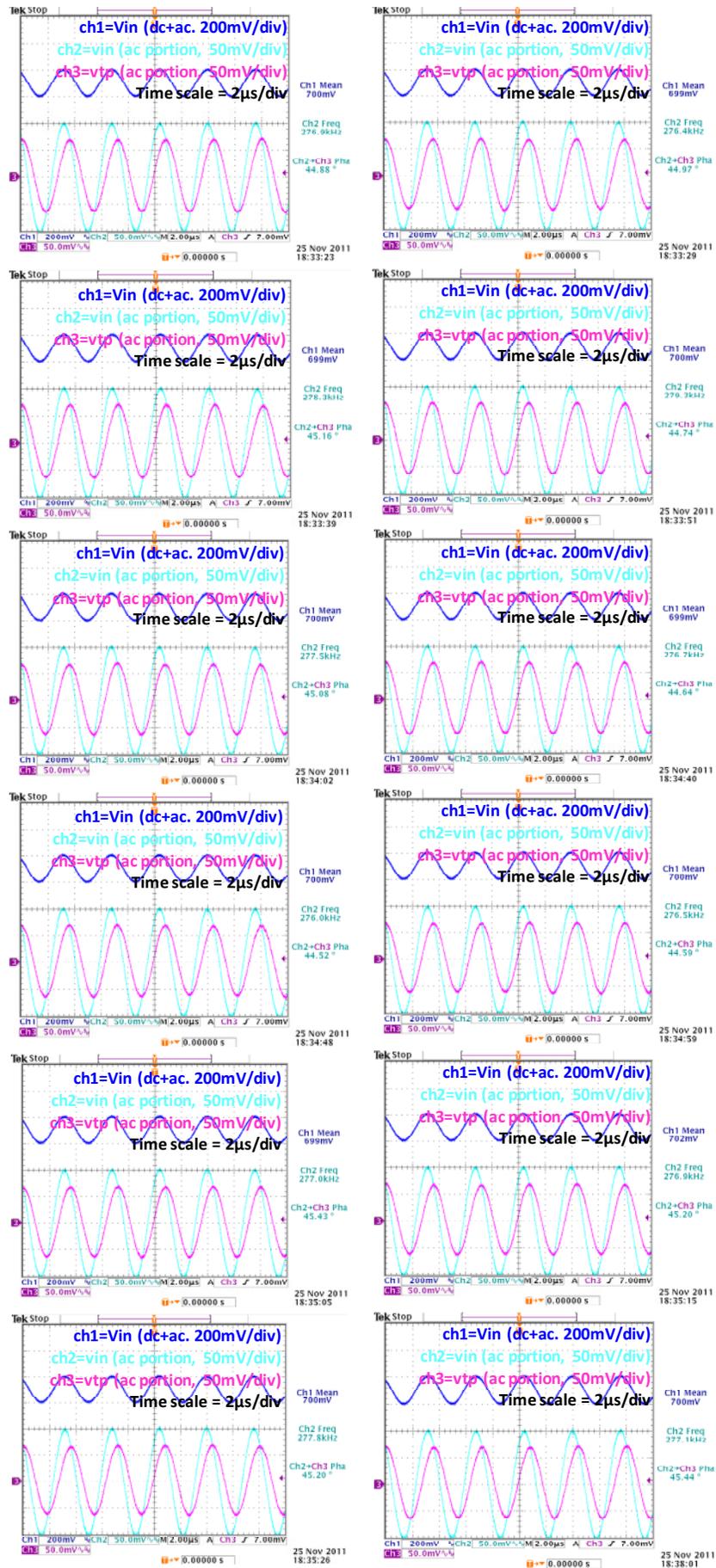
# Measurements at **NoQFG** point with **VBIAS=0.7V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.29 | 2.774E+05 | 1.23E-11 |
| 2          | 44.90 | 2.786E+05 | 1.21E-11 |
| 3          | 45.35 | 2.770E+05 | 1.24E-11 |
| 4          | 44.63 | 2.782E+05 | 1.20E-11 |
| 5          | 45.23 | 2.769E+05 | 1.23E-11 |
| 6          | 44.86 | 2.781E+05 | 1.21E-11 |
| 7          | 45.49 | 2.786E+05 | 1.24E-11 |
| 8          | 44.85 | 2.784E+05 | 1.21E-11 |
| 9          | 44.88 | 2.769E+05 | 1.22E-11 |
| 10         | 44.97 | 2.764E+05 | 1.22E-11 |
| 11         | 45.16 | 2.783E+05 | 1.22E-11 |
| 12         | 44.74 | 2.793E+05 | 1.20E-11 |
| 13         | 45.08 | 2.775E+05 | 1.22E-11 |
| 14         | 44.64 | 2.767E+05 | 1.21E-11 |
| 15         | 44.52 | 2.760E+05 | 1.21E-11 |
| 16         | 44.59 | 2.765E+05 | 1.21E-11 |
| 17         | 45.43 | 2.770E+05 | 1.24E-11 |
| 18         | 45.20 | 2.769E+05 | 1.23E-11 |
| 19         | 45.20 | 2.778E+05 | 1.23E-11 |
| 20         | 45.44 | 2.771E+05 | 1.24E-11 |

Average 45.02 2.775E+05 **1.222E-11**  
 STD 0.31 8.853E+02 **1.337E-13**



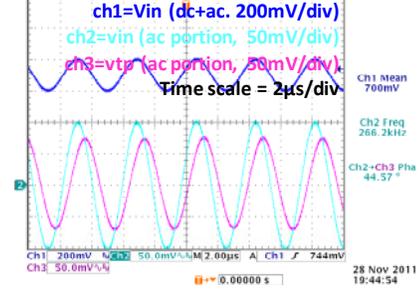
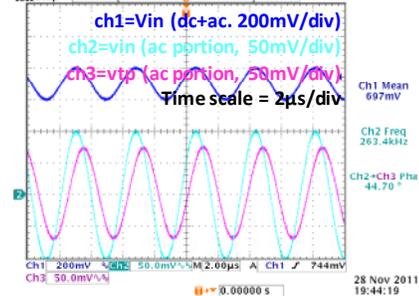
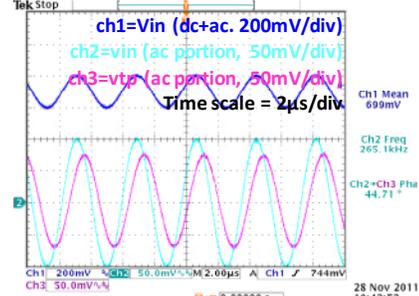
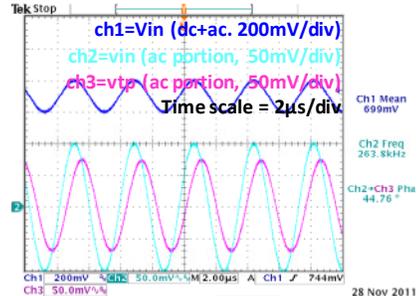
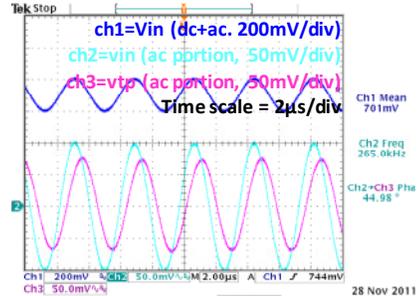
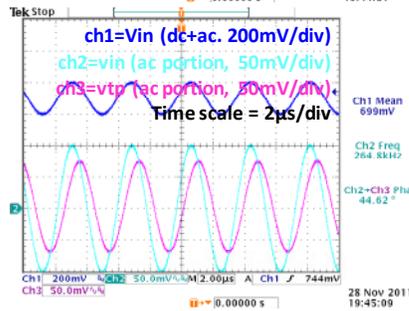
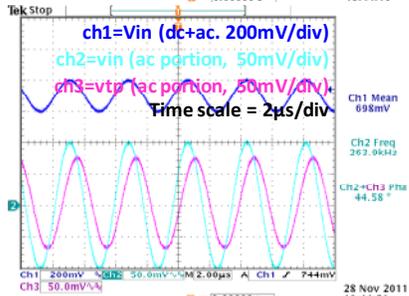
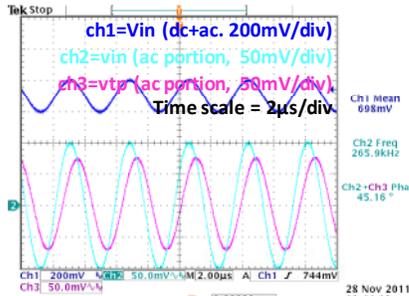


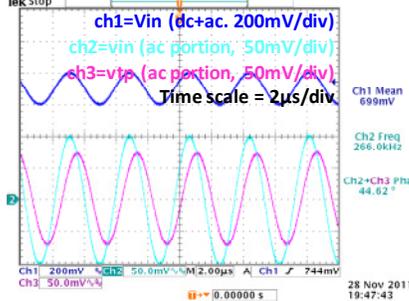
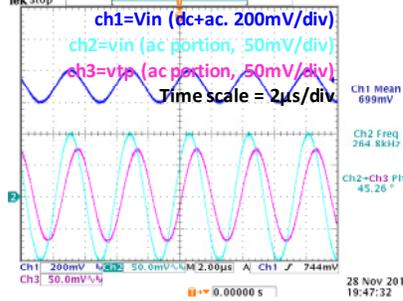
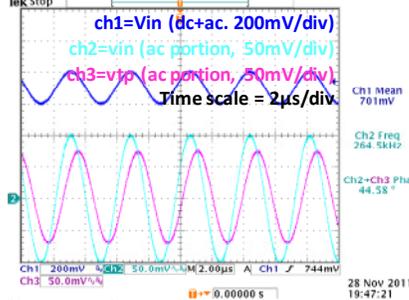
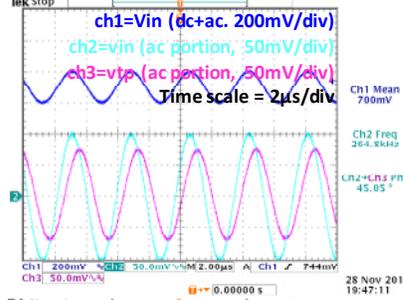
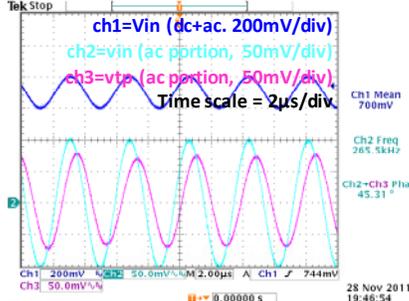
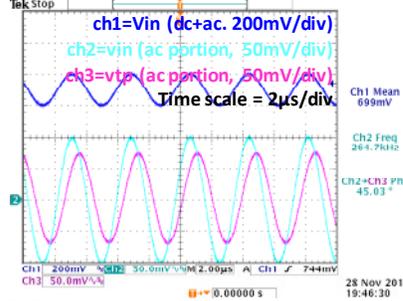
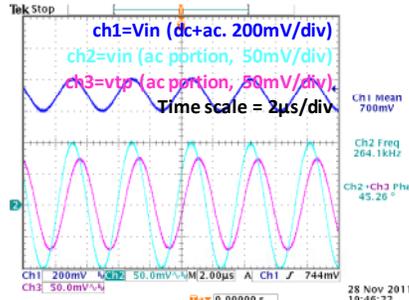
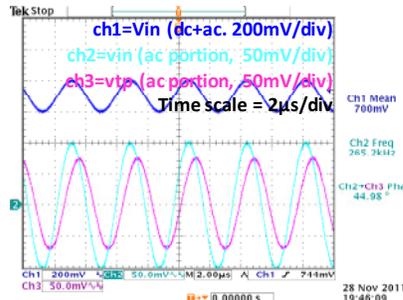
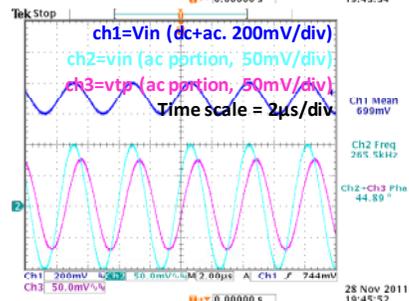
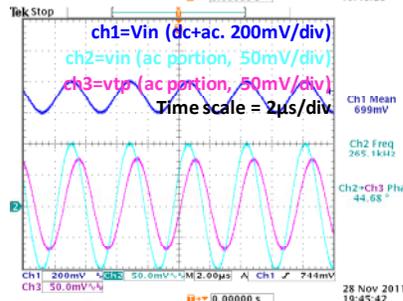
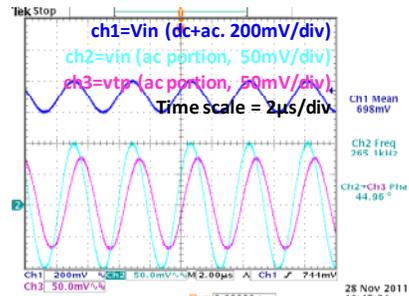
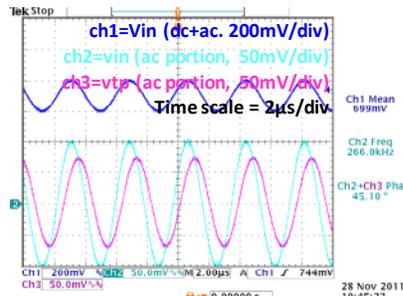
# Measurements at QFG point with VBIAS=0.7V

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.98 | 2.650E+05 | 1.28E-11 |
| 2          | 44.76 | 2.638E+05 | 1.27E-11 |
| 3          | 44.71 | 2.651E+05 | 1.27E-11 |
| 4          | 45.16 | 2.659E+05 | 1.28E-11 |
| 5          | 44.70 | 2.634E+05 | 1.27E-11 |
| 6          | 44.58 | 2.639E+05 | 1.27E-11 |
| 7          | 44.57 | 2.662E+05 | 1.25E-11 |
| 8          | 44.62 | 2.648E+05 | 1.26E-11 |
| 9          | 45.10 | 2.660E+05 | 1.28E-11 |
| 10         | 44.96 | 2.651E+05 | 1.28E-11 |
| 11         | 44.68 | 2.651E+05 | 1.26E-11 |
| 12         | 44.89 | 2.655E+05 | 1.27E-11 |
| 13         | 44.98 | 2.652E+05 | 1.28E-11 |
| 14         | 45.26 | 2.641E+05 | 1.29E-11 |
| 15         | 45.03 | 2.647E+05 | 1.28E-11 |
| 16         | 45.31 | 2.655E+05 | 1.29E-11 |
| 17         | 45.05 | 2.648E+05 | 1.28E-11 |
| 18         | 44.58 | 2.645E+05 | 1.26E-11 |
| 19         | 45.26 | 2.648E+05 | 1.29E-11 |
| 20         | 44.62 | 2.660E+05 | 1.26E-11 |

Average 44.89 2.650E+05 1.274E-11  
 STD 0.25 7.706E+02 1.128E-13



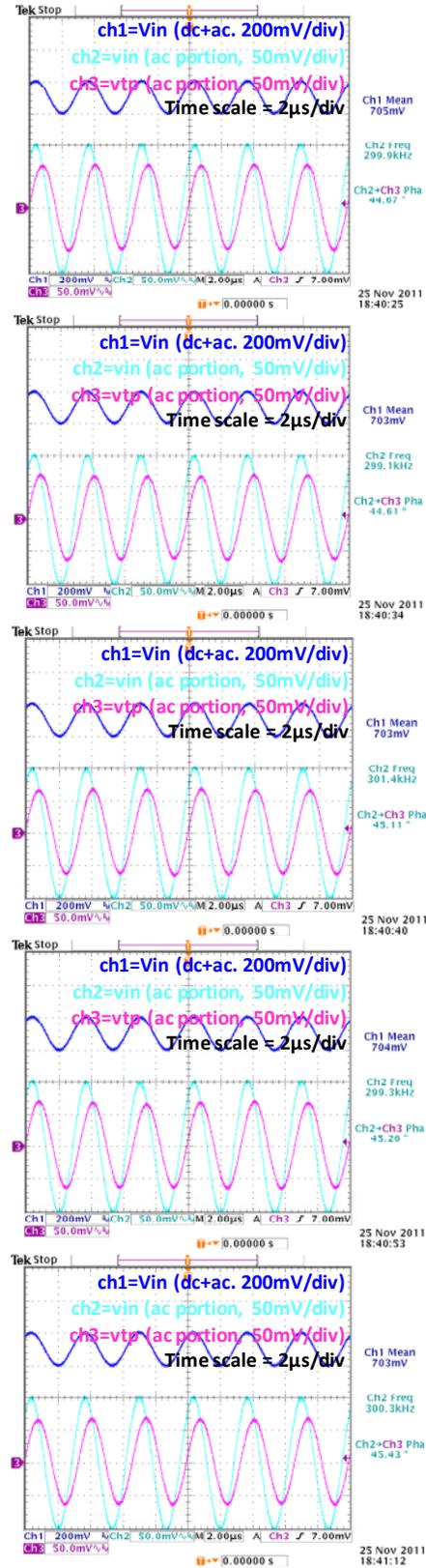
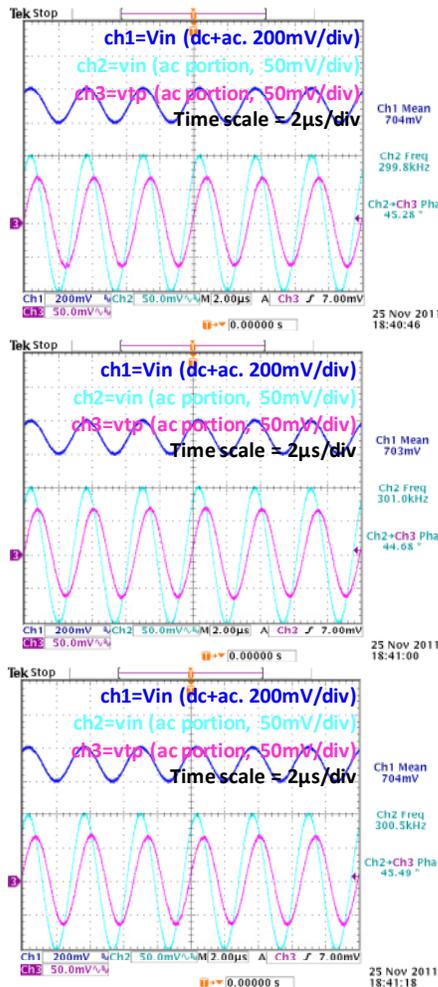


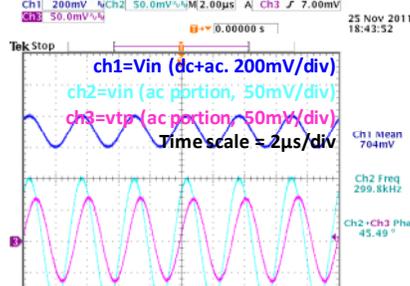
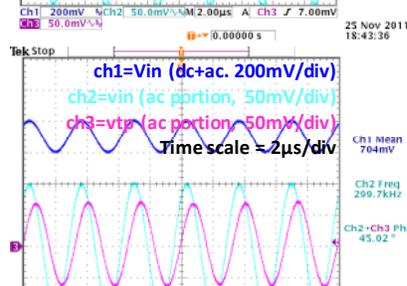
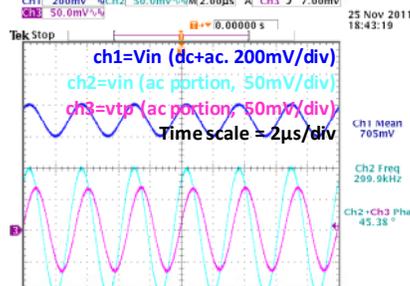
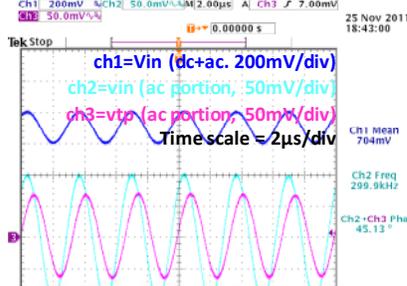
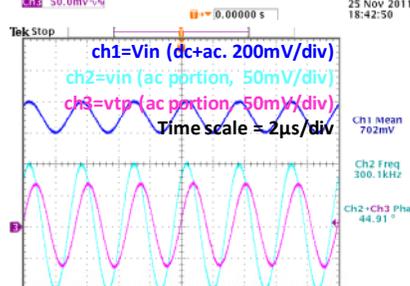
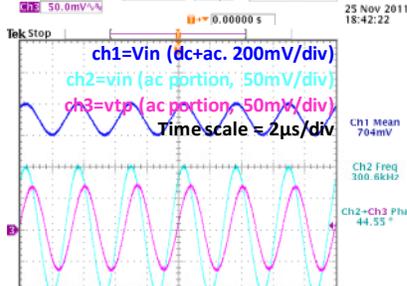
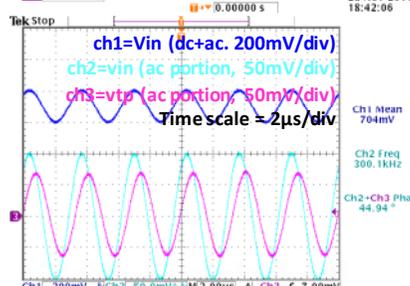
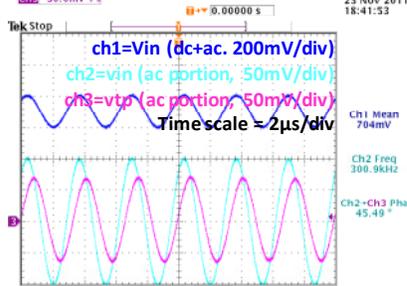
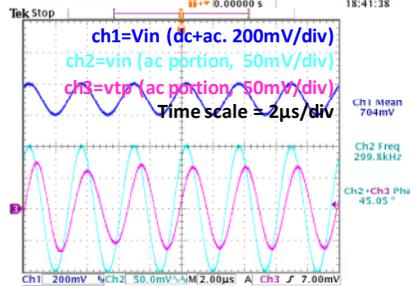
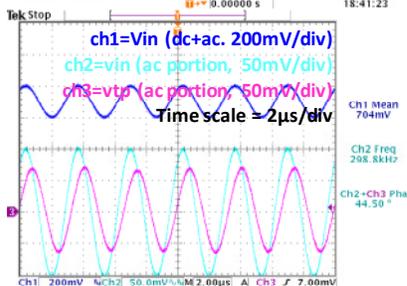
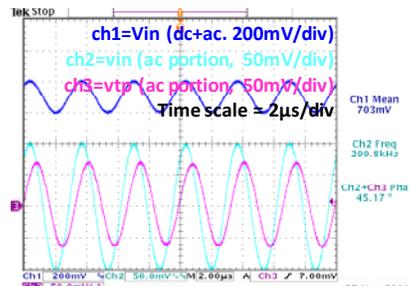
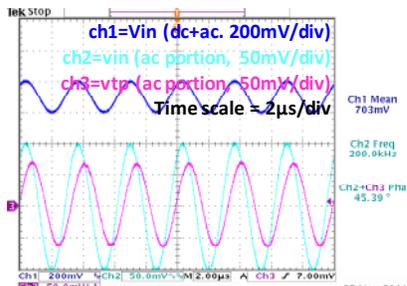
# Measurements at **PADONLY** point with **VBIAS=0.7V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.67 | 2.999E+05 | 1.12E-11 |
| 2          | 44.61 | 2.991E+05 | 1.12E-11 |
| 3          | 45.11 | 3.014E+05 | 1.13E-11 |
| 4          | 45.28 | 2.998E+05 | 1.14E-11 |
| 5          | 45.26 | 2.993E+05 | 1.14E-11 |
| 6          | 44.68 | 3.010E+05 | 1.11E-11 |
| 7          | 45.43 | 3.003E+05 | 1.15E-11 |
| 8          | 45.49 | 3.005E+05 | 1.15E-11 |
| 9          | 45.39 | 2.999E+05 | 1.15E-11 |
| 10         | 45.17 | 2.998E+05 | 1.14E-11 |
| 11         | 44.50 | 2.988E+05 | 1.11E-11 |
| 12         | 45.05 | 2.998E+05 | 1.13E-11 |
| 13         | 45.49 | 3.009E+05 | 1.15E-11 |
| 14         | 44.94 | 3.001E+05 | 1.13E-11 |
| 15         | 44.55 | 3.006E+05 | 1.11E-11 |
| 16         | 44.91 | 3.001E+05 | 1.13E-11 |
| 17         | 45.13 | 2.999E+05 | 1.13E-11 |
| 18         | 45.38 | 2.999E+05 | 1.14E-11 |
| 19         | 45.02 | 2.997E+05 | 1.13E-11 |
| 20         | 45.49 | 2.998E+05 | 1.15E-11 |

Average 45.08 3.000E+05 1.132E-11  
 STD 0.33 6.284E+02 1.288E-13



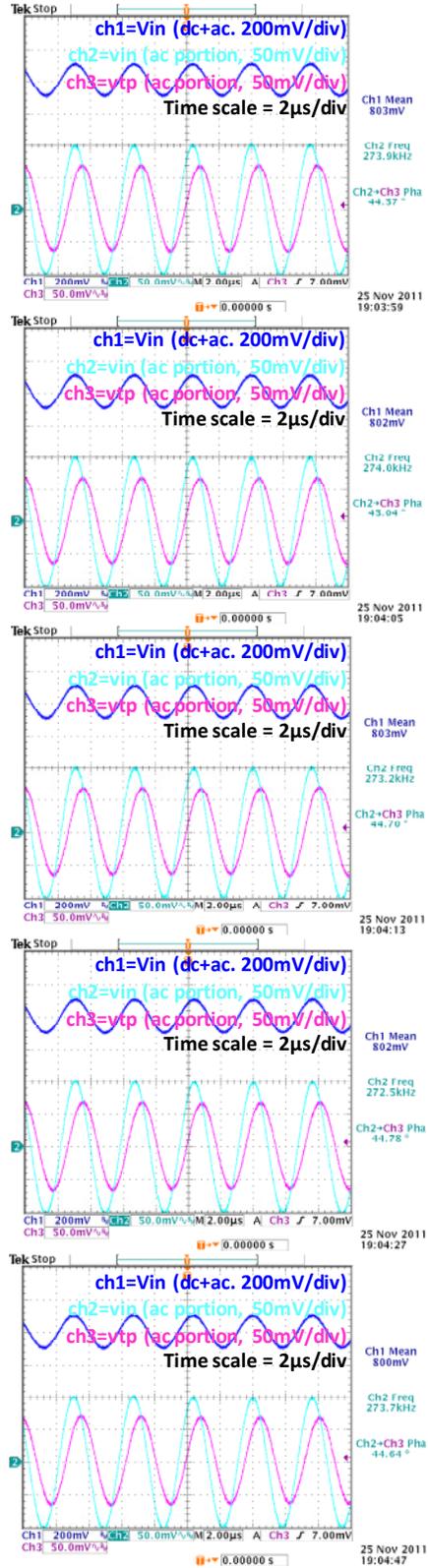
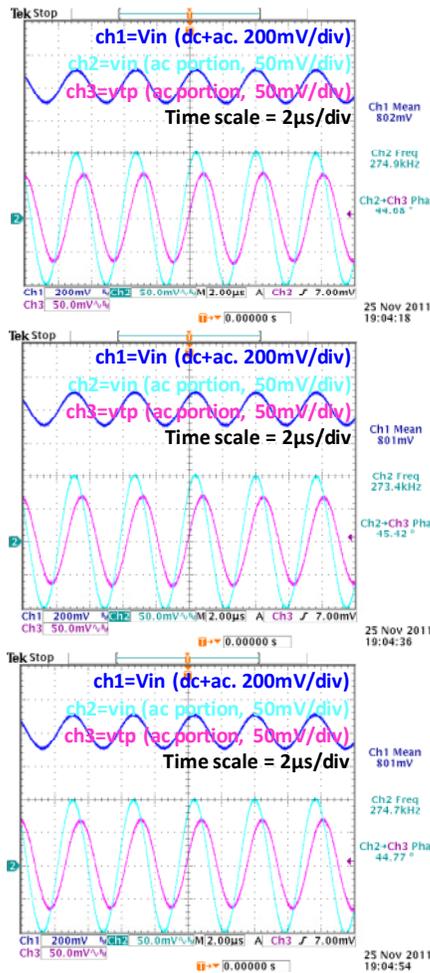


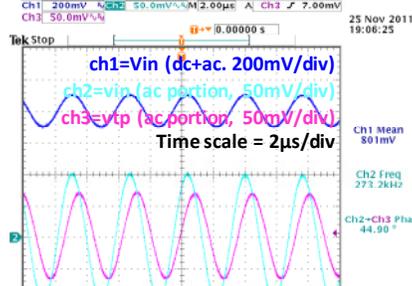
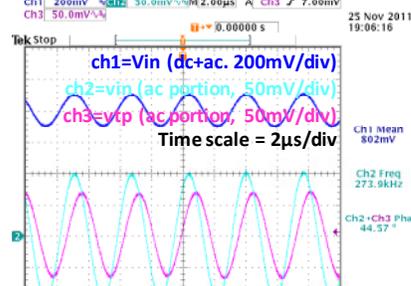
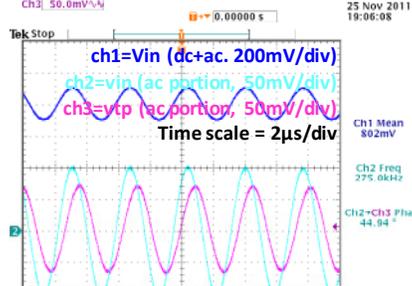
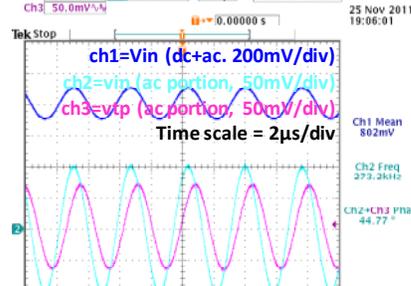
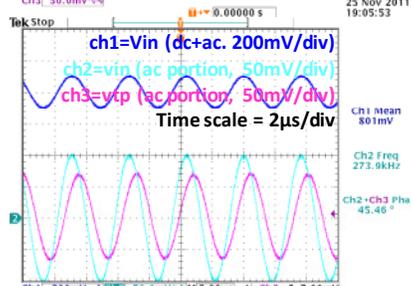
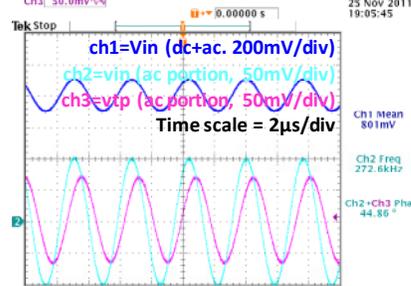
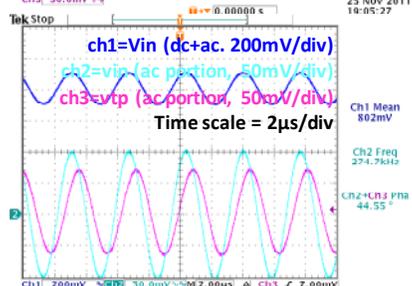
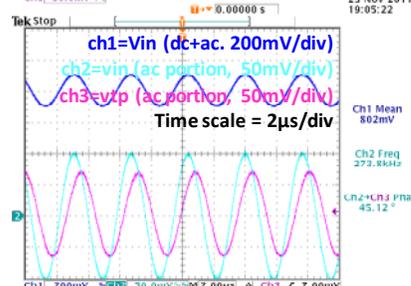
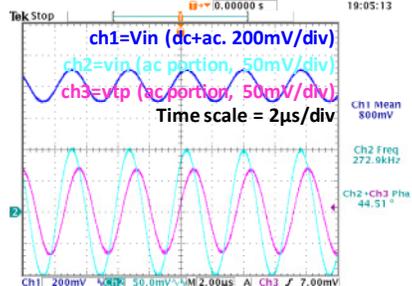
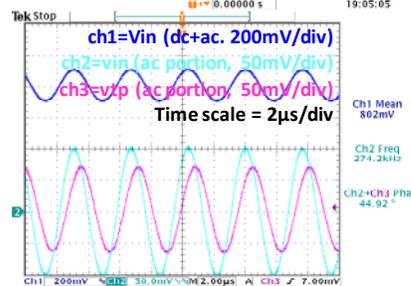
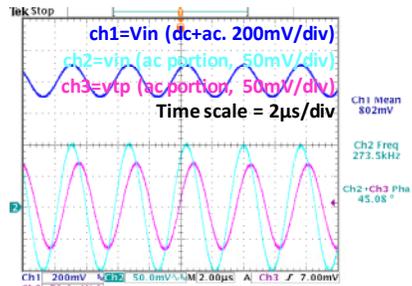
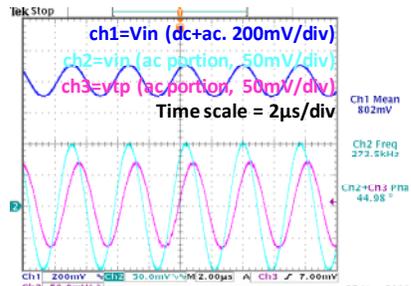
# Measurements at **NoQFG** point with **VBIAS=0.8V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.57 | 2.739E+05 | 1.22E-11 |
| 2          | 45.04 | 2.740E+05 | 1.24E-11 |
| 3          | 44.70 | 2.732E+05 | 1.23E-11 |
| 4          | 44.68 | 2.749E+05 | 1.22E-11 |
| 5          | 44.78 | 2.725E+05 | 1.23E-11 |
| 6          | 45.42 | 2.734E+05 | 1.26E-11 |
| 7          | 44.64 | 2.737E+05 | 1.22E-11 |
| 8          | 44.77 | 2.747E+05 | 1.22E-11 |
| 9          | 44.98 | 2.735E+05 | 1.24E-11 |
| 10         | 45.08 | 2.735E+05 | 1.24E-11 |
| 11         | 44.92 | 2.742E+05 | 1.23E-11 |
| 12         | 44.51 | 2.729E+05 | 1.22E-11 |
| 13         | 45.12 | 2.738E+05 | 1.24E-11 |
| 14         | 44.55 | 2.747E+05 | 1.21E-11 |
| 15         | 44.86 | 2.726E+05 | 1.24E-11 |
| 16         | 45.46 | 2.739E+05 | 1.26E-11 |
| 17         | 44.77 | 2.732E+05 | 1.23E-11 |
| 18         | 44.94 | 2.750E+05 | 1.23E-11 |
| 19         | 44.57 | 2.739E+05 | 1.22E-11 |
| 20         | 44.90 | 2.732E+05 | 1.24E-11 |

Average 44.86 2.737E+05 **1.232E-11**  
 STD 0.27 7.177E+02 **1.213E-13**



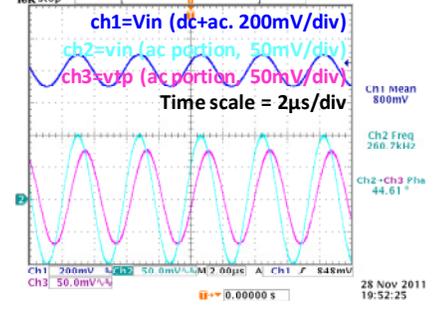
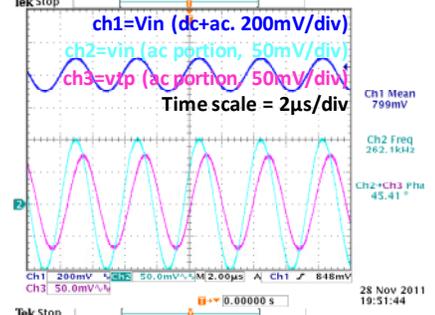
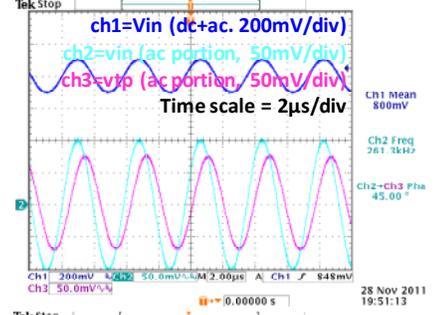
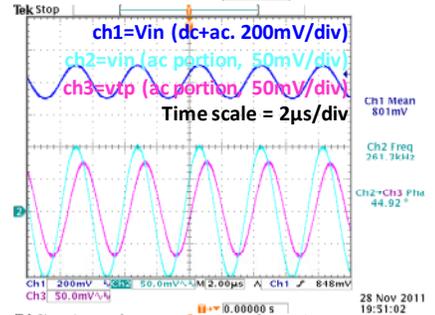
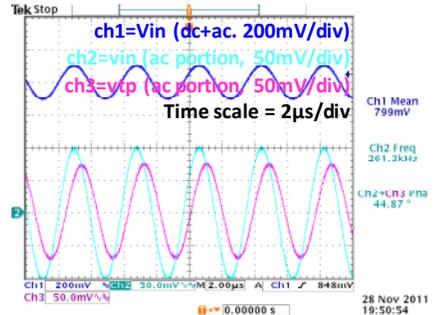
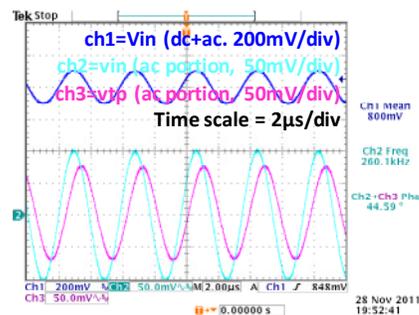
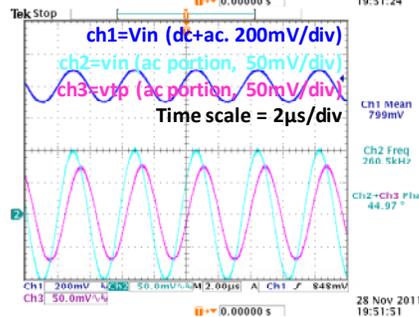
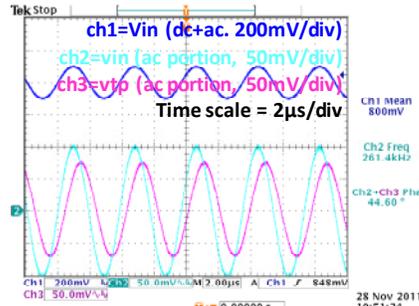


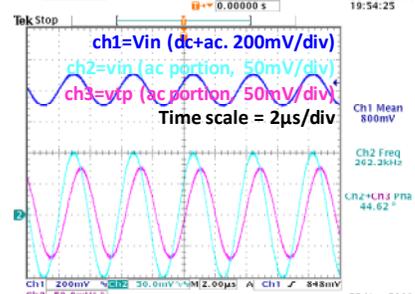
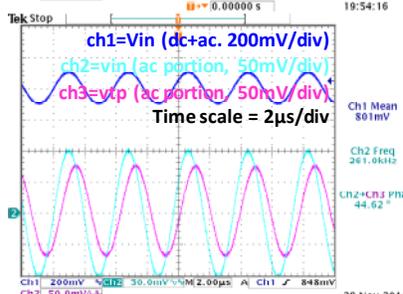
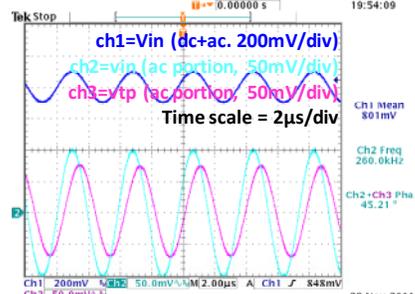
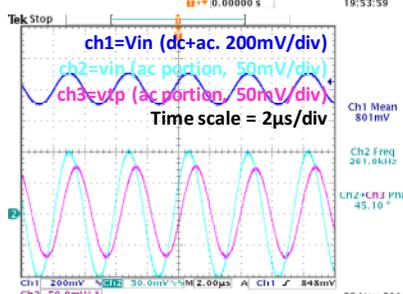
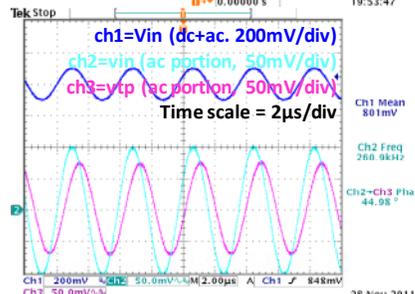
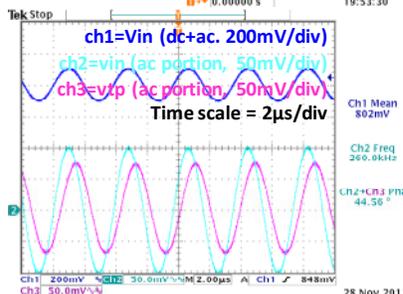
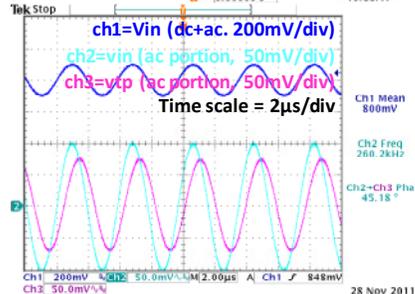
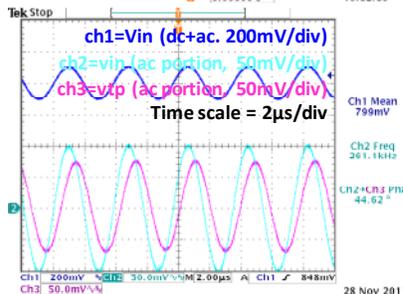
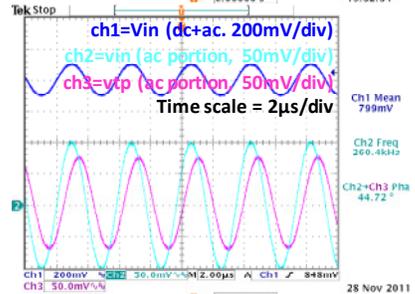
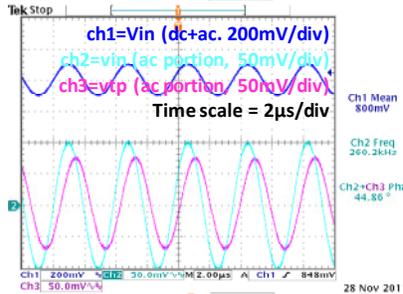
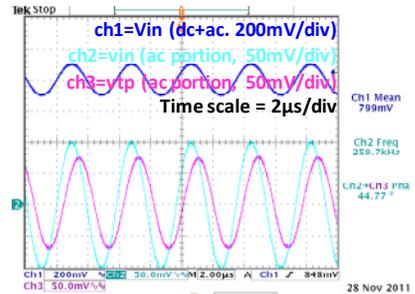
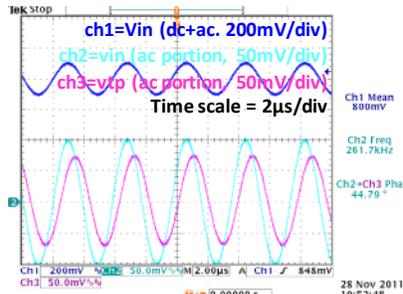
# Measurements at QFG point with VBIAS=0.8V

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.87 | 2.613E+05 | 1.29E-11 |
| 2          | 44.92 | 2.613E+05 | 1.29E-11 |
| 3          | 45.00 | 2.613E+05 | 1.30E-11 |
| 4          | 44.60 | 2.614E+05 | 1.28E-11 |
| 5          | 45.41 | 2.621E+05 | 1.31E-11 |
| 6          | 44.97 | 2.605E+05 | 1.30E-11 |
| 7          | 44.61 | 2.607E+05 | 1.28E-11 |
| 8          | 44.59 | 2.601E+05 | 1.28E-11 |
| 9          | 44.79 | 2.617E+05 | 1.29E-11 |
| 10         | 44.77 | 2.597E+05 | 1.29E-11 |
| 11         | 44.86 | 2.602E+05 | 1.30E-11 |
| 12         | 44.72 | 2.604E+05 | 1.29E-11 |
| 13         | 44.62 | 2.611E+05 | 1.28E-11 |
| 14         | 45.18 | 2.602E+05 | 1.31E-11 |
| 15         | 44.56 | 2.609E+05 | 1.28E-11 |
| 16         | 44.98 | 2.609E+05 | 1.30E-11 |
| 17         | 45.10 | 2.610E+05 | 1.30E-11 |
| 18         | 45.21 | 2.600E+05 | 1.31E-11 |
| 19         | 44.62 | 2.610E+05 | 1.28E-11 |
| 20         | 44.62 | 2.622E+05 | 1.28E-11 |

Average 44.85 2.609E+05 1.292E-11  
 STD 0.24 6.836E+02 1.147E-13



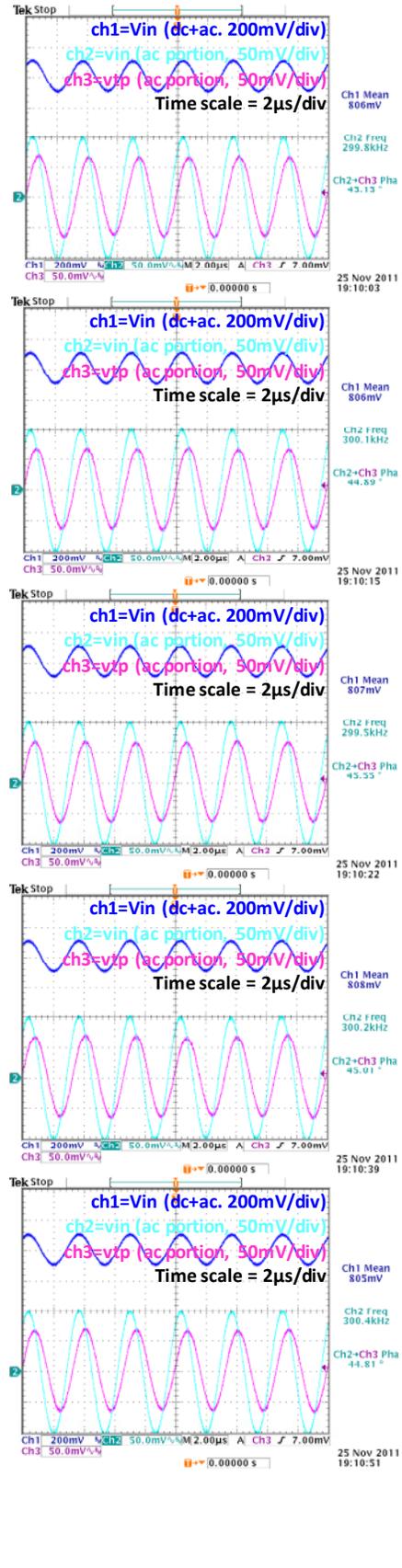
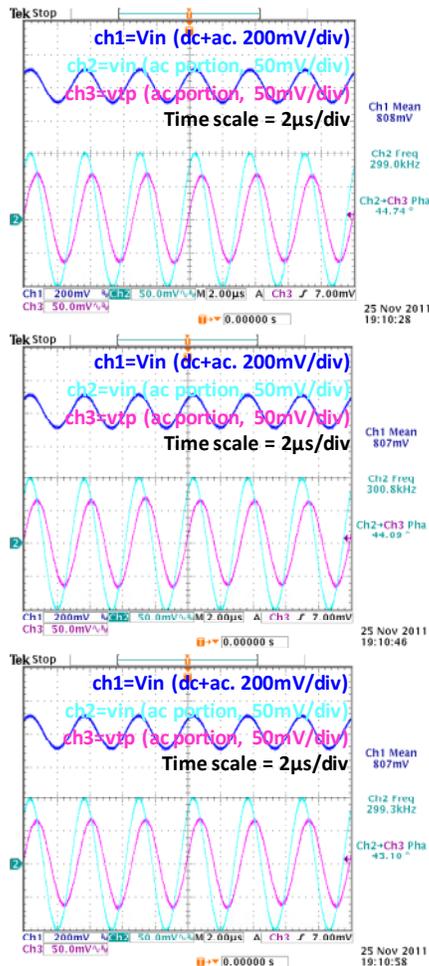


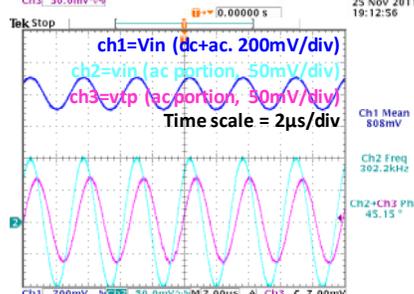
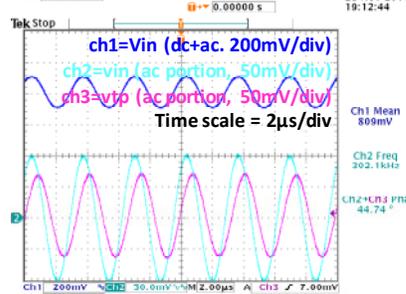
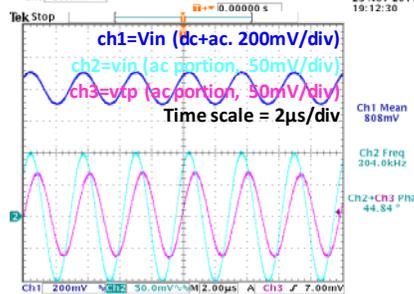
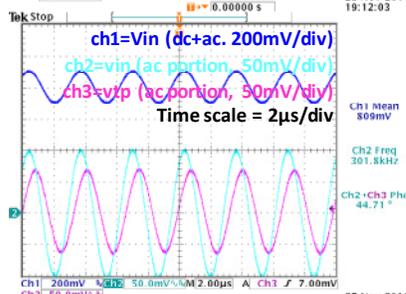
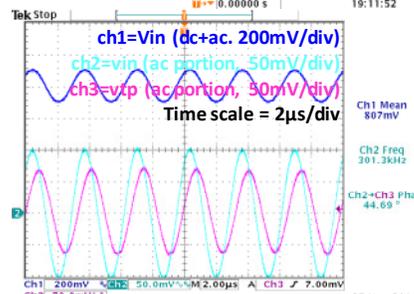
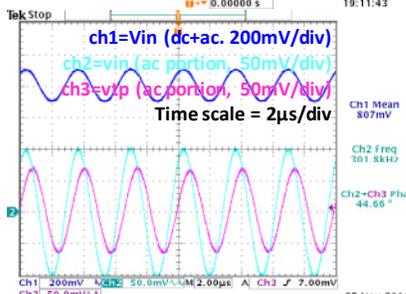
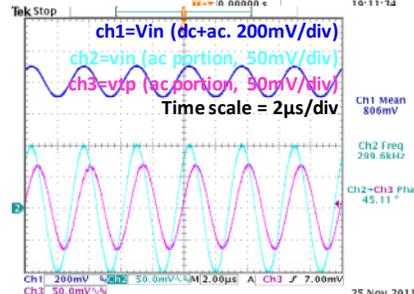
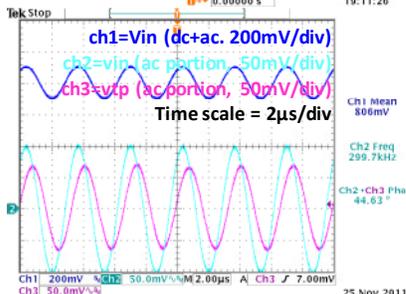
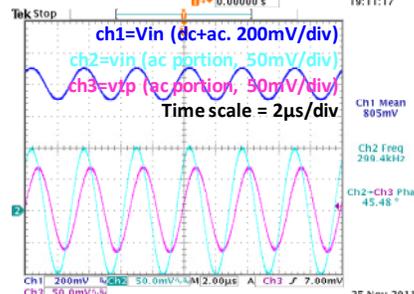
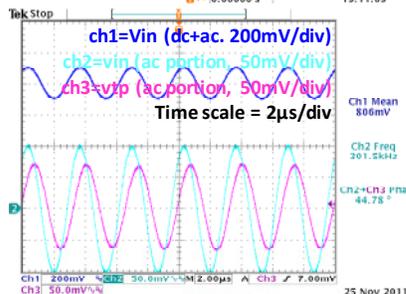
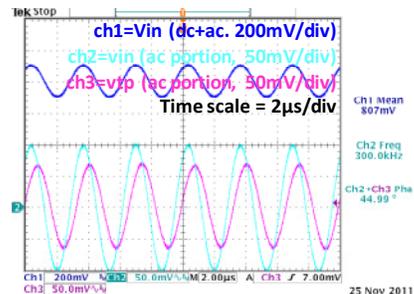
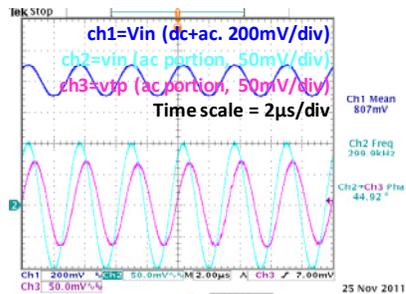
# Measurements at **PADONLY** point with **VBIAS=0.8V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.15 | 2.998E+05 | 1.14E-11 |
| 2          | 44.89 | 3.001E+05 | 1.12E-11 |
| 3          | 45.55 | 2.995E+05 | 1.15E-11 |
| 4          | 44.74 | 2.990E+05 | 1.12E-11 |
| 5          | 45.01 | 3.002E+05 | 1.13E-11 |
| 6          | 44.69 | 3.008E+05 | 1.11E-11 |
| 7          | 44.81 | 3.004E+05 | 1.12E-11 |
| 8          | 45.10 | 2.993E+05 | 1.14E-11 |
| 9          | 44.92 | 2.999E+05 | 1.13E-11 |
| 10         | 44.99 | 3.000E+05 | 1.13E-11 |
| 11         | 44.78 | 3.015E+05 | 1.12E-11 |
| 12         | 45.48 | 2.994E+05 | 1.15E-11 |
| 13         | 44.63 | 2.997E+05 | 1.12E-11 |
| 14         | 45.11 | 2.996E+05 | 1.14E-11 |
| 15         | 44.66 | 3.018E+05 | 1.11E-11 |
| 16         | 44.69 | 3.013E+05 | 1.11E-11 |
| 17         | 44.71 | 3.018E+05 | 1.11E-11 |
| 18         | 44.84 | 3.040E+05 | 1.11E-11 |
| 19         | 44.74 | 3.021E+05 | 1.11E-11 |
| 20         | 45.15 | 3.022E+05 | 1.13E-11 |

Average 44.93 3.006E+05 **1.125E-11**  
 STD 0.26 1.282E+03 **1.300E-13**



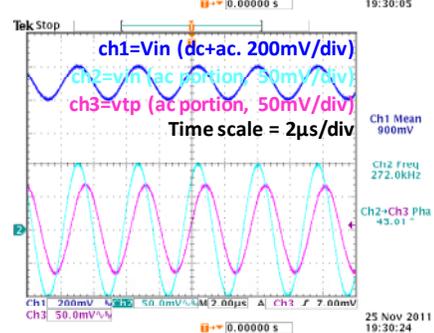
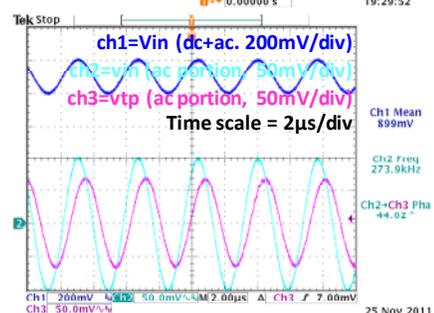
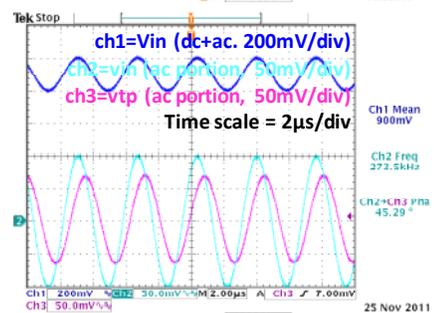
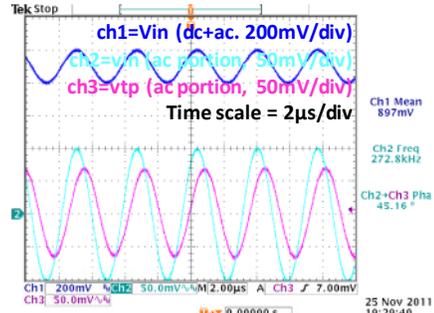
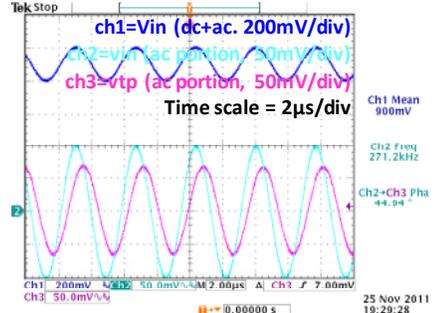
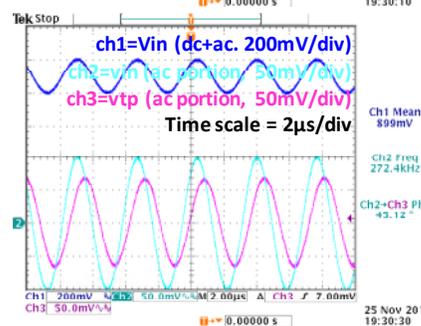
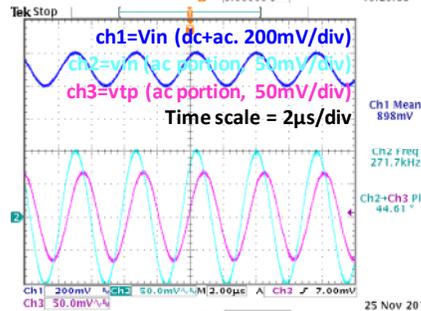
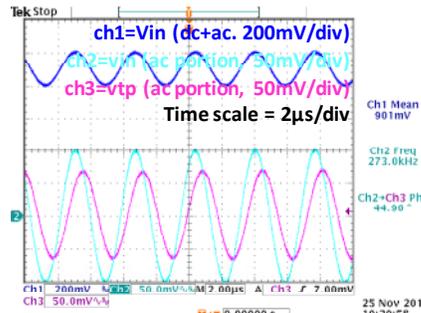


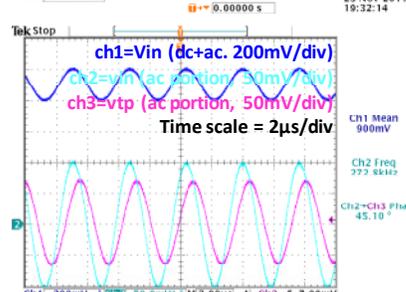
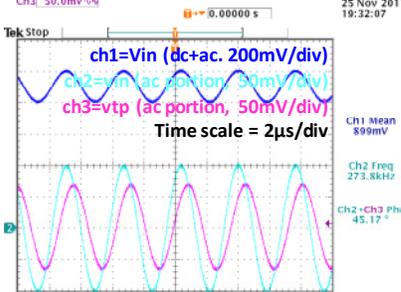
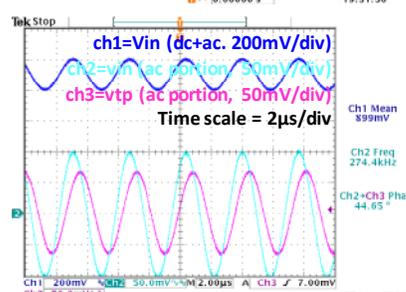
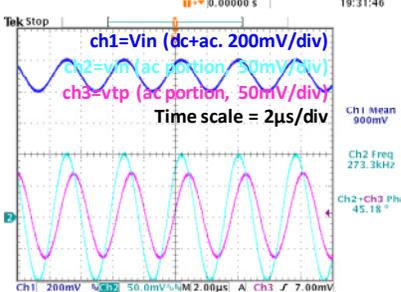
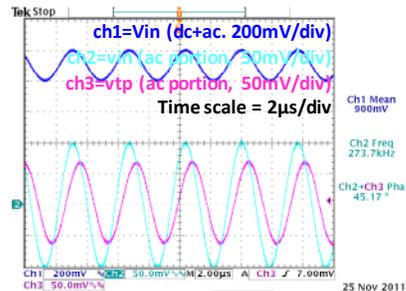
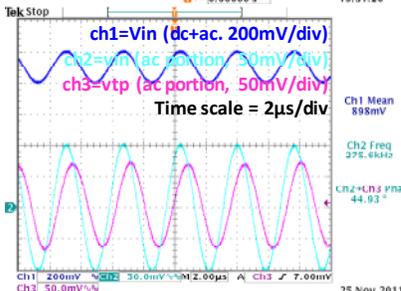
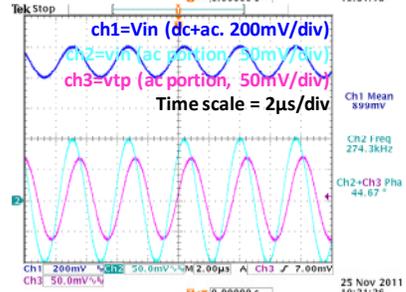
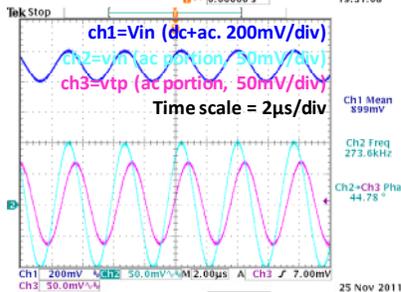
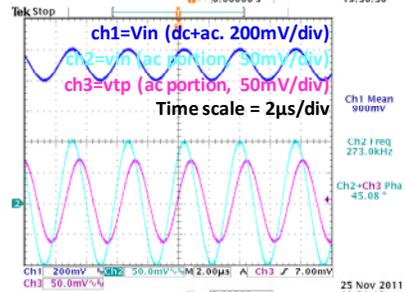
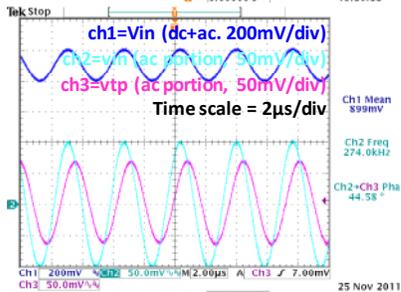
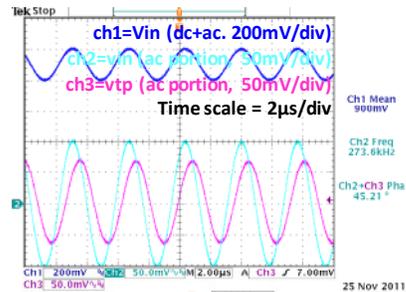
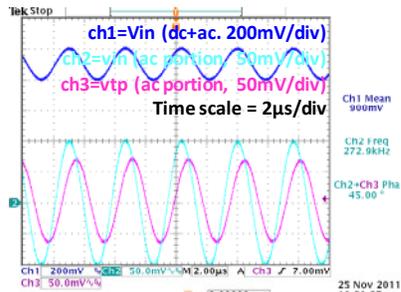
# Measurements at **NoQFG** point with **VBIAS=0.9V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.94 | 2.712E+05 | 1.25E-11 |
| 2          | 45.16 | 2.728E+05 | 1.25E-11 |
| 3          | 45.29 | 2.735E+05 | 1.25E-11 |
| 4          | 44.96 | 2.730E+05 | 1.24E-11 |
| 5          | 44.62 | 2.739E+05 | 1.22E-11 |
| 6          | 44.61 | 2.717E+05 | 1.23E-11 |
| 7          | 45.01 | 2.720E+05 | 1.25E-11 |
| 8          | 45.12 | 2.724E+05 | 1.25E-11 |
| 9          | 45.00 | 2.729E+05 | 1.24E-11 |
| 10         | 45.21 | 2.736E+05 | 1.25E-11 |
| 11         | 44.58 | 2.740E+05 | 1.22E-11 |
| 12         | 45.08 | 2.730E+05 | 1.24E-11 |
| 13         | 44.78 | 2.736E+05 | 1.23E-11 |
| 14         | 44.67 | 2.743E+05 | 1.22E-11 |
| 15         | 44.93 | 2.756E+05 | 1.23E-11 |
| 16         | 45.17 | 2.737E+05 | 1.25E-11 |
| 17         | 45.18 | 2.733E+05 | 1.25E-11 |
| 18         | 44.65 | 2.744E+05 | 1.22E-11 |
| 19         | 45.17 | 2.738E+05 | 1.24E-11 |
| 20         | 45.10 | 2.728E+05 | 1.25E-11 |

Average 44.96 2.733E+05 **1.238E-11**  
 STD 0.23 1.007E+03 **1.158E-13**



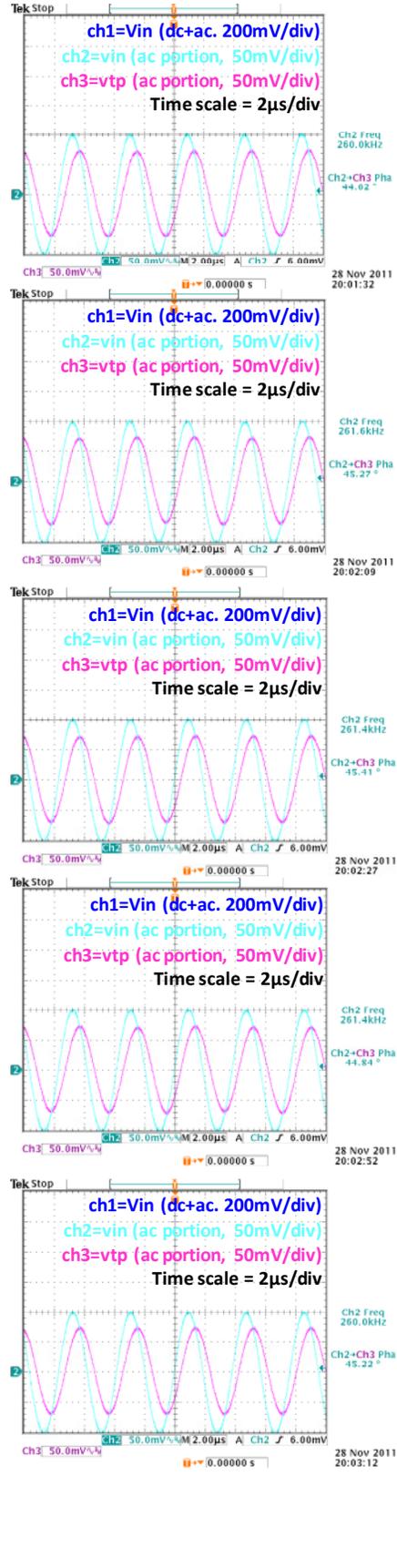
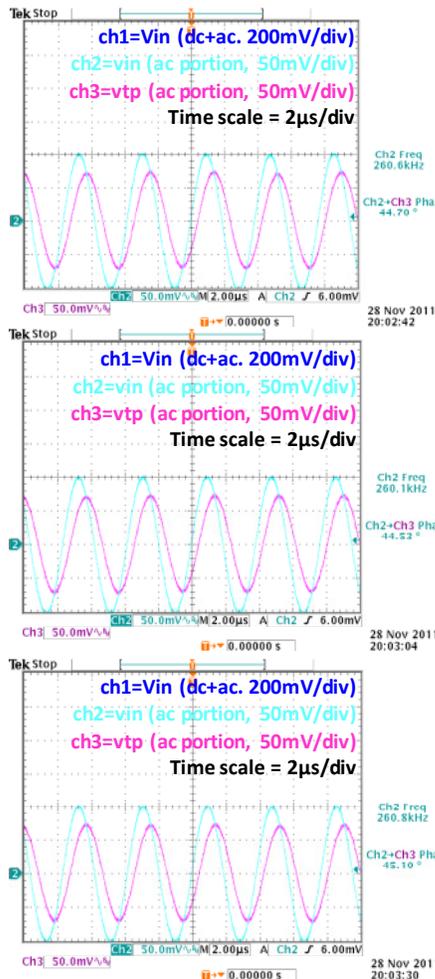


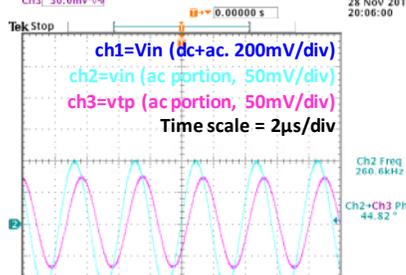
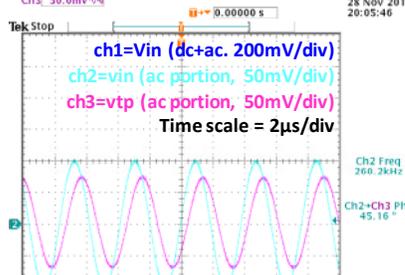
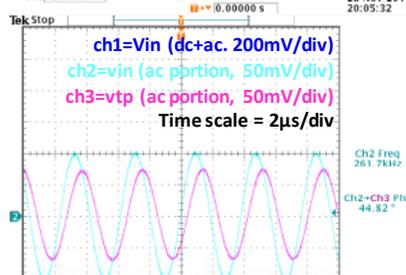
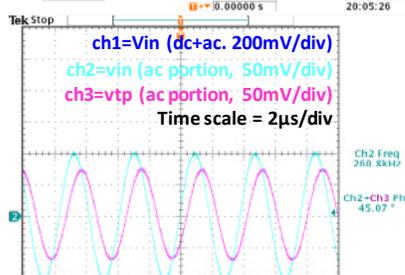
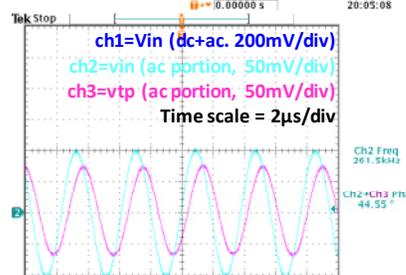
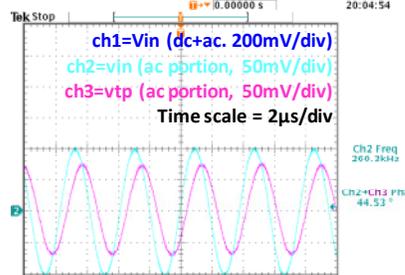
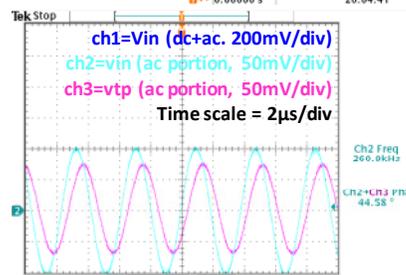
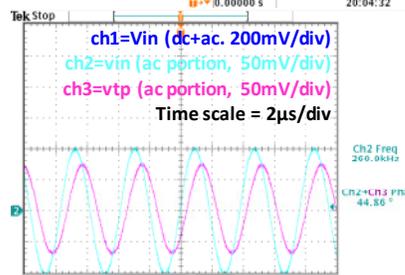
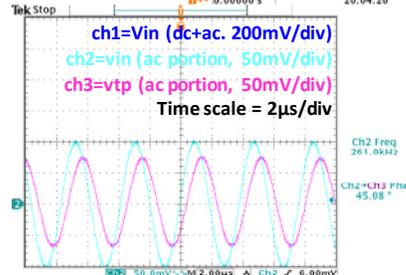
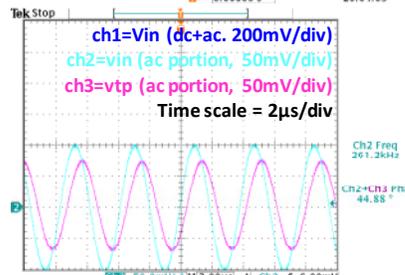
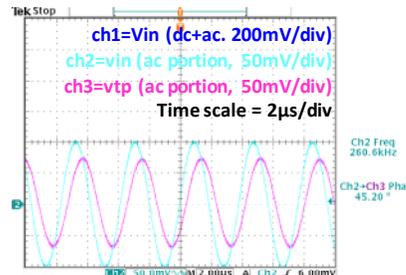
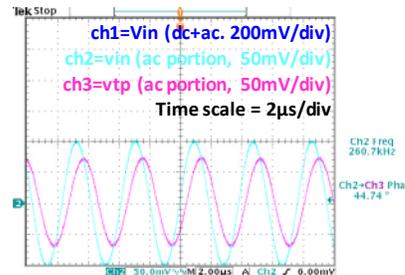
# Measurements at QFG point with **VBIAS=0.9V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.62 | 2.600E+05 | 1.29E-11 |
| 2          | 45.27 | 2.616E+05 | 1.31E-11 |
| 3          | 45.41 | 2.614E+05 | 1.31E-11 |
| 4          | 44.70 | 2.606E+05 | 1.29E-11 |
| 5          | 44.84 | 2.614E+05 | 1.29E-11 |
| 6          | 44.53 | 2.601E+05 | 1.28E-11 |
| 7          | 45.22 | 2.600E+05 | 1.31E-11 |
| 8          | 45.10 | 2.608E+05 | 1.30E-11 |
| 9          | 44.74 | 2.607E+05 | 1.29E-11 |
| 10         | 45.20 | 2.606E+05 | 1.31E-11 |
| 11         | 44.88 | 2.612E+05 | 1.29E-11 |
| 12         | 45.08 | 2.610E+05 | 1.30E-11 |
| 13         | 44.86 | 2.609E+05 | 1.29E-11 |
| 14         | 44.58 | 2.609E+05 | 1.28E-11 |
| 15         | 44.53 | 2.603E+05 | 1.28E-11 |
| 16         | 44.55 | 2.615E+05 | 1.28E-11 |
| 17         | 45.07 | 2.608E+05 | 1.30E-11 |
| 18         | 44.82 | 2.617E+05 | 1.29E-11 |
| 19         | 45.16 | 2.602E+05 | 1.31E-11 |
| 20         | 44.82 | 2.606E+05 | 1.29E-11 |

Average 44.90 2.608E+05 1.295E-11  
 STD 0.27 5.324E+02 1.216E-13



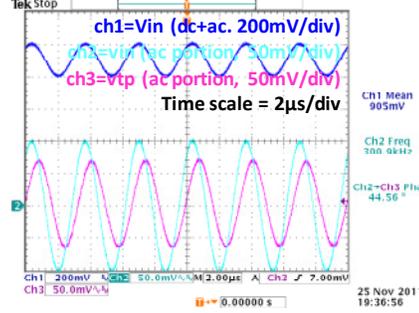
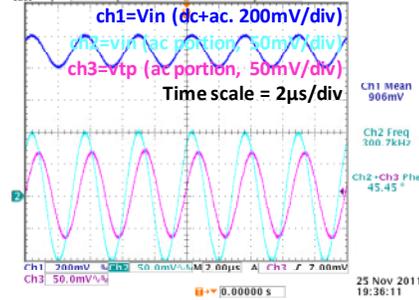
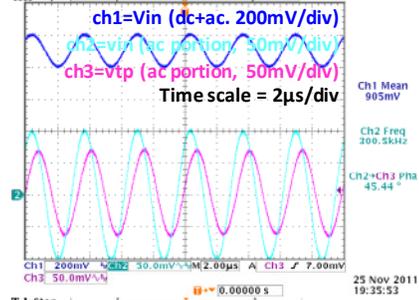
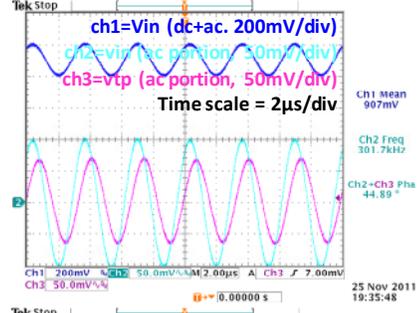
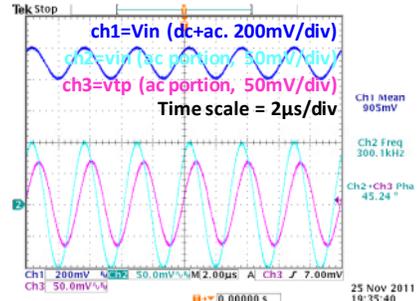
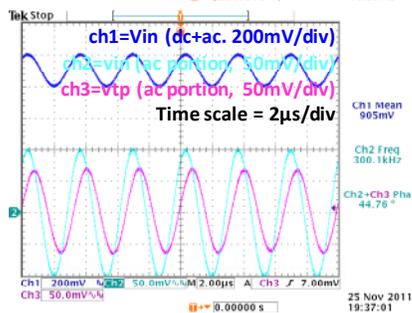
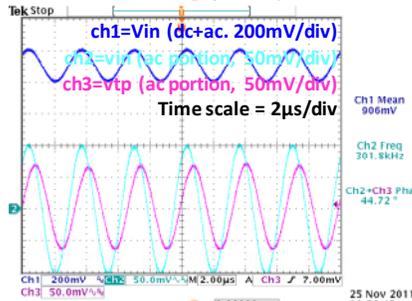
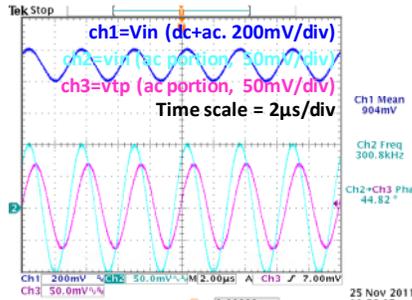


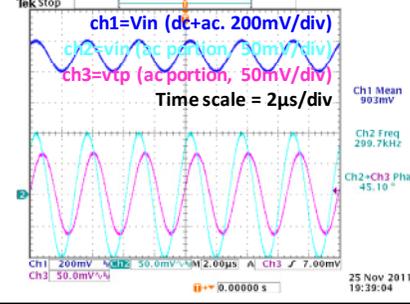
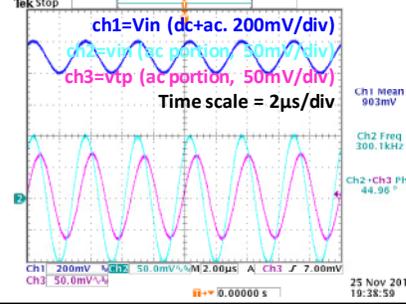
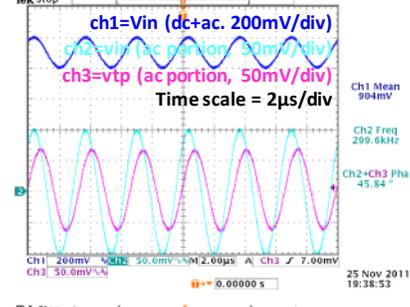
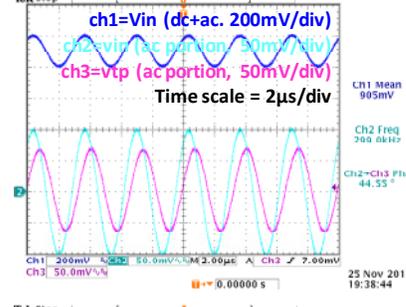
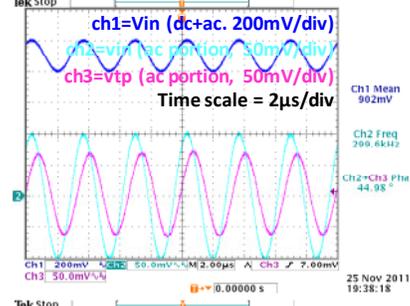
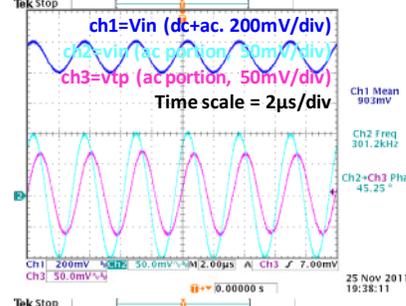
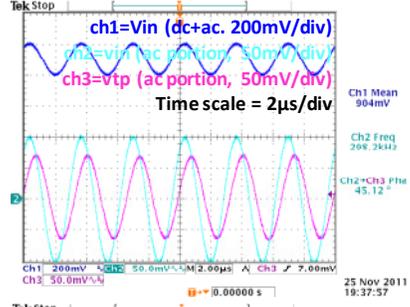
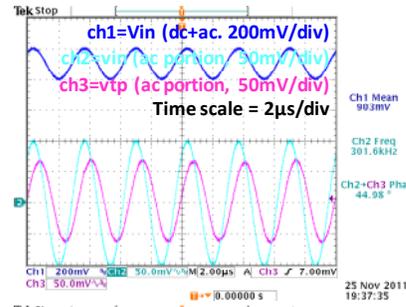
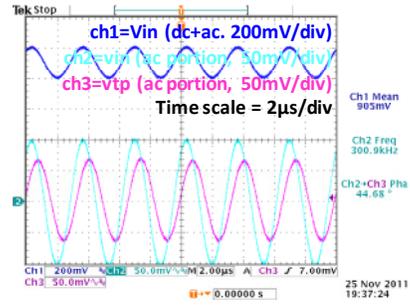
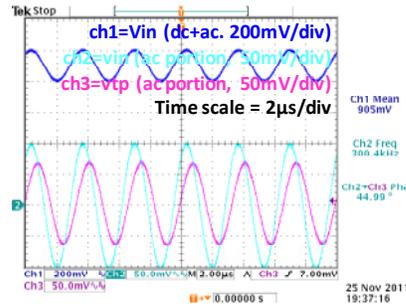
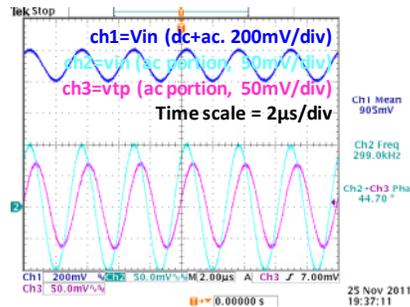
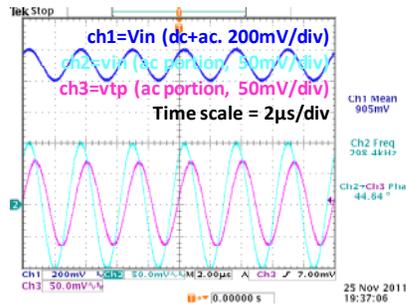
# Measurements at **PADONLY** point with **VBIAS=0.9V**

RIN= 4.697E+04

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.24 | 3.001E+05 | 1.14E-11 |
| 2          | 44.89 | 3.017E+05 | 1.12E-11 |
| 3          | 45.44 | 3.005E+05 | 1.15E-11 |
| 4          | 44.82 | 3.008E+05 | 1.12E-11 |
| 5          | 45.45 | 3.007E+05 | 1.14E-11 |
| 6          | 44.72 | 3.018E+05 | 1.11E-11 |
| 7          | 44.56 | 3.009E+05 | 1.11E-11 |
| 8          | 44.76 | 3.001E+05 | 1.12E-11 |
| 9          | 44.64 | 2.984E+05 | 1.12E-11 |
| 10         | 44.70 | 2.990E+05 | 1.12E-11 |
| 11         | 44.99 | 3.004E+05 | 1.13E-11 |
| 12         | 44.68 | 3.009E+05 | 1.11E-11 |
| 13         | 44.98 | 3.016E+05 | 1.12E-11 |
| 14         | 45.12 | 2.982E+05 | 1.14E-11 |
| 15         | 45.25 | 3.012E+05 | 1.13E-11 |
| 16         | 44.98 | 2.996E+05 | 1.13E-11 |
| 17         | 44.55 | 2.990E+05 | 1.12E-11 |
| 18         | 45.84 | 2.996E+05 | 1.16E-11 |
| 19         | 44.96 | 3.001E+05 | 1.13E-11 |
| 20         | 45.10 | 2.997E+05 | 1.13E-11 |

Average 44.98 3.002E+05 1.128E-11  
 STD 0.34 1.041E+03 1.380E-13



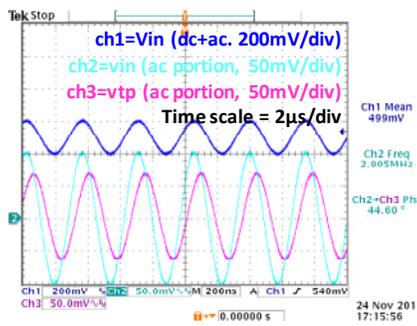
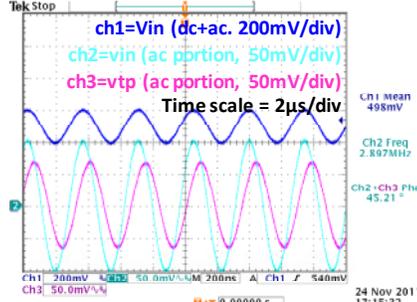
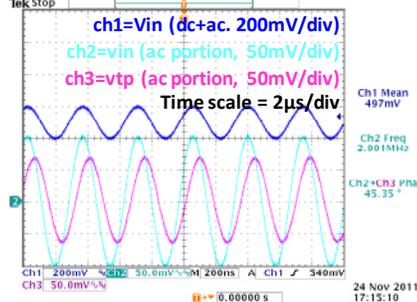
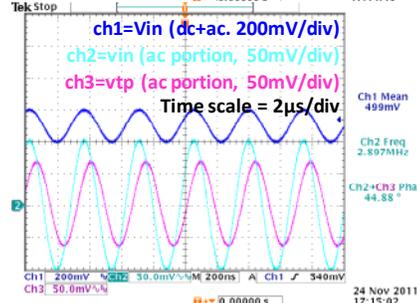
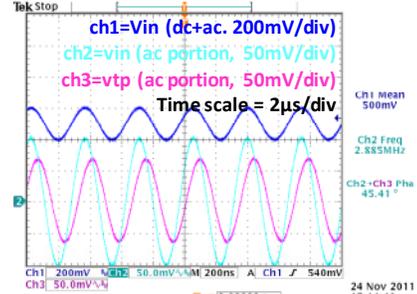
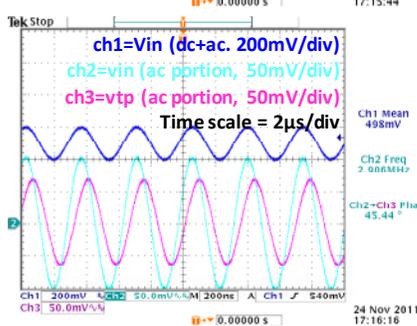
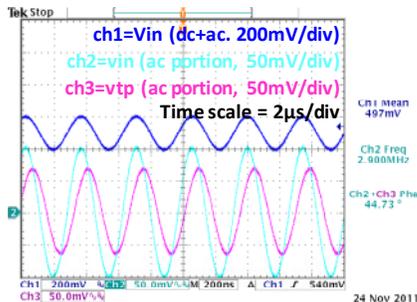
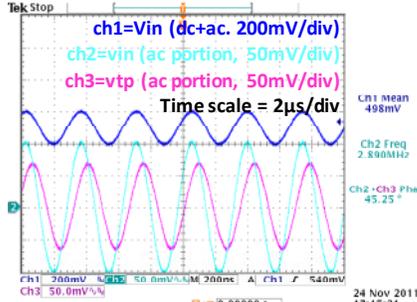


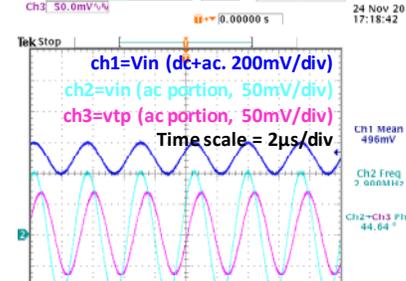
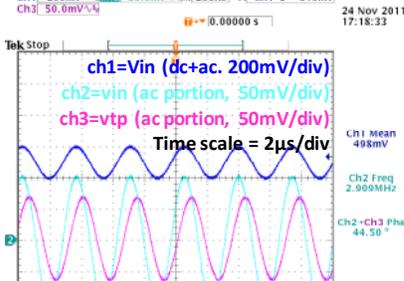
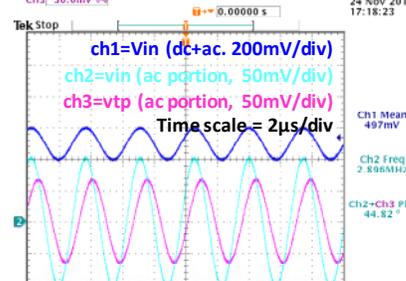
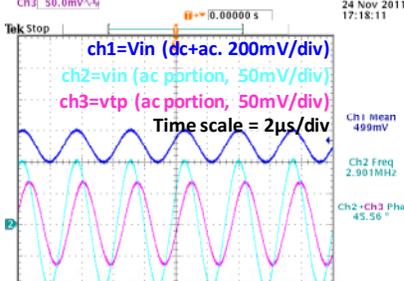
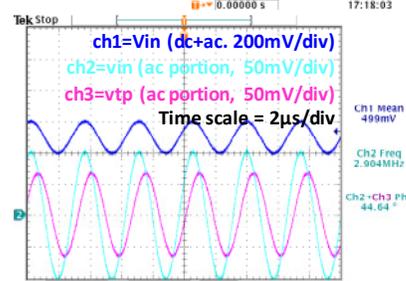
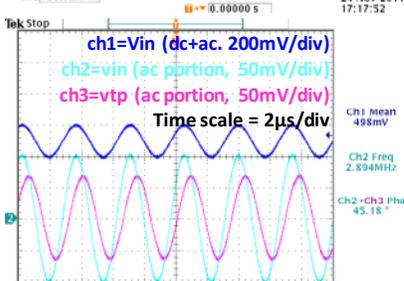
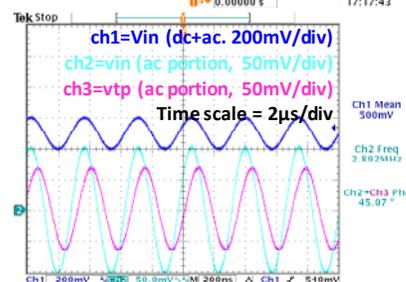
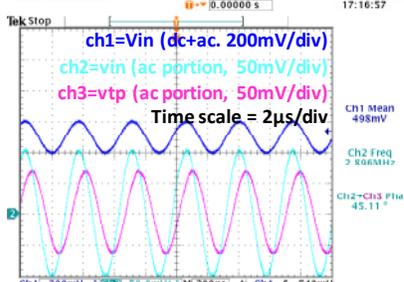
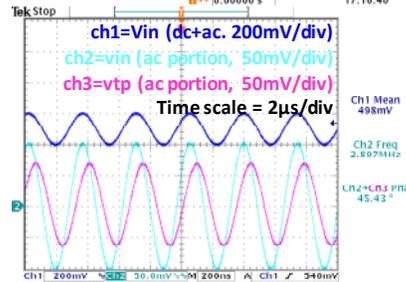
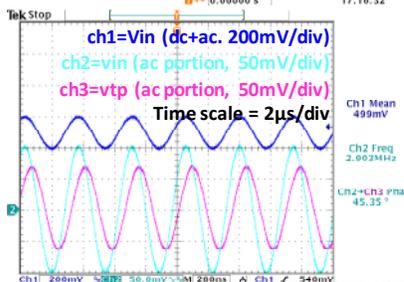
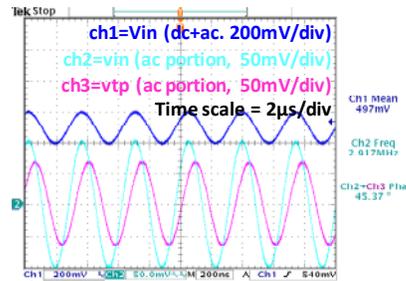
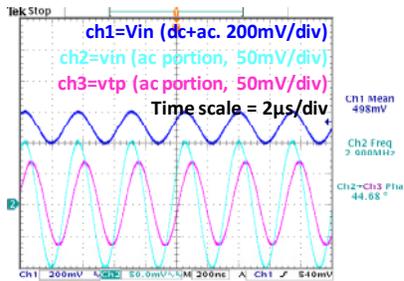
# testsignal noQFG with 200mV 4k7 @0.5V

RIN= 4.692E+03

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.41 | 2.885E+06 | 1.19E-11 |
| 2          | 44.88 | 2.897E+06 | 1.17E-11 |
| 3          | 45.35 | 2.901E+06 | 1.18E-11 |
| 4          | 45.25 | 2.890E+06 | 1.18E-11 |
| 5          | 45.21 | 2.897E+06 | 1.18E-11 |
| 6          | 44.73 | 2.900E+06 | 1.16E-11 |
| 7          | 44.60 | 2.905E+06 | 1.15E-11 |
| 8          | 45.44 | 2.906E+06 | 1.19E-11 |
| 9          | 44.68 | 2.900E+06 | 1.16E-11 |
| 10         | 45.37 | 2.971E+06 | 1.16E-11 |
| 11         | 45.35 | 2.903E+06 | 1.18E-11 |
| 12         | 45.43 | 2.897E+06 | 1.19E-11 |
| 13         | 45.11 | 2.896E+06 | 1.18E-11 |
| 14         | 45.07 | 2.892E+06 | 1.18E-11 |
| 15         | 45.18 | 2.894E+06 | 1.18E-11 |
| 16         | 44.64 | 2.904E+06 | 1.15E-11 |
| 17         | 45.56 | 2.901E+06 | 1.19E-11 |
| 18         | 44.82 | 2.896E+06 | 1.16E-11 |
| 19         | 44.50 | 2.909E+06 | 1.15E-11 |
| 20         | 44.64 | 2.900E+06 | 1.16E-11 |

Average 45.06 2.902E+06 1.171E-11  
 STD 0.34 1.716E+04 1.506E-13



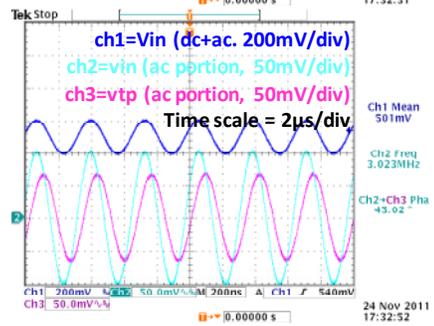
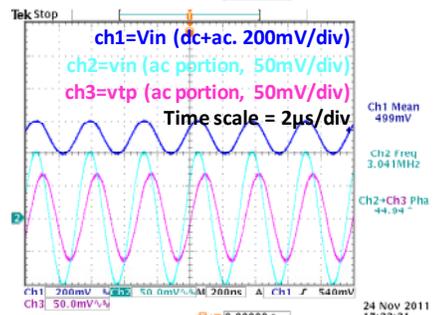
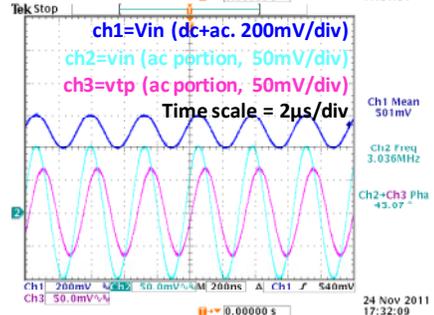
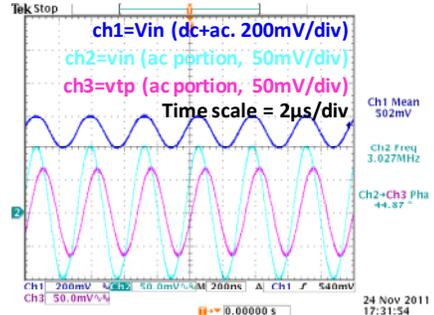
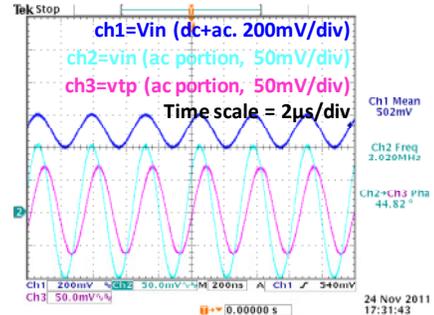
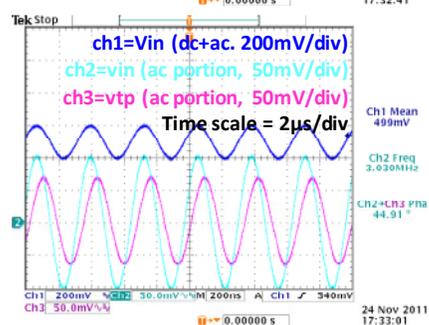
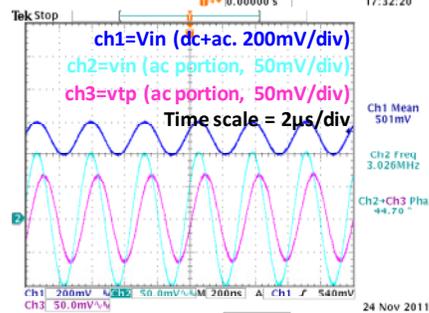
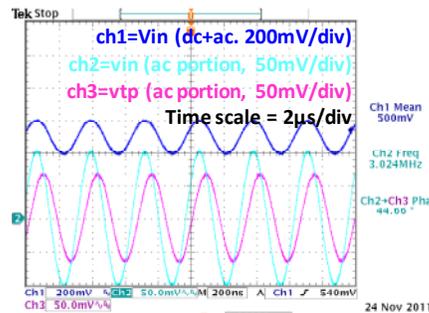


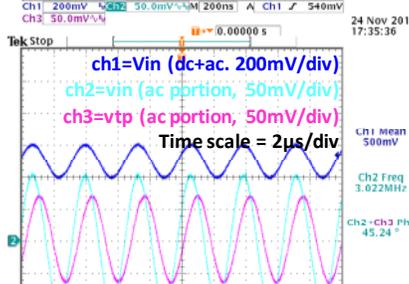
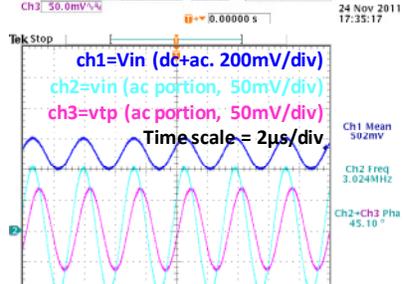
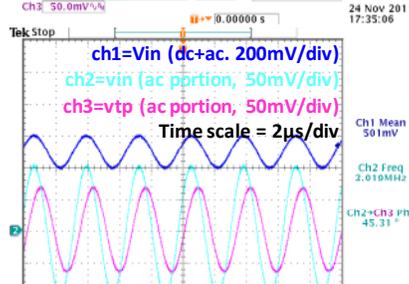
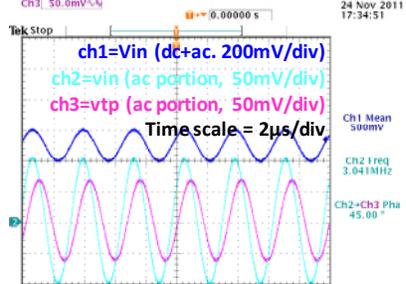
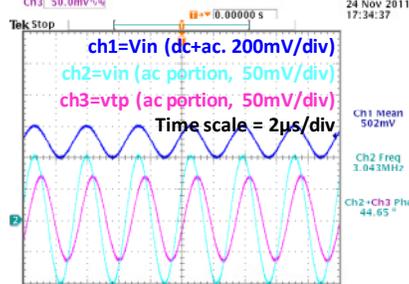
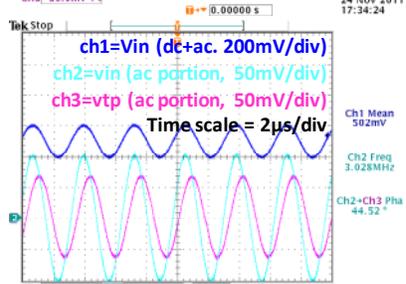
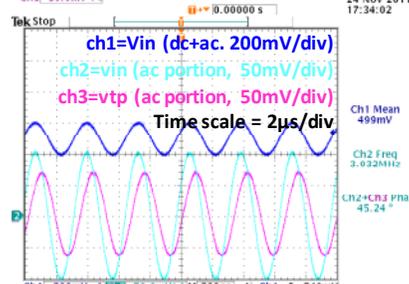
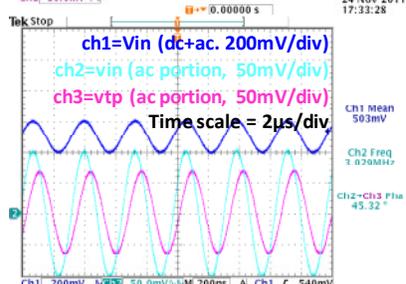
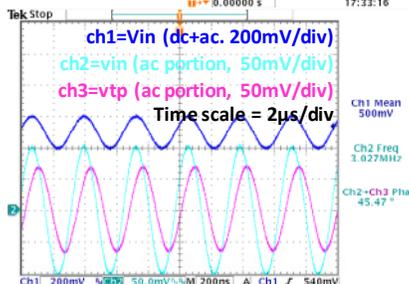
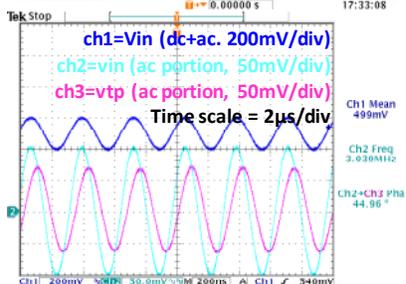
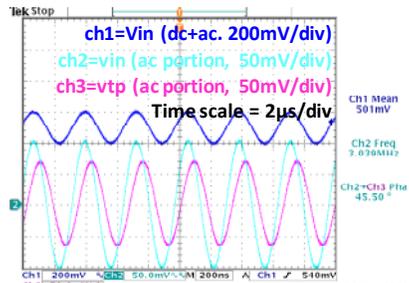
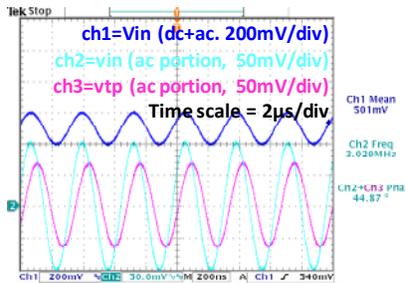
# testsignal PADONLY with 200mV 4k7 @0.5V

RIN= 4.692E+03

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.82 | 3.029E+06 | 1.11E-11 |
| 2          | 44.87 | 3.027E+06 | 1.12E-11 |
| 3          | 45.07 | 3.036E+06 | 1.12E-11 |
| 4          | 44.66 | 3.024E+06 | 1.11E-11 |
| 5          | 44.94 | 3.041E+06 | 1.11E-11 |
| 6          | 44.70 | 3.026E+06 | 1.11E-11 |
| 7          | 45.02 | 3.023E+06 | 1.12E-11 |
| 8          | 44.91 | 3.030E+06 | 1.12E-11 |
| 9          | 44.87 | 3.029E+06 | 1.11E-11 |
| 10         | 45.50 | 3.039E+06 | 1.14E-11 |
| 11         | 44.96 | 3.039E+06 | 1.11E-11 |
| 12         | 45.47 | 3.027E+06 | 1.14E-11 |
| 13         | 45.32 | 3.029E+06 | 1.13E-11 |
| 14         | 45.24 | 3.032E+06 | 1.13E-11 |
| 15         | 44.52 | 3.028E+06 | 1.10E-11 |
| 16         | 44.65 | 3.043E+06 | 1.10E-11 |
| 17         | 45.00 | 3.041E+06 | 1.12E-11 |
| 18         | 45.31 | 3.019E+06 | 1.14E-11 |
| 19         | 45.10 | 3.024E+06 | 1.13E-11 |
| 20         | 45.24 | 3.022E+06 | 1.13E-11 |

Average 45.01 3.030E+06 1.120E-11  
 STD 0.27 7.096E+03 1.128E-13



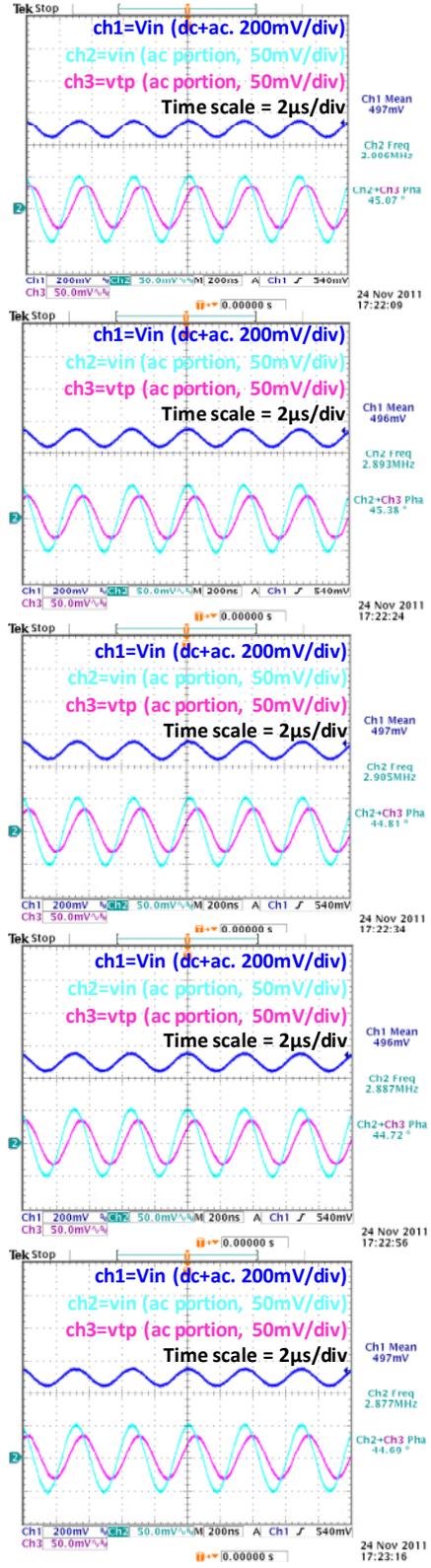
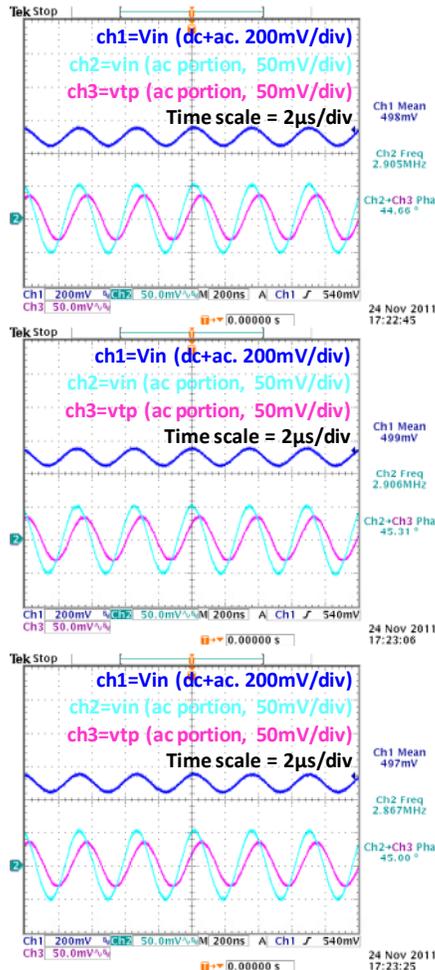


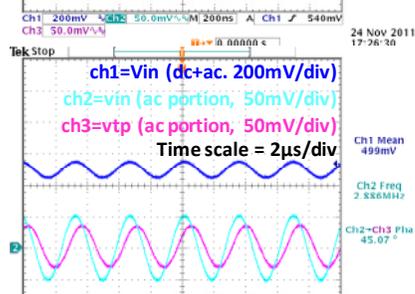
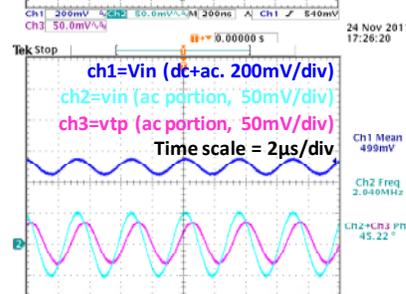
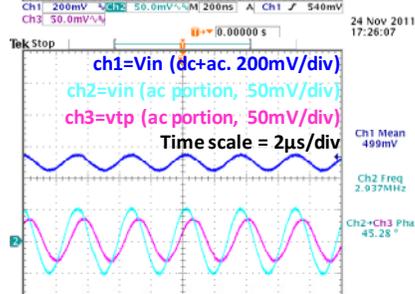
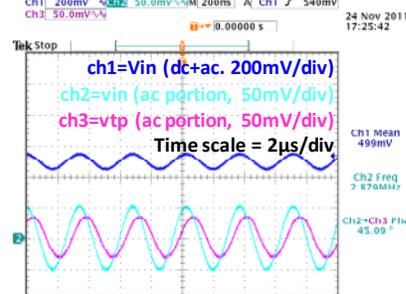
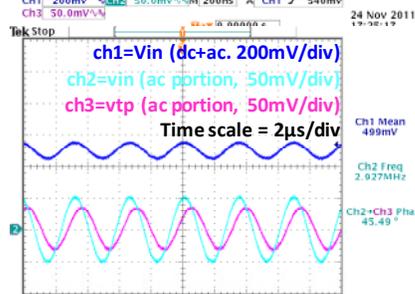
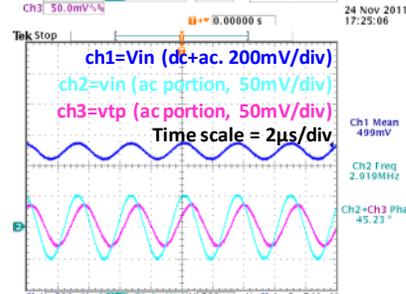
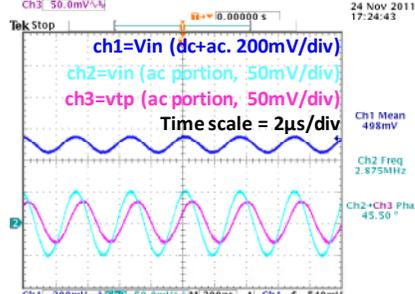
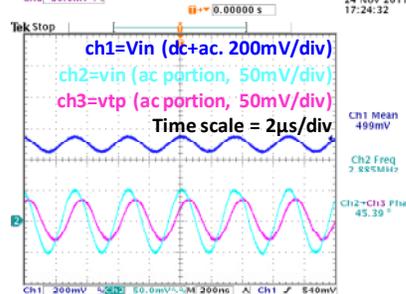
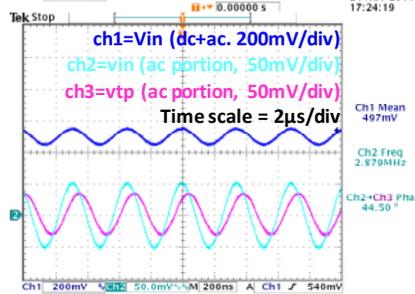
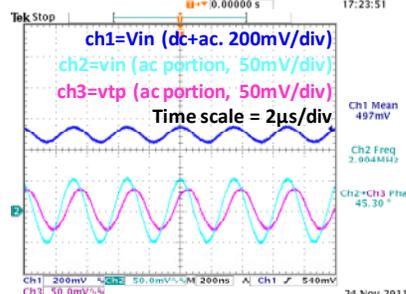
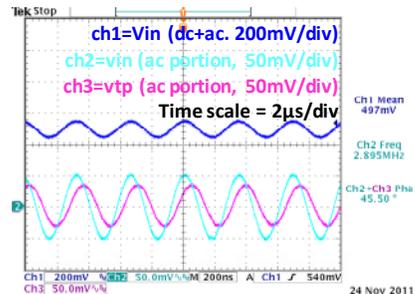
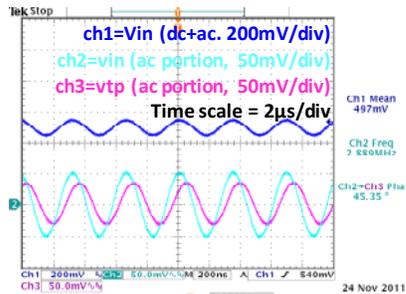
# testsignal noQFG with 100mV 4k7 @0.5V

RIN= 4.692E+03

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.07 | 2.906E+06 | 1.17E-11 |
| 2          | 45.38 | 2.893E+06 | 1.19E-11 |
| 3          | 44.81 | 2.905E+06 | 1.16E-11 |
| 4          | 44.66 | 2.905E+06 | 1.15E-11 |
| 5          | 44.72 | 2.887E+06 | 1.16E-11 |
| 6          | 45.31 | 2.906E+06 | 1.18E-11 |
| 7          | 44.69 | 2.877E+06 | 1.17E-11 |
| 8          | 45.00 | 2.867E+06 | 1.18E-11 |
| 9          | 45.35 | 2.889E+06 | 1.19E-11 |
| 10         | 45.50 | 2.895E+06 | 1.19E-11 |
| 11         | 45.30 | 2.904E+06 | 1.18E-11 |
| 12         | 44.50 | 2.879E+06 | 1.16E-11 |
| 13         | 45.39 | 2.885E+06 | 1.19E-11 |
| 14         | 45.50 | 2.875E+06 | 1.20E-11 |
| 15         | 45.23 | 2.919E+06 | 1.17E-11 |
| 16         | 45.49 | 2.972E+06 | 1.16E-11 |
| 17         | 45.09 | 2.879E+06 | 1.18E-11 |
| 18         | 45.28 | 2.937E+06 | 1.17E-11 |
| 19         | 45.22 | 2.940E+06 | 1.16E-11 |
| 20         | 45.07 | 2.886E+06 | 1.18E-11 |

Average 45.13 2.900E+06 1.175E-11  
 STD 0.31 2.571E+04 1.340E-13



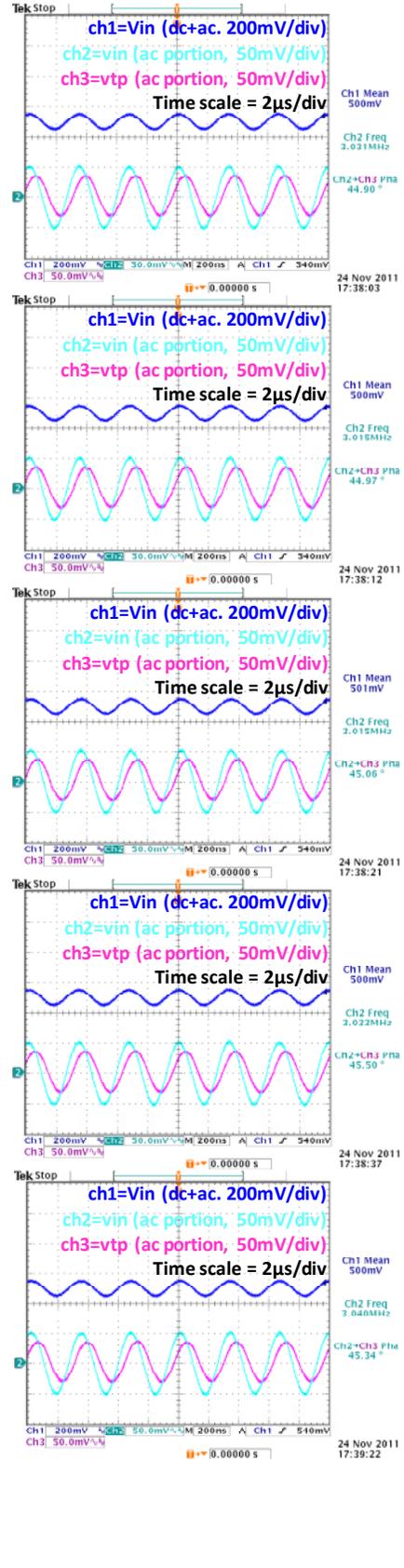
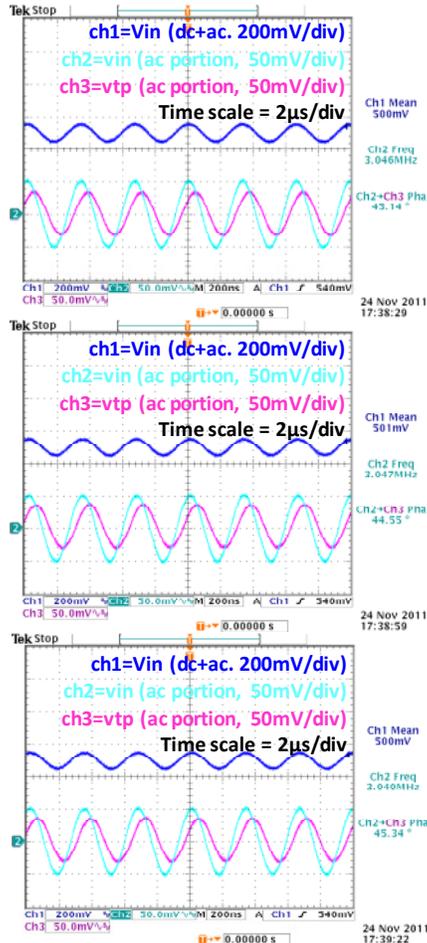


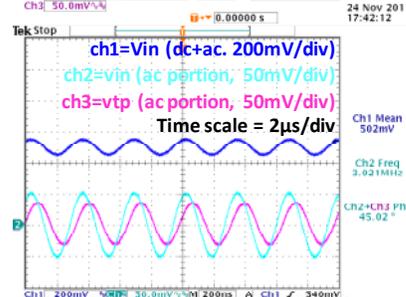
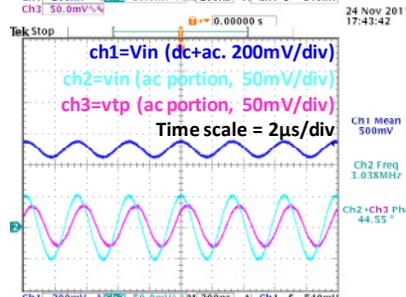
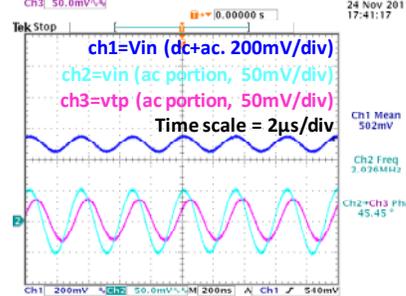
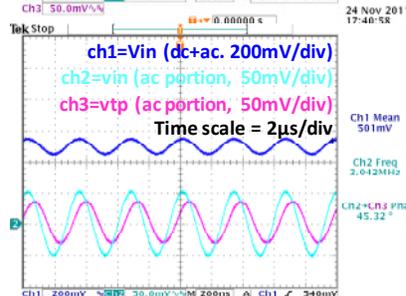
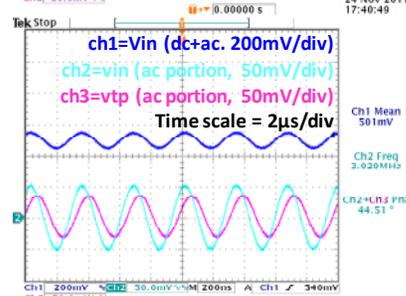
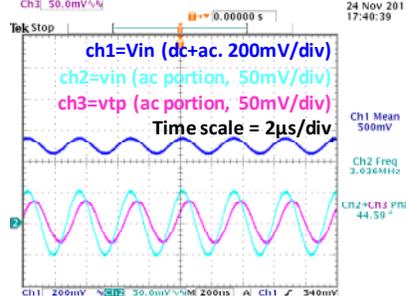
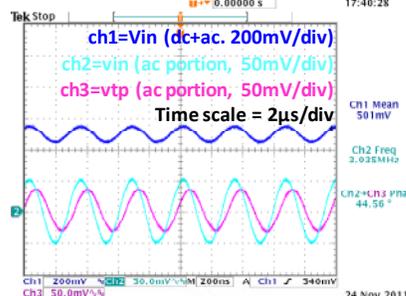
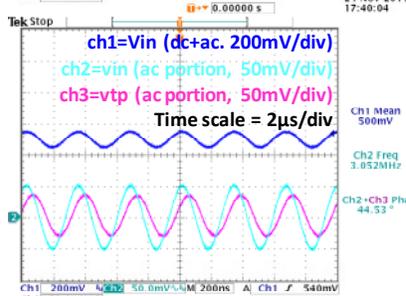
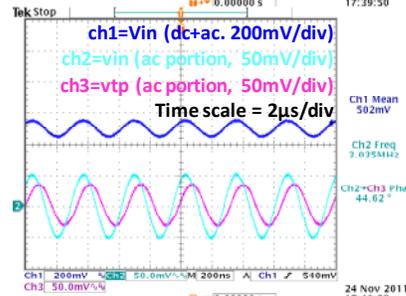
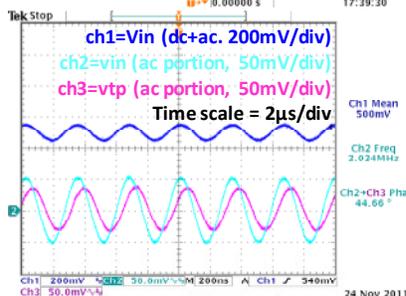
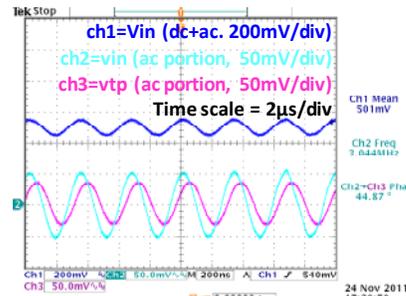
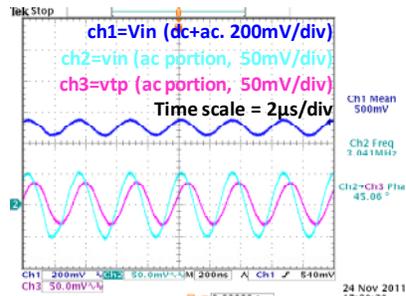
# testsignal PADONLY with 100mV 4k7 @0.5V

RIN= 4.692E+03

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.90 | 3.031E+06 | 1.12E-11 |
| 2          | 44.97 | 3.015E+06 | 1.12E-11 |
| 3          | 45.06 | 3.015E+06 | 1.13E-11 |
| 4          | 45.14 | 3.046E+06 | 1.12E-11 |
| 5          | 45.50 | 3.033E+06 | 1.14E-11 |
| 6          | 45.55 | 3.047E+06 | 1.13E-11 |
| 7          | 45.06 | 3.046E+06 | 1.12E-11 |
| 8          | 45.34 | 3.040E+06 | 1.13E-11 |
| 9          | 45.06 | 3.041E+06 | 1.12E-11 |
| 10         | 44.87 | 3.044E+06 | 1.11E-11 |
| 11         | 44.66 | 3.034E+06 | 1.10E-11 |
| 12         | 44.62 | 3.035E+06 | 1.10E-11 |
| 13         | 45.53 | 3.052E+06 | 1.13E-11 |
| 14         | 44.56 | 3.035E+06 | 1.10E-11 |
| 15         | 44.59 | 3.036E+06 | 1.10E-11 |
| 16         | 44.51 | 3.029E+06 | 1.10E-11 |
| 17         | 44.46 | 3.021E+06 | 1.10E-11 |
| 18         | 45.45 | 3.036E+06 | 1.13E-11 |
| 19         | 44.55 | 3.038E+06 | 1.10E-11 |
| 20         | 45.02 | 3.021E+06 | 1.12E-11 |

Average 44.97 3.035E+06 1.117E-11  
 STD 0.37 1.045E+04 1.337E-13



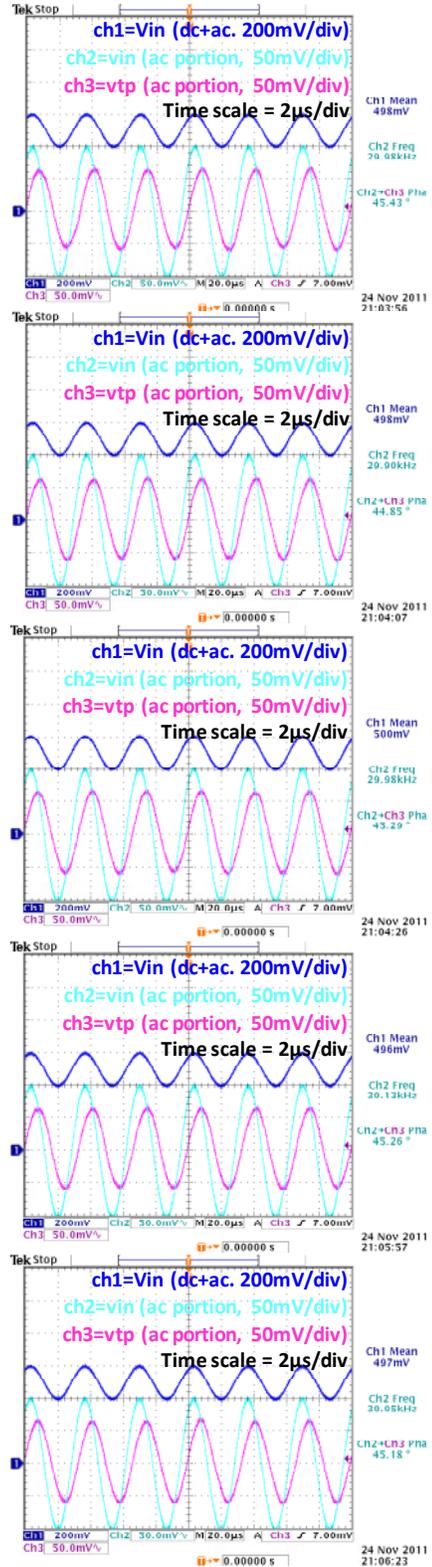
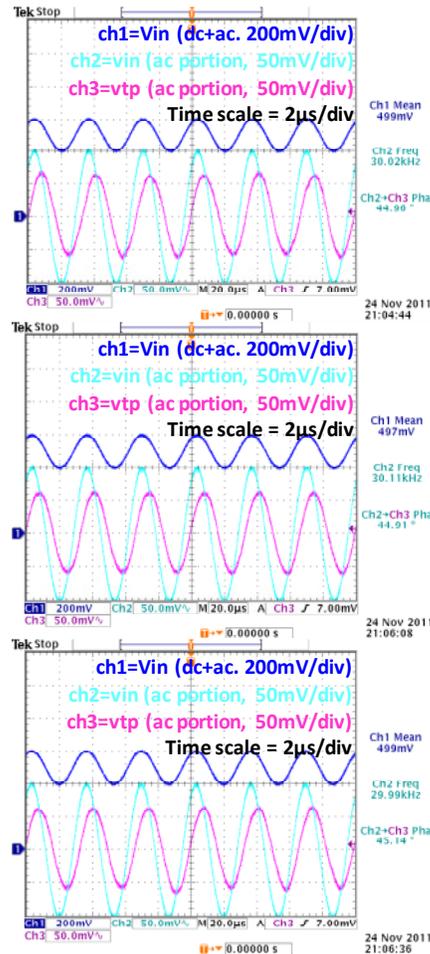


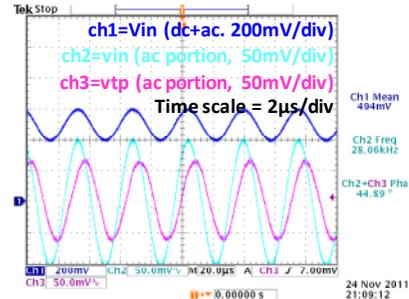
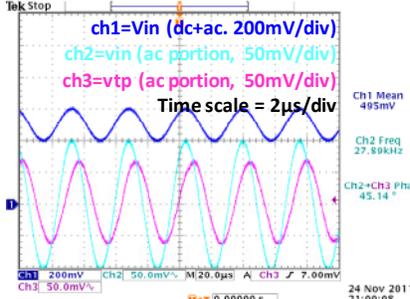
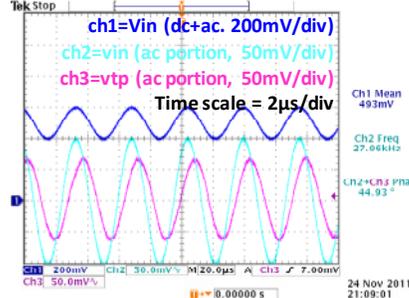
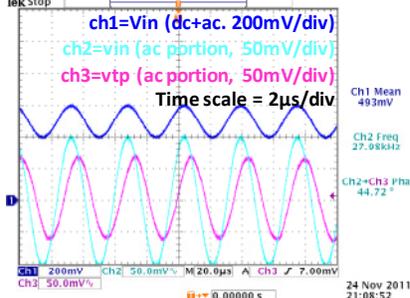
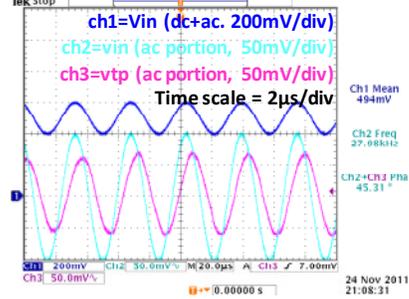
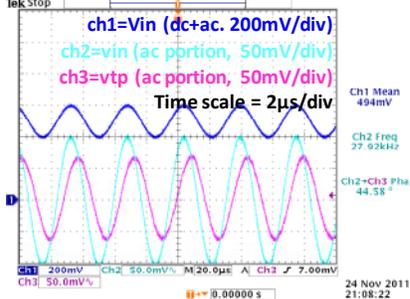
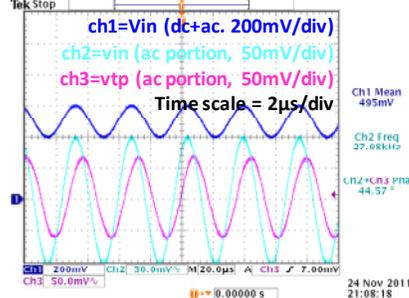
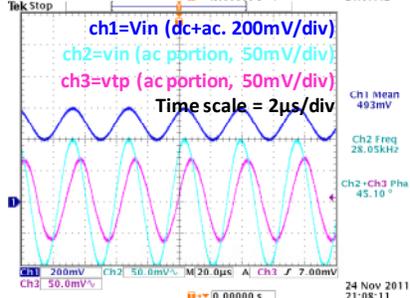
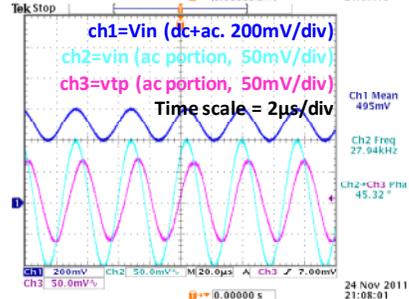
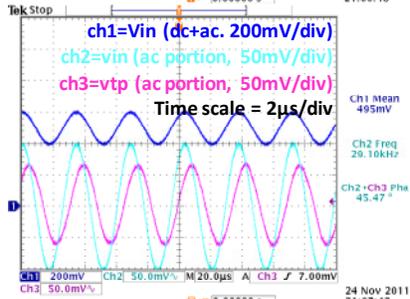
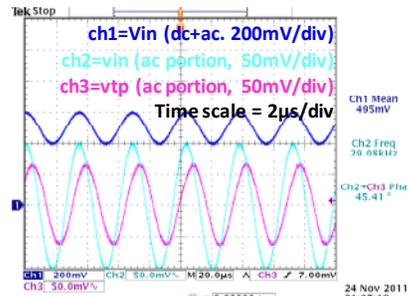
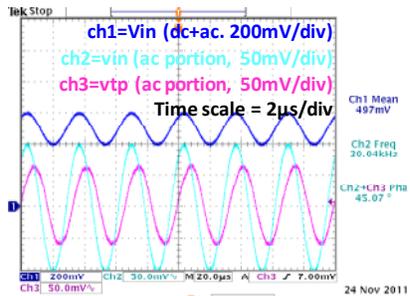
# testsignal noQFG5 with 200mVpp 470k @0.5VDC

RIN= 4.715E+05

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 45.43 | 2.998E+04 | 1.14E-11 |
| 2          | 44.85 | 2.990E+04 | 1.12E-11 |
| 3          | 45.29 | 2.998E+04 | 1.14E-11 |
| 4          | 44.96 | 3.002E+04 | 1.12E-11 |
| 5          | 45.26 | 3.013E+04 | 1.13E-11 |
| 6          | 44.91 | 3.011E+04 | 1.12E-11 |
| 7          | 45.18 | 3.005E+04 | 1.13E-11 |
| 8          | 45.14 | 2.999E+04 | 1.13E-11 |
| 9          | 45.07 | 3.004E+04 | 1.13E-11 |
| 10         | 45.41 | 2.908E+04 | 1.18E-11 |
| 11         | 45.47 | 2.910E+04 | 1.18E-11 |
| 12         | 45.32 | 2.794E+04 | 1.22E-11 |
| 13         | 45.10 | 2.805E+04 | 1.21E-11 |
| 14         | 44.57 | 2.798E+04 | 1.19E-11 |
| 15         | 44.58 | 2.792E+04 | 1.19E-11 |
| 16         | 45.31 | 2.798E+04 | 1.22E-11 |
| 17         | 44.72 | 2.798E+04 | 1.19E-11 |
| 18         | 44.93 | 2.796E+04 | 1.20E-11 |
| 19         | 45.14 | 2.789E+04 | 1.22E-11 |
| 20         | 44.89 | 2.806E+04 | 1.20E-11 |

Average 45.08 2.901E+04 1.168E-11  
 STD 0.27 9.992E+02 3.815E-13



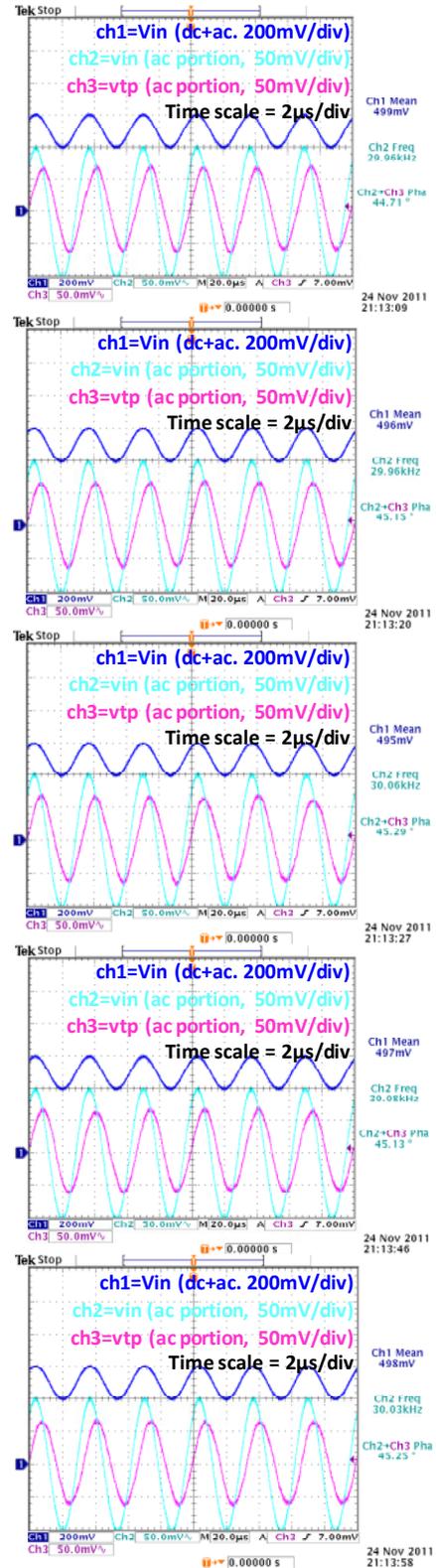
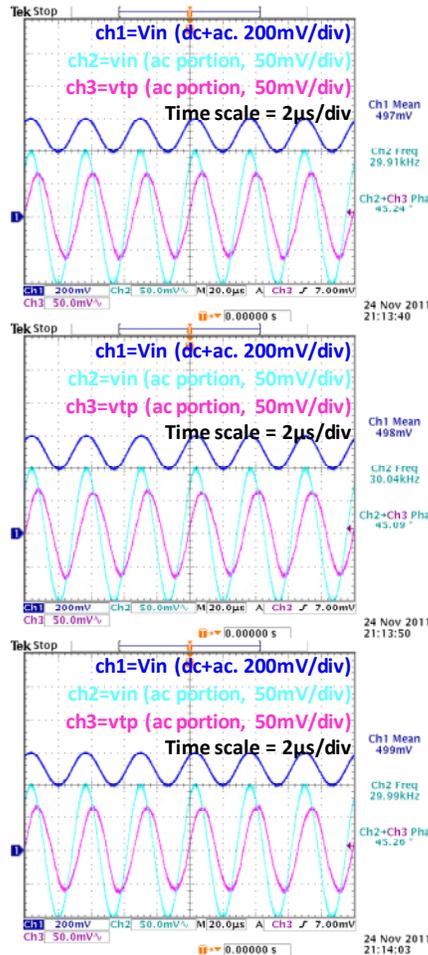


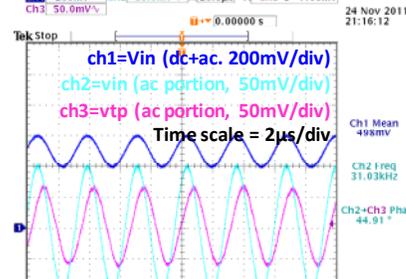
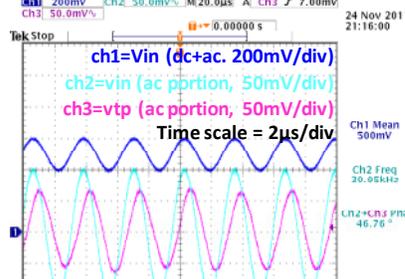
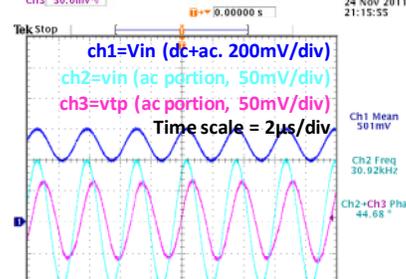
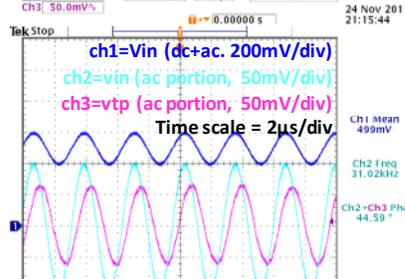
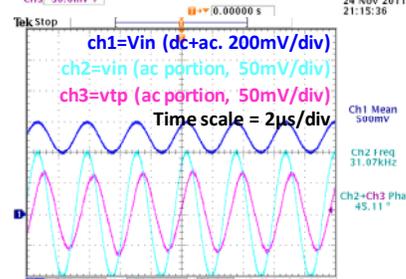
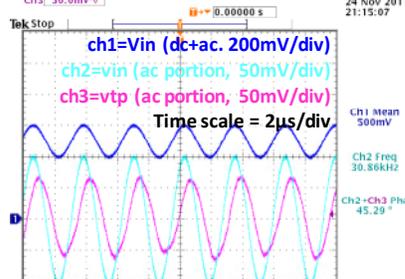
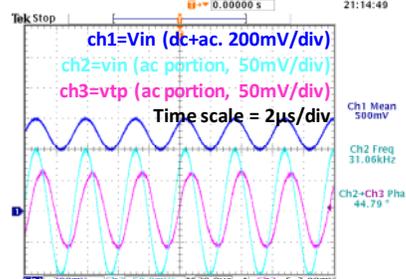
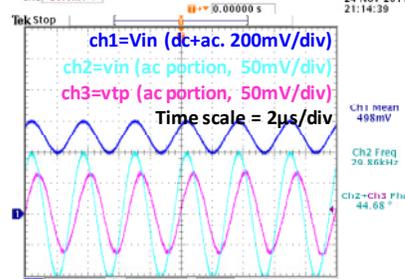
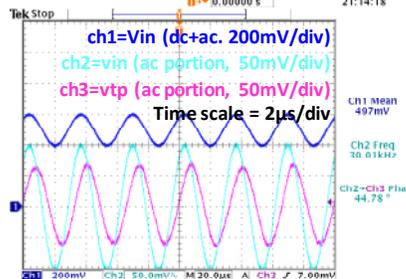
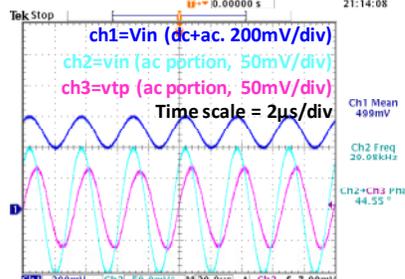
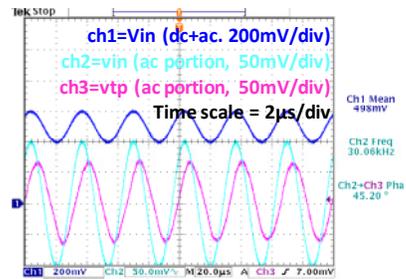
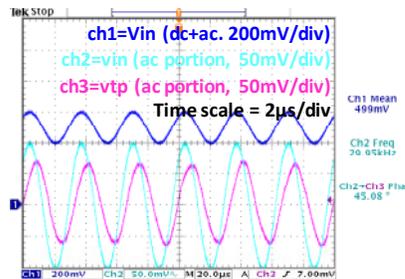
# testsignal PADONLY with 200mVpp 470k @0.5VDC

RIN= 4.715E+05

| Sample No. | phase | f         | c        |
|------------|-------|-----------|----------|
| 1          | 44.71 | 2.996E+04 | 1.12E-11 |
| 2          | 45.15 | 2.996E+04 | 1.13E-11 |
| 3          | 45.29 | 3.006E+04 | 1.13E-11 |
| 4          | 45.24 | 2.991E+04 | 1.14E-11 |
| 5          | 45.13 | 3.008E+04 | 1.13E-11 |
| 6          | 45.09 | 3.004E+04 | 1.13E-11 |
| 7          | 45.25 | 3.003E+04 | 1.13E-11 |
| 8          | 45.26 | 2.999E+04 | 1.14E-11 |
| 9          | 45.08 | 2.995E+04 | 1.13E-11 |
| 10         | 45.20 | 3.006E+04 | 1.13E-11 |
| 11         | 44.55 | 2.998E+04 | 1.11E-11 |
| 12         | 44.78 | 3.001E+04 | 1.12E-11 |
| 13         | 44.68 | 2.986E+04 | 1.12E-11 |
| 14         | 44.79 | 3.106E+04 | 1.08E-11 |
| 15         | 45.29 | 3.086E+04 | 1.10E-11 |
| 16         | 45.11 | 3.107E+04 | 1.09E-11 |
| 17         | 44.59 | 3.102E+04 | 1.07E-11 |
| 18         | 44.68 | 3.092E+04 | 1.08E-11 |
| 19         | 46.76 | 3.095E+04 | 1.16E-11 |
| 20         | 44.91 | 3.103E+04 | 1.08E-11 |

Average 45.08 3.034E+04 1.116E-11  
 STD 0.47 4.918E+02 2.385E-13





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